# Cheatsheet - Comparison and Non-Comparison Sorting Algorithms

Fabio Lama – fabio.lama@pm.me

#### 1. About

This cheatsheet provides an overview of some common sorting algorithms.

### 2. Comparison Sort Overview

Name	Worst case complexity	Best case complexity
Bubble	$\Thetaig(N^2ig)$	$\Theta(N)$
Insertion	$\Thetaig(N^2ig)$	$\Theta(N)$
Selection	$\Theta(N^2)$	$\Thetaig(N^2ig)$
Quicksort	$\Theta(N^2)$	$\Theta(N  imes \log N)$
Mergesort	$\Theta(N  imes \log N)$	$\Theta(N  imes \log N)$
Radix Sort	$\Theta(d imes N)$	$\Theta(d imes N)$
Bucket Sort	$\Theta(N^2)$	$\Theta\left(N + \frac{N}{b} + b\right)$

Note that the d in Radix Sort is the number of digits and b in Bucket Sort is the number of buckets. Because comparison sorts must compare pairs of elements, they cannot run faster than  $N \times \log N$ .

## 3. Note: Sorting Algorithm Visualizer

It's recommended to lookup a sorting algorithm visualizer online, such as: https://www.toptal.com/developers/sorting-algorithms

## 4. Bubble Sort

```
1. function BubbleSort(A, N)
       \mathtt{swapped} = true
       while (swapped) do
          \mathtt{swapped} = false
 4.
          \quad \mathbf{for} \ \ 0 \leq i < N-1 \ \ \mathbf{do}
 5.
            if (A[i] > A[i+1]) then
               swap(A[i], A[i+1])
               \mathtt{swapped} = true
 8.
             end if
 9.
          end for
10.
          N = N - 1
11.
       end while
12.
13.
       return A
14. end function
```

#### 4.1. Time Complexity

The **best case** for bubble sort is:

$$T(N) = C_0 \times N + C_1$$

Additionally:

- T(N) is O(N),  $O(N^2)$  and  $O(N^3)$ , etc.
- T(N) is  $\Omega(N)$ ,  $\Omega(\log N)$  and  $\Omega(1)$ , etc.
- T(N) is  $\Theta(N)$

The worst case for bubble sort is:

$$T(N) = C_0 \times N^2 + C_1 \times N + C_2.$$

Additionally:

```
• T(N) is O(N^2) and O(N^3), etc.
• T(N) is \Omega(N^2), \Omega(\log N) and \Omega(1), etc.
• T(N) is \Theta(N^2)
```

### 5. Insertion Sort

```
1. function InsertionSort(A, N)
      for 1 \leq j \leq N-1 do
         \mathtt{ins} = A[j]
         i = j - 1
 4.
         while (i \ge 0 \text{ and ins } < A[i]) do
 5.
           A[i+1] = A[i]
 6.
           i = i - 1
         end while
 8.
         A[i+1] = \mathtt{ins}
 9.
10.
      end for
```

#### 6. Selection Sort

11. end function

```
1. function SelectionSort(A, N)
2. for 0 \le i < N-1 do
3. min = pos_{\min}(A, i, N-1)
4. swap(A[i], A[\min])
5. end for
```

function Quicksort(A, low, high)
 if low < high then</li>

6. end function

The function  $pos\_min(A, a, b)$  returns the position of the minimum value between positions a and b (both inclusive) in array A.

### 7. Quicksort

```
p = partition(A, low, high)
 3.
         Quicksort(A, low, p-1)
 4.
         \operatorname{Quicksort}(A, {\tt p+1}, {\tt high})
 5.
      end if
 7. end function
 8. function partition(A, low, high)
      pivot = A[high]
10.
      i = low - 1
      for j = low to high - 1 do
11.
         if A[j] < pivot then
12.
         \mathbf{i} = \mathbf{i} + 1
13.
         swap(A[i], A[j])
14.
15.
      end for
      swap(A[i+1], A[high])
16.
      return i+1
17.
```

#### 7.1. Explanation

18. end function

The function  $\mathbf{partition}(A, \mathbf{low}, \mathbf{high})$  selects a pivot element (usually the last element in the current segment of the array). It then rearranges the elements in the array such that all elements less than the pivot are moved to the left of the pivot and all elements greater than or equal to the pivot are moved to the right. The pivot is then placed in its correct position, and the index of the pivot is returned.

## 8. Mergesort

```
1. function MergeSort(A, low, high)
2. if (low < high)
3. mid = low + floor((high - 1) \div 2)
4. MergeSort(A, low, mid)
5. MergeSort(A, mid + low, high)
6. Merge(A, low, mid, high)
7. end if
```

The function Merge creates two arrays of both halves (left and right) and then merges them to produce a single, sorted array.

### 9. Radix Sort

8. end function

```
1. function RadixSort(A, N)
        \max = \operatorname{findMax}(A, N)
        exp = 1
 3.
        while max \div exp > 0 do
 4.
           CountSort(A, N, exp)
 5.
           \exp=\exp	imes 10
 6.
        end while
 8. end function
 9. function CountSort(A, N, exp)
        output = new array of size N
10.
11.
        count = new array of size 10 initialized to 0
        for 0 \le i < N do
12.
           \mathtt{index} = (A[i] \div \mathtt{exp}) \% 10
13.
14.
           \mathtt{count}[\mathtt{index}] = \mathtt{count}[\mathtt{index}] + 1
        end for
15.
        for 1 \le i < 10 do
16.
           \mathtt{count}[i] = \mathtt{count}[i] + \mathtt{count}[i-1]
17.
        end for
18.
        \mathbf{i} = N - 1
19.
        while i \geq 0 do
20.
           \mathtt{index} = (A[i] \div \mathtt{exp}) \% 10
21.
           \mathtt{output}[\mathtt{count}[\mathtt{index}] - 1] = A[i]
22.
           \mathtt{count}[\mathtt{index}] = \mathtt{count}[\mathtt{index}] - 1
23.
           i = i - 1
24.
25.
        end while
        for 0 \le i < N do
26.
27.
           A[i] = \mathtt{output}[i]
        end for
28.
```

## 10. Bucket Sort

29. end function

```
    function BucketSort(A, N, max)
    buckets = new array of empty lists of size N
    for i = 0 to N - 1 do
    index = floor(A[i] ÷ (max + 1) × N)
    append(buckets[index], A[i])
    end for
    for i = 0 to N - 1 do
```

```
8.
             {\tt InsertionSort}({\tt buckets}[i])
         end for
 9.
         k = 0
10.
         \mathbf{for} \ i=0 \ \mathbf{to} \ N-1 \ \mathbf{do}
11.
             \mathbf{for} \ \ j = 0 \ \ \mathbf{to} \ \ \mathrm{len}(\mathtt{buckets}[i]) - 1 \ \ \mathbf{do}
12.
                 A[\mathtt{k}] = \mathtt{buckets}[i][j]
13.
                 \mathtt{k}=\mathtt{k}+1
14.
15.
              end for
          end for
16.
```

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17. end function