



Homework 8

Vertex Cover Problem

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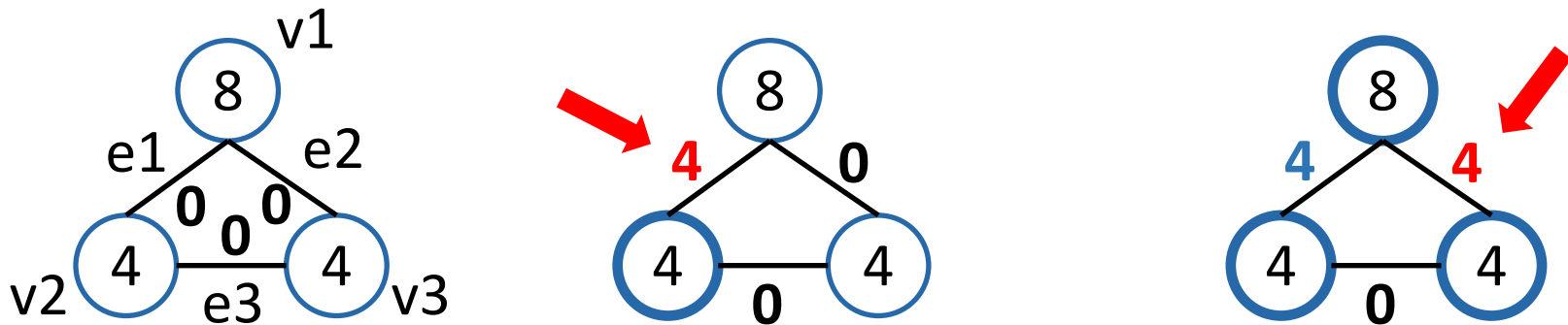


Exercise 7-1

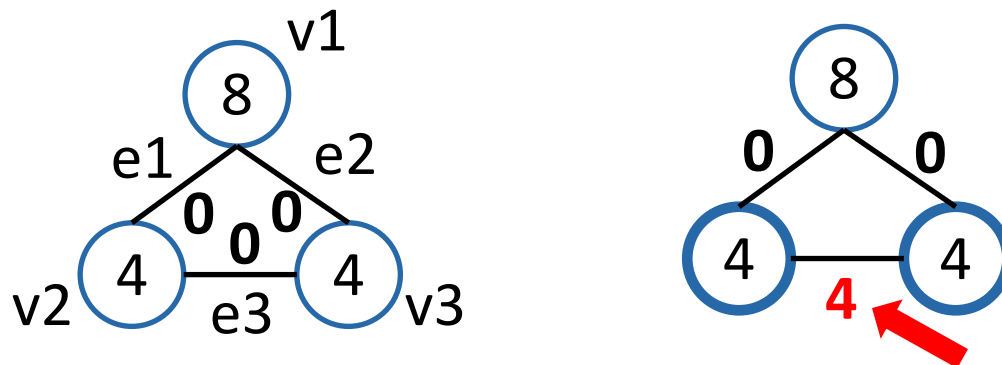
- An example where different results are obtained depending on the order of edges

Simple example:

Example 1, order={e1,e2,e3}, $S_1=\{v1,v2,v3\}$, $w(S_1)=16$



Example 2, order={e3,e2,e1}, $S_2=\{v2,v3\}$, $w(S_2)=8$



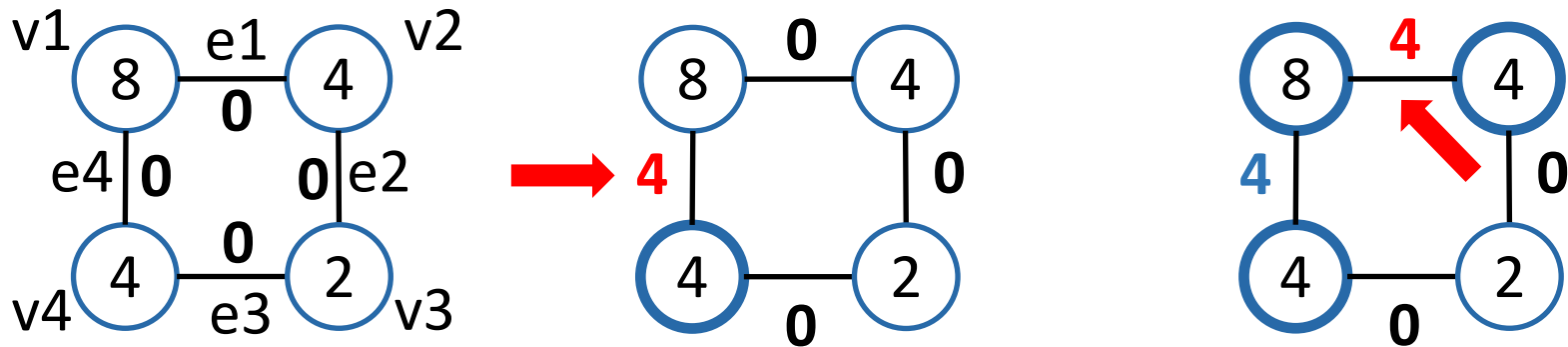


Exercise 7-2

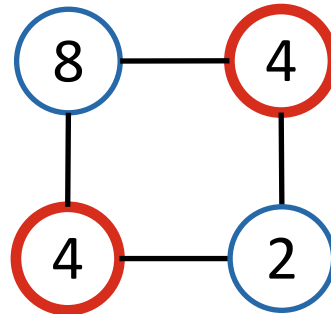
- An example where a good solution is not obtained by the pricing method

Simple example: $w=2w^*$

The pricing method, $\text{order}=\{e_4, e_1, e_2, e_3\}, S=\{v_1, v_2, v_4\}, w(S)=16$



The optimal solution, $S^=\{v_2, v_4\}, w(S^*)=8$*



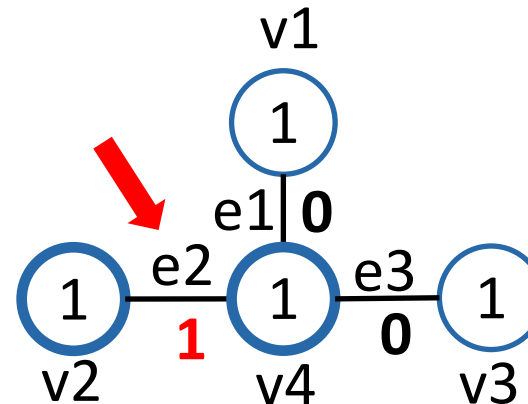
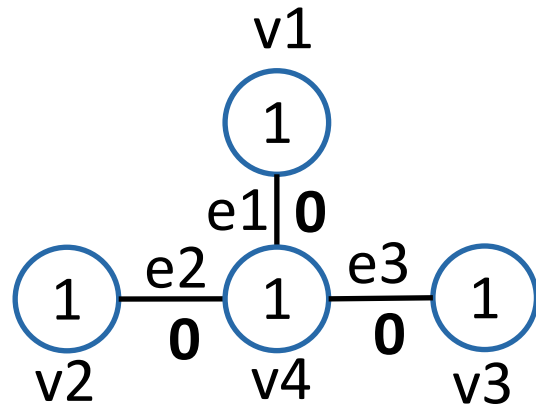


Exercise 7-3

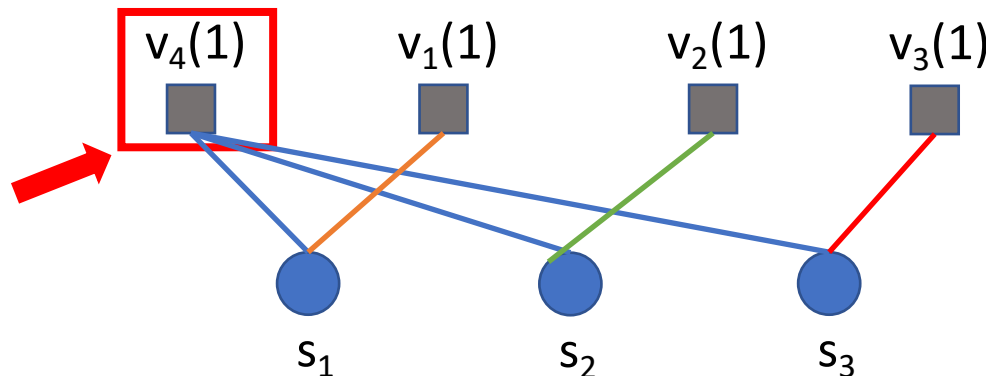
- An example where a better result is always obtained by the greedy set cover algorithm

Simple example:

The pricing method, $S=\{v_4, v_2 \text{ or } v_1 \text{ or } v_3\}$, $w(S)=2$



The greedy set cover algorithm, $S^=\{v_4\}$, $w(S^*)=1<2$*



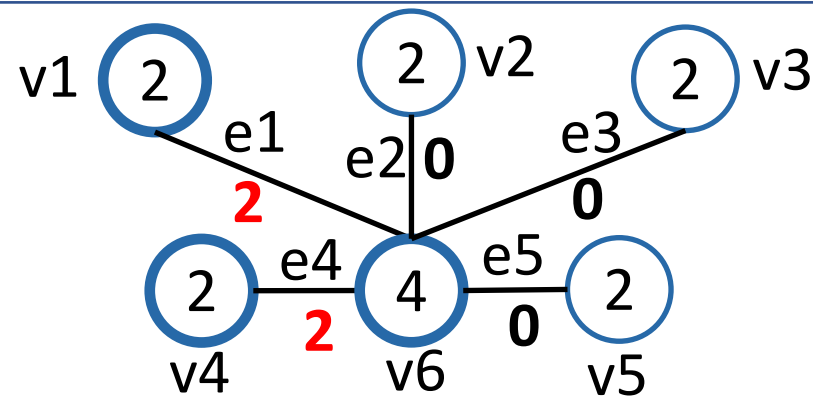
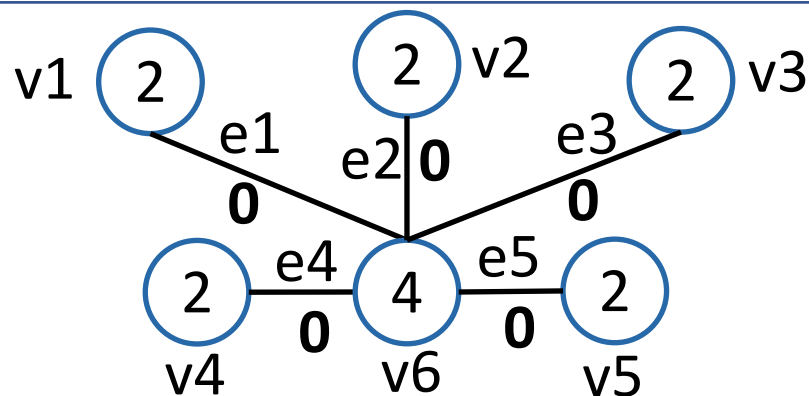


Exercise 7-4

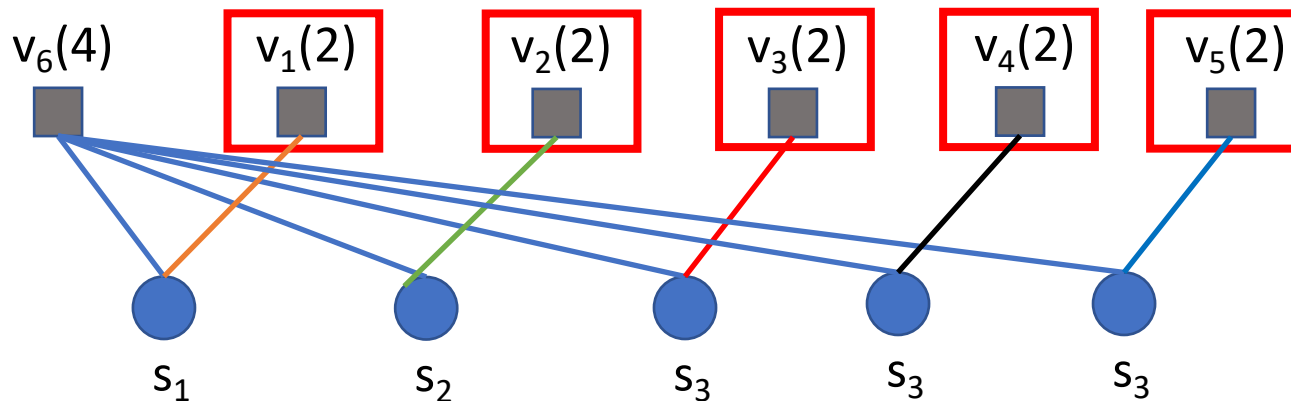
■ An example where a better result is always obtained by the pricing method

Simple example:

The pricing method, $w(S^)=8$*



The greedy set covet algorithm, $w(S)=10>8$





Thanks!

**Please contact me with email
if you have any problem**

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