

Assume Tables and Schema

Sample Tables:

1. **Employees:** Contains employee information.
 - **Attributes:** emp_id, name, age, department_id, salary
2. **Departments:** Contains department details.
 - **Attributes:** dept_id, dept_name, location
3. **Projects:** Contains project details.
 - **Attributes:** proj_id, proj_name, dept_id, budget
4. **Works_On:** Contains details of employees working on projects.
 - **Attributes:** emp_id, proj_id, hours
5. **Salaries:** Contains historical salary data.
 - **Attributes:** emp_id, year, annual_salary

Relational Algebra Queries

Selection (σ)

1. $\sigma(\text{age} > 30)(\text{Employees})$
2. $\sigma(\text{dept_name} = \text{'HR'})(\text{Departments})$
3. $\sigma(\text{salary} > 70000)(\text{Employees})$
4. $\sigma(\text{location} = \text{'New York'})(\text{Departments})$
5. $\sigma(\text{budget} > 100000)(\text{Projects})$

Projection (π)

6. $\pi(\text{name}, \text{age})(\text{Employees})$
7. $\pi(\text{dept_name})(\text{Departments})$
8. $\pi(\text{proj_name}, \text{budget})(\text{Projects})$
9. $\pi(\text{emp_id}, \text{salary})(\text{Employees})$
10. $\pi(\text{location})(\text{Departments})$

Union (\cup)

11. $\pi(\text{emp_id}, \text{salary})(\text{Employees}) \cup \pi(\text{emp_id}, \text{annual_salary})(\text{Salaries})$
12. $\pi(\text{dept_id}, \text{location})(\text{Departments}) \cup \pi(\text{dept_id}, \text{dept_name})(\text{Departments})$
13. $\pi(\text{emp_id}, \text{proj_id})(\text{Works_On}) \cup \pi(\text{emp_id}, \text{proj_id})(\text{Works_On})$
14. $\pi(\text{dept_id})(\text{Departments}) \cup \pi(\text{dept_id})(\text{Projects})$
15. $\pi(\text{name})(\text{Employees}) \cup \pi(\text{proj_name})(\text{Projects})$

Set Difference (-)

- 16. $\pi(\text{emp_id})(\text{Employees}) - \pi(\text{emp_id})(\text{Works_On})$
- 17. $\pi(\text{dept_id})(\text{Departments}) - \pi(\text{dept_id})(\text{Projects})$
- 18. $\pi(\text{proj_id})(\text{Projects}) - \pi(\text{proj_id})(\text{Works_On})$
- 19. $\pi(\text{emp_id})(\text{Employees}) - \pi(\text{emp_id})(\text{Salaries})$
- 20. $\pi(\text{location})(\text{Departments}) - \pi(\text{location})(\text{Departments})$

Cartesian Product (\times)

- 21. $\text{Employees} \times \text{Departments}$
- 22. $\text{Projects} \times \text{Departments}$
- 23. $\text{Employees} \times \text{Projects}$
- 24. $\text{Departments} \times \text{Works_On}$
- 25. $\text{Salaries} \times \text{Works_On}$

Rename (ρ)

- 26. $\rho(\text{Emp}(\text{emp_id}, \text{name}, \text{age}, \text{dept_id}, \text{salary}))(\text{Employees})$
- 27. $\rho(\text{Dept}(\text{dept_id}, \text{dept_name}, \text{location}))(\text{Departments})$
- 28. $\rho(\text{Proj}(\text{proj_id}, \text{proj_name}, \text{dept_id}, \text{budget}))(\text{Projects})$
- 29. $\rho(\text{Work}(\text{emp_id}, \text{proj_id}, \text{hours}))(\text{Works_On})$
- 30. $\rho(\text{Sal}(\text{emp_id}, \text{year}, \text{annual_salary}))(\text{Salaries})$

Join (\bowtie)

- 31. $\text{Employees} \bowtie \text{dept_id} = \text{dept_id} \text{ Departments}$
- 32. $\text{Projects} \bowtie \text{dept_id} = \text{dept_id} \text{ Departments}$
- 33. $\text{Works_On} \bowtie \text{emp_id} = \text{emp_id} \text{ Employees}$
- 34. $\text{Employees} \bowtie \text{emp_id} = \text{emp_id} \text{ Salaries}$
- 35. $\text{Projects} \bowtie \text{dept_id} = \text{dept_id} \text{ Works_On}$

Natural Join (\bowtie)

- 36. $\text{Employees} \bowtie \text{Departments}$
- 37. $\text{Projects} \bowtie \text{Departments}$
- 38. $\text{Works_On} \bowtie \text{Employees}$
- 39. $\text{Employees} \bowtie \text{Salaries}$
- 40. $\text{Projects} \bowtie \text{Works_On}$

Division (\div)

- 41. $\pi(\text{emp_id}, \text{proj_id})(\text{Works_On}) \div \pi(\text{proj_id})(\text{Projects})$
- 42. $\pi(\text{emp_id}, \text{dept_id})(\text{Employees}) \div \pi(\text{dept_id})(\text{Departments})$

43. $\pi(\text{emp_id}, \text{proj_id})(\text{Works_On}) \div \pi(\text{proj_id})(\text{Works_On})$
44. $\pi(\text{emp_id}, \text{proj_id})(\text{Works_On}) \div \pi(\text{emp_id})(\text{Employees})$
45. $\pi(\text{proj_id})(\text{Projects}) \div \pi(\text{dept_id})(\text{Departments})$

Intersection (\cap)

46. $\pi(\text{emp_id})(\text{Employees}) \cap \pi(\text{emp_id})(\text{Works_On})$
47. $\pi(\text{dept_id})(\text{Departments}) \cap \pi(\text{dept_id})(\text{Projects})$
48. $\pi(\text{proj_id})(\text{Projects}) \cap \pi(\text{proj_id})(\text{Works_On})$
49. $\pi(\text{emp_id})(\text{Employees}) \cap \pi(\text{emp_id})(\text{Salaries})$
50. $\pi(\text{location})(\text{Departments}) \cap \pi(\text{location})(\text{Departments})$

SQL Queries

Basic SELECT

1. SELECT * FROM Employees WHERE age > 30;
2. SELECT * FROM Departments WHERE dept_name = 'HR';
3. SELECT * FROM Employees WHERE salary > 70000;
4. SELECT * FROM Departments WHERE location = 'New York';
5. SELECT * FROM Projects WHERE budget > 100000;

SELECT with Specific Columns

6. SELECT name, age FROM Employees;
7. SELECT dept_name FROM Departments;
8. SELECT proj_name, budget FROM Projects;
9. SELECT emp_id, salary FROM Employees;
10. SELECT location FROM Departments;

UNION

11. SELECT emp_id, salary FROM Employees UNION SELECT emp_id, annual_salary FROM Salaries;
12. SELECT dept_id, location FROM Departments UNION SELECT dept_id, dept_name FROM Departments;
13. SELECT emp_id, proj_id FROM Works_On UNION SELECT emp_id, proj_id FROM Works_On;
14. SELECT dept_id FROM Departments UNION SELECT dept_id FROM Projects;
15. SELECT name FROM Employees UNION SELECT proj_name FROM Projects;

EXCEPT (Set Difference)

16. SELECT emp_id FROM Employees EXCEPT SELECT emp_id FROM Works_On;
17. SELECT dept_id FROM Departments EXCEPT SELECT dept_id FROM Projects;
18. SELECT proj_id FROM Projects EXCEPT SELECT proj_id FROM Works_On;
19. SELECT emp_id FROM Employees EXCEPT SELECT emp_id FROM Salaries;
20. SELECT location FROM Departments EXCEPT SELECT location FROM Departments;

JOIN

21. SELECT * FROM Employees INNER JOIN Departments ON Employees.department_id = Departments.dept_id;
22. SELECT * FROM Projects INNER JOIN Departments ON Projects.dept_id = Departments.dept_id;
23. SELECT * FROM Works_On INNER JOIN Employees ON Works_On.emp_id = Employees.emp_id;
24. SELECT * FROM Employees INNER JOIN Salaries ON Employees.emp_id = Salaries.emp_id;
25. SELECT * FROM Projects INNER JOIN Works_On ON Projects.proj_id = Works_On.proj_id;

LEFT JOIN

26. SELECT * FROM Employees LEFT JOIN Departments ON Employees.department_id = Departments.dept_id;
27. SELECT * FROM Projects LEFT JOIN Departments ON Projects.dept_id = Departments.dept_id;
28. SELECT * FROM Works_On LEFT JOIN Employees ON Works_On.emp_id = Employees.emp_id;
29. SELECT * FROM Employees LEFT JOIN Salaries ON Employees.emp_id = Salaries.emp_id;
30. SELECT * FROM Projects LEFT JOIN Works_On ON Projects.proj_id = Works_On.proj_id;

RIGHT JOIN

31. SELECT * FROM Employees RIGHT JOIN Departments ON Employees.department_id = Departments.dept_id;
32. SELECT * FROM Projects RIGHT JOIN Departments ON Projects.dept_id = Departments.dept_id;
33. SELECT * FROM Works_On RIGHT JOIN Employees ON Works_On.emp_id = Employees.emp_id;
34. SELECT * FROM Employees RIGHT JOIN Salaries ON Employees.emp_id = Salaries.emp_id;
35. SELECT * FROM Projects RIGHT JOIN Works_On ON Projects.proj_id = Works_On.proj_id;

FULL OUTER JOIN

```
36. SELECT * FROM Employees FULL OUTER JOIN Departments ON
    Employees.department_id = Departments.dept_id;
37. SELECT * FROM Projects FULL OUTER JOIN Departments ON
    Projects.dept_id = Departments.dept_id;
38. SELECT * FROM Works_On FULL OUTER JOIN Employees ON
    Works_On.emp_id = Employees.emp_id;
39. SELECT * FROM Employees FULL OUTER JOIN Salaries ON
    Employees.emp_id = Salaries.emp_id;
40. SELECT * FROM Projects FULL OUTER JOIN Works_On ON
    Projects.proj_id = Works_On.proj_id;
```

Subqueries

```
41. SELECT name FROM Employees WHERE emp_id IN (SELECT emp_id
    FROM Works_On WHERE proj_id = 101);
42. SELECT dept_name FROM Departments WHERE dept_id = (SELECT
    dept_id FROM Projects WHERE proj_name = 'Project A');
43. SELECT emp_id FROM Employees WHERE salary = (SELECT
    MAX(salary) FROM Employees);
44. SELECT proj_id FROM Projects WHERE dept_id = (SELECT dept_id
    FROM Departments WHERE dept_name = 'Finance');
45. SELECT emp_id FROM Works_On WHERE proj_id IN (SELECT proj_id
    FROM Projects WHERE budget > 50000);
```

Aggregation

```
46. SELECT AVG(salary) FROM Employees;
47. SELECT COUNT(emp_id) FROM Employees;
48. SELECT SUM(budget) FROM Projects;
49. SELECT MIN(age) FROM Employees;
```

Descriptions of Relational Algebra (RA) Queries

Selection (σ)

1. $\sigma(\text{age} > 30)(\text{Employees})$: Selects all employees older than 30 years.
 - **Minimum Tuples**: 0 (if no employee is older than 30)
 - **Maximum Tuples**: Total number of tuples in **Employees**
2. $\sigma(\text{dept_name} = \text{'HR'})(\text{Departments})$: Selects all departments named 'HR'.
 - **Minimum Tuples**: 0 (if there is no 'HR' department)
 - **Maximum Tuples**: Total number of tuples in **Departments**
3. $\sigma(\text{salary} > 70000)(\text{Employees})$: Selects all employees with a salary greater than 70,000.
 - **Minimum Tuples**: 0 (if no employee earns more than 70,000)
 - **Maximum Tuples**: Total number of tuples in **Employees**
4. $\sigma(\text{location} = \text{'New York'})(\text{Departments})$: Selects all departments located in New York.
 - **Minimum Tuples**: 0 (if no department is in New York)
 - **Maximum Tuples**: Total number of tuples in **Departments**
5. $\sigma(\text{budget} > 100000)(\text{Projects})$: Selects all projects with a budget greater than 100,000.
 - **Minimum Tuples**: 0 (if no project has a budget above 100,000)
 - **Maximum Tuples**: Total number of tuples in **Projects**

Projection (π)

6. $\pi(\text{name, age})(\text{Employees})$: Projects the names and ages of all employees.
 - **Minimum Tuples**: 0 (if **Employees** is empty)
 - **Maximum Tuples**: Total number of tuples in **Employees**
7. $\pi(\text{dept_name})(\text{Departments})$: Projects the names of all departments.
 - **Minimum Tuples**: 0 (if **Departments** is empty)
 - **Maximum Tuples**: Total number of tuples in **Departments**
8. $\pi(\text{proj_name, budget})(\text{Projects})$: Projects the names and budgets of all projects.
 - **Minimum Tuples**: 0 (if **Projects** is empty)
 - **Maximum Tuples**: Total number of tuples in **Projects**
9. $\pi(\text{emp_id, salary})(\text{Employees})$: Projects the employee IDs and salaries.
 - **Minimum Tuples**: 0 (if **Employees** is empty)
 - **Maximum Tuples**: Total number of tuples in **Employees**
10. $\pi(\text{location})(\text{Departments})$: Projects the locations of all departments.
 - **Minimum Tuples**: 0 (if **Departments** is empty)
 - **Maximum Tuples**: Total number of tuples in **Departments**

Union (U)

11. $\pi(\text{emp_id}, \text{salary})(\text{Employees}) \cup \pi(\text{emp_id}, \text{annual_salary})(\text{Salaries})$: Combines employee IDs and their current or annual salaries.
 - **Minimum Tuples**: Size of the larger relation (whichever has more unique `emp_id`)
 - **Maximum Tuples**: Sum of unique tuples from both `Employees` and `Salaries`
12. $\pi(\text{dept_id}, \text{location})(\text{Departments}) \cup \pi(\text{dept_id}, \text{dept_name})(\text{Departments})$: Combines department IDs and their respective locations or names.
 - **Minimum Tuples**: Size of the `Departments` table (assuming all entries are unique)
 - **Maximum Tuples**: Sum of unique tuples from both operations on `Departments`
13. $\pi(\text{emp_id}, \text{proj_id})(\text{Works_On}) \cup \pi(\text{emp_id}, \text{proj_id})(\text{Works_On})$: Combines employees and project IDs they work on. This will likely be redundant.
 - **Minimum Tuples**: Size of `Works_On` (assuming duplicates are removed)
 - **Maximum Tuples**: Size of `Works_On` (if there are no duplicates)
14. $\pi(\text{dept_id})(\text{Departments}) \cup \pi(\text{dept_id})(\text{Projects})$: Combines department IDs from departments and projects.
 - **Minimum Tuples**: Number of unique `dept_id` in `Departments` or `Projects`, whichever is larger
 - **Maximum Tuples**: Sum of unique `dept_id` in `Departments` and `Projects`
15. $\pi(\text{name})(\text{Employees}) \cup \pi(\text{proj_name})(\text{Projects})$: Combines employee names and project names into a single set.
 - **Minimum Tuples**: Number of unique names in `Employees` or `Projects`, whichever is larger
 - **Maximum Tuples**: Sum of unique names in `Employees` and `Projects`

Set Difference (-)

16. $\pi(\text{emp_id})(\text{Employees}) - \pi(\text{emp_id})(\text{Works_On})$: Finds employees not working on any project.
 - **Minimum Tuples**: 0 (if all employees work on at least one project)
 - **Maximum Tuples**: Total number of tuples in `Employees`
17. $\pi(\text{dept_id})(\text{Departments}) - \pi(\text{dept_id})(\text{Projects})$: Finds departments that have no associated projects.
 - **Minimum Tuples**: 0 (if all departments have projects)
 - **Maximum Tuples**: Total number of tuples in `Departments`
18. $\pi(\text{proj_id})(\text{Projects}) - \pi(\text{proj_id})(\text{Works_On})$: Finds projects that have no employees working on them.
 - **Minimum Tuples**: 0 (if all projects have employees working on them)
 - **Maximum Tuples**: Total number of tuples in `Projects`
19. $\pi(\text{emp_id})(\text{Employees}) - \pi(\text{emp_id})(\text{Salaries})$: Finds employees without any salary record.
 - **Minimum Tuples**: 0 (if all employees have salary records)

- **Maximum Tuples:** Total number of tuples in **Employees**
- 20. $\pi(\text{location})(\text{Departments}) - \pi(\text{location})(\text{Departments})$:** Finds locations that are not used in any department. This will always result in an empty set because a set minus itself is empty.
 - **Minimum Tuples:** 0
 - **Maximum Tuples:** 0

Cartesian Product (\times)

- 21. **Employees \times Departments**:** Creates a Cartesian product of all employees with all departments.
 - **Minimum Tuples:** 0 (if either **Employees** or **Departments** is empty)
 - **Maximum Tuples:** Product of the number of tuples in **Employees** and **Departments**
- 22. **Projects \times Departments**:** Creates a Cartesian product of all projects with all departments.
 - **Minimum Tuples:** 0 (if either **Projects** or **Departments** is empty)
 - **Maximum Tuples:** Product of the number of tuples in **Projects** and **Departments**
- 23. **Employees \times Projects**:** Creates a Cartesian product of all employees with all projects.
 - **Minimum Tuples:** 0 (if either **Employees** or **Projects** is empty)
 - **Maximum Tuples:** Product of the number of tuples in **Employees** and **Projects**
- 24. **Departments \times Works_On**:** Creates a Cartesian product of all departments with all project assignments.
 - **Minimum Tuples:** 0 (if either **Departments** or **Works_On** is empty)
 - **Maximum Tuples:** Product of the number of tuples in **Departments** and **Works_On**
- 25. **Salaries \times Works_On**:** Creates a Cartesian product of all salaries with all project assignments.
 - **Minimum Tuples:** 0 (if either **Salaries** or **Works_On** is empty)
 - **Maximum Tuples:** Product of the number of tuples in **Salaries** and **Works_On**

Rename (ρ)

- 26. $\rho(\text{Emp}(\text{emp_id}, \text{name}, \text{age}, \text{dept_id}, \text{salary}))(\text{Employees})$:** Renames the **Employees** relation to **Emp**.
 - **Minimum Tuples:** 0 (if **Employees** is empty)
 - **Maximum Tuples:** Total number of tuples in **Employees**
- 27. $\rho(\text{Dept}(\text{dept_id}, \text{dept_name}, \text{location}))(\text{Departments})$:** Renames the **Departments** relation to **Dept**.
 - **Minimum Tuples:** 0 (if **Departments** is empty)
 - **Maximum Tuples:** Total number of tuples in **Departments**
- 28. $\rho(\text{Proj}(\text{proj_id}, \text{proj_name}, \text{dept_id}, \text{budget}))(\text{Projects})$:** Renames the **Projects** relation to **Proj**.

- **Minimum Tuples:** 0 (if `Projects` is empty)
- **Maximum Tuples:** Total number of tuples in `Projects`
- 29. $\rho(\text{Work}(\text{emp_id}, \text{proj_id}, \text{hours}))(\text{Works_On})$: Renames the `Works_On` relation to `Work`.
 - **Minimum Tuples:** 0 (if `Works_On` is empty)
 - **Maximum Tuples:** Total number of tuples in `Works_On`
- 30. $\rho(\text{Sal}(\text{emp_id}, \text{year}, \text{annual_salary}))(\text{Salaries})$: Renames the `Salaries` relation to `Sal`.
 - **Minimum Tuples:** 0 (if `Salaries` is empty)
 - **Maximum Tuples:** Total number of tuples in `Salaries`

Join (\bowtie) (continued)

- 31. `Employees` \bowtie `dept_id = dept_id Departments`: Joins employees with their respective departments on `dept_id`.
 - **Minimum Tuples:** 0 (if no `dept_id` matches between `Employees` and `Departments`)
 - **Maximum Tuples:** Total number of tuples in `Employees` (if every employee belongs to a department)
- 32. `Projects` \bowtie `dept_id = dept_id Departments`: Joins projects with their respective departments on `dept_id`.
 - **Minimum Tuples:** 0 (if no `dept_id` matches between `Projects` and `Departments`)
 - **Maximum Tuples:** Total number of tuples in `Projects` (if every project is associated with a department)
- 33. `Works_On` \bowtie `emp_id = emp_id Employees`: Joins `Works_On` with `Employees` on `emp_id` to get detailed employee information.
 - **Minimum Tuples:** 0 (if no `emp_id` matches between `Works_On` and `Employees`)
 - **Maximum Tuples:** Total number of tuples in `Works_On` (if every entry corresponds to a valid employee)
- 34. `Employees` \bowtie `emp_id = emp_id Salaries`: Joins `Employees` with `Salaries` on `emp_id` to get historical salary data.
 - **Minimum Tuples:** 0 (if no `emp_id` matches between `Employees` and `Salaries`)
 - **Maximum Tuples:** Total number of tuples in `Salaries` (if every salary record corresponds to a valid employee)
- 35. `Projects` \bowtie `dept_id = dept_id Works_On`: This join does not make logical sense as `Projects` should ideally join with `Works_On` on `proj_id`, not `dept_id`. Assuming it was meant to be `proj_id`:
 - **Minimum Tuples:** 0 (if no `proj_id` matches between `Projects` and `Works_On`)
 - **Maximum Tuples:** Total number of tuples in `Works_On` (if every work assignment corresponds to a valid project)

Natural Join (\bowtie)

- 36. `Employees` \bowtie `Departments`: Performs a natural join between `Employees` and `Departments` on `dept_id`.
 - **Minimum Tuples:** 0 (if no common `dept_id` exists)
 - **Maximum Tuples:** Number of tuples in `Employees` (if all employees belong to valid departments)
- 37. `Projects` \bowtie `Departments`: Performs a natural join between `Projects` and `Departments` on `dept_id`.

- **Minimum Tuples:** 0 (if no common dept_id exists)
 - **Maximum Tuples:** Number of tuples in Projects (if all projects are linked to valid departments)
38. **Works_On \bowtie Employees:** Performs a natural join on emp_id between Works_On and Employees.
- **Minimum Tuples:** 0 (if no common emp_id exists)
 - **Maximum Tuples:** Number of tuples in Works_On (if all work assignments correspond to valid employees)
39. **Employees \bowtie Salaries:** Performs a natural join on emp_id between Employees and Salaries.
- **Minimum Tuples:** 0 (if no common emp_id exists)
 - **Maximum Tuples:** Number of tuples in Salaries (if all salary records correspond to valid employees)
40. **Projects \bowtie Works_On:** Performs a natural join on proj_id between Projects and Works_On.
- **Minimum Tuples:** 0 (if no common proj_id exists)
 - **Maximum Tuples:** Number of tuples in Works_On (if all work assignments are linked to valid projects)

Division (\div)

41. $\pi(\text{emp_id}, \text{proj_id})(\text{Works_On}) \div \pi(\text{proj_id})(\text{Projects})$: Finds employees who have worked on all projects listed.
- **Minimum Tuples:** 0 (if no employee has worked on all projects)
 - **Maximum Tuples:** Number of unique emp_id in Works_On (if every employee has worked on all projects)
42. $\pi(\text{emp_id}, \text{dept_id})(\text{Employees}) \div \pi(\text{dept_id})(\text{Departments})$: Finds employees assigned to all departments.
- **Minimum Tuples:** 0 (if no employee is in all departments)
 - **Maximum Tuples:** Number of unique emp_id in Employees (if every employee is in all departments)
43. $\pi(\text{emp_id}, \text{proj_id})(\text{Works_On}) \div \pi(\text{proj_id})(\text{Works_On})$: This seems to be a division operation of Works_On by itself, which would result in an empty relation unless there is an implied constant or universal project set.
- **Minimum Tuples:** 0
 - **Maximum Tuples:** Typically 0, as the division of a set by itself should yield the universal set unless constrained
44. $\pi(\text{emp_id}, \text{proj_id})(\text{Works_On}) \div \pi(\text{emp_id})(\text{Employees})$: This operation checks if all employees are working on a particular set of projects. Typically, division requires consistent sets on both sides.
- **Minimum Tuples:** 0 (if the sets do not align)
 - **Maximum Tuples:** Number of unique emp_id in Works_On
45. $\pi(\text{proj_id})(\text{Projects}) \div \pi(\text{dept_id})(\text{Departments})$: Division here seems incorrect as projects and departments should not divide over each other logically. Assuming it checks projects per department:
- **Minimum Tuples:** 0 (if no project exists for all departments)
 - **Maximum Tuples:** Number of unique proj_id (but typically not valid)

Intersection (\cap)

46. $\pi(\text{emp_id})(\text{Employees}) \cap \pi(\text{emp_id})(\text{Works_On})$: Finds employees who are also listed in the `Works_On` table.
 - **Minimum Tuples**: 0 (if no common `emp_id` exists)
 - **Maximum Tuples**: Number of unique `emp_id` in `Employees` or `Works_On`, whichever is smaller
47. $\pi(\text{dept_id})(\text{Departments}) \cap \pi(\text{dept_id})(\text{Projects})$: Finds department IDs common to both departments and projects.
 - **Minimum Tuples**: 0 (if no common `dept_id` exists)
 - **Maximum Tuples**: Number of unique `dept_id` in `Departments` or `Projects`, whichever is smaller
48. $\pi(\text{proj_id})(\text{Projects}) \cap \pi(\text{proj_id})(\text{Works_On})$: Finds project IDs that exist in both the `Projects` and `Works_On` tables.
 - **Minimum Tuples**: 0 (if no common `proj_id` exists)
 - **Maximum Tuples**: Number of unique `proj_id` in `Projects` or `Works_On`, whichever is smaller
49. $\pi(\text{emp_id})(\text{Employees}) \cap \pi(\text{emp_id})(\text{Salaries})$: Finds employees with records in both `Employees` and `Salaries`.
 - **Minimum Tuples**: 0 (if no common `emp_id` exists)
 - **Maximum Tuples**: Number of unique `emp_id` in `Employees` or `Salaries`, whichever is smaller
50. $\pi(\text{location})(\text{Departments}) \cap \pi(\text{location})(\text{Departments})$: This operation is redundant and will simply return all unique department locations.
 - **Minimum Tuples**: Number of unique `location` in `Departments`
 - **Maximum Tuples**: Number of unique `location` in `Departments`

Corresponding SQL:

Corresponding SQL Queries :

Basic SELECT

1. **SELECT * FROM Employees WHERE age > 30;** Retrieves all columns for employees older than 30.
 - **Minimum Tuples**: 0 (if no employee is older than 30)
 - **Maximum Tuples**: Total number of rows in `Employees`
2. **SELECT * FROM Departments WHERE dept_name = 'HR';** Retrieves all columns for departments named 'HR'.
 - **Minimum Tuples**: 0 (if there is no 'HR' department)
 - **Maximum Tuples**: Total number of rows in `Departments`
3. **SELECT * FROM Employees WHERE salary > 70000;** Retrieves all employees with a salary over 70,000.
 - **Minimum Tuples**: 0 (if no employee earns more than 70,000)
 - **Maximum Tuples**: Total number of rows in `Employees`
4. **SELECT * FROM Departments WHERE location = 'New York';** Retrieves all departments located in New York.

- **Minimum Tuples:** 0 (if no department is in New York)
 - **Maximum Tuples:** Total number of rows in `Departments`
5. **SELECT * FROM Projects WHERE budget > 100000;** Retrieves all projects with a budget over 100,000.
- **Minimum Tuples:** 0 (if no project has a budget above 100,000)
 - **Maximum Tuples:** Total number of rows in `Projects`

SELECT with Specific Columns (continued)

6. **SELECT name, age FROM Employees;** Retrieves only the name and age columns for all employees.
- **Minimum Tuples:** 0 (if `Employees` table is empty)
 - **Maximum Tuples:** Total number of rows in `Employees`
7. **SELECT dept_name FROM Departments;** Retrieves only the dept_name column for all departments.
- **Minimum Tuples:** 0 (if `Departments` table is empty)
 - **Maximum Tuples:** Total number of rows in `Departments`
8. **SELECT proj_name, budget FROM Projects;** Retrieves the proj_name and budget columns for all projects.
- **Minimum Tuples:** 0 (if `Projects` table is empty)
 - **Maximum Tuples:** Total number of rows in `Projects`
9. **SELECT emp_id, salary FROM Employees;** Retrieves the emp_id and salary columns for all employees.
- **Minimum Tuples:** 0 (if `Employees` table is empty)
 - **Maximum Tuples:** Total number of rows in `Employees`
10. **SELECT location FROM Departments;** Retrieves the location column for all departments.
- **Minimum Tuples:** 0 (if `Departments` table is empty)
 - **Maximum Tuples:** Total number of rows in `Departments`

JOIN Operations

11. **SELECT Employees.name, Departments.dept_name FROM Employees JOIN Departments ON Employees.dept_id = Departments.dept_id;** Joins `Employees` and `Departments` on dept_id and selects employee names and department names.
- **Minimum Tuples:** 0 (if no matching dept_id exists between `Employees` and `Departments`)
 - **Maximum Tuples:** Total number of rows in `Employees` (if every employee is associated with a valid department)
12. **SELECT Projects.proj_name, Departments.location FROM Projects JOIN Departments ON Projects.dept_id = Departments.dept_id;** Joins `Projects` and `Departments` on dept_id and selects project names and department locations.

- **Minimum Tuples:** 0 (if no matching dept_id exists between Projects and Departments)
 - **Maximum Tuples:** Total number of rows in Projects (if every project is associated with a valid department)
- 13. SELECT Employees.emp_id, Works_On.proj_id FROM Employees JOIN Works_On ON Employees.emp_id = Works_On.emp_id;** Joins Employees and Works_On on emp_id and selects employee IDs and project IDs.
- **Minimum Tuples:** 0 (if no matching emp_id exists between Employees and Works_On)
 - **Maximum Tuples:** Total number of rows in Works_On (if every project assignment has a corresponding employee)
- 14. SELECT Employees.emp_id, Salaries.annual_salary FROM Employees JOIN Salaries ON Employees.emp_id = Salaries.emp_id;** Joins Employees and Salaries on emp_id and selects employee IDs and annual salaries.
- **Minimum Tuples:** 0 (if no matching emp_id exists between Employees and Salaries)
 - **Maximum Tuples:** Total number of rows in Salaries (if every salary record corresponds to a valid employee)
- 15. SELECT Projects.proj_id, Works_On.emp_id FROM Projects JOIN Works_On ON Projects.proj_id = Works_On.proj_id;** Joins Projects and Works_On on proj_id and selects project IDs and employee IDs.
- **Minimum Tuples:** 0 (if no matching proj_id exists between Projects and Works_On)
 - **Maximum Tuples:** Total number of rows in Works_On (if every work assignment corresponds to a valid project)

UNION Operations

- 16. SELECT emp_id, salary FROM Employees UNION SELECT emp_id, annual_salary FROM Salaries;** Combines employee IDs and their current or annual salaries.
- **Minimum Tuples:** Number of unique emp_id across Employees and Salaries
 - **Maximum Tuples:** Sum of unique emp_id tuples in both Employees and Salaries
- 17. SELECT dept_id, location FROM Departments UNION SELECT dept_id, dept_name FROM Departments;** Combines department IDs with their respective locations or names.
- **Minimum Tuples:** Number of unique dept_id in Departments (assuming unique pairs)
 - **Maximum Tuples:** Sum of unique tuples from both queries on Departments
- 18. SELECT emp_id, proj_id FROM Works_On UNION SELECT emp_id, proj_id FROM Works_On;** Combines employee and project IDs they work on, but since it's the same relation, it results in unique tuples.

- **Minimum Tuples:** Number of unique (emp_id, proj_id) pairs in Works_On
 - **Maximum Tuples:** Number of unique (emp_id, proj_id) pairs in Works_On
- 19. SELECT dept_id FROM Departments UNION SELECT dept_id FROM Projects;** Combines department IDs from departments and projects.
- **Minimum Tuples:** Number of unique dept_id in Departments or Projects, whichever is larger
 - **Maximum Tuples:** Sum of unique dept_id tuples in both Departments and Projects
- 20. SELECT name FROM Employees UNION SELECT proj_name FROM Projects;** Combines employee names and project names.
- **Minimum Tuples:** Number of unique names in Employees or Projects, whichever is larger
 - **Maximum Tuples:** Sum of unique names in both Employees and Projects

INTERSECT Operations

- 21. SELECT emp_id FROM Employees INTERSECT SELECT emp_id FROM Works_On;** Finds employee IDs that are present in both Employees and Works_On.
- **Minimum Tuples:** 0 (if no emp_id is common)
 - **Maximum Tuples:** Number of unique emp_id in Employees or Works_On, whichever is smaller
- 22. SELECT dept_id FROM Departments INTERSECT SELECT dept_id FROM Projects;** Finds department IDs that are present in both Departments and Projects.
- **Minimum Tuples:** 0 (if no dept_id is common)
 - **Maximum Tuples:** Number of unique dept_id in Departments or Projects, whichever is smaller
- 23. SELECT proj_id FROM Projects INTERSECT SELECT proj_id FROM Works_On;** Finds project IDs that are present in both Projects and Works_On.
- **Minimum Tuples:** 0 (if no proj_id is common)
 - **Maximum Tuples:** Number of unique proj_id in Projects or Works_On, whichever is smaller
- 24. SELECT emp_id FROM Employees INTERSECT SELECT emp_id FROM Salaries;** Finds employee IDs that are present in both Employees and Salaries.
- **Minimum Tuples:** 0 (if no emp_id is common)
 - **Maximum Tuples:** Number of unique emp_id in Employees or Salaries, whichever is smaller
- 25. SELECT location FROM Departments INTERSECT SELECT location FROM Departments;** This operation is redundant and returns all unique department locations.
- **Minimum Tuples:** Number of unique location in Departments
 - **Maximum Tuples:** Number of unique location in Departments

MINUS (EXCEPT) Operations

- 26. SELECT emp_id FROM Employees EXCEPT SELECT emp_id FROM Works_On;** Finds employee IDs that are in Employees but not in Works_On.
- **Minimum Tuples:** 0 (if all employees have a project record in Works_On)
 - **Maximum Tuples:** Number of unique emp_id in Employees
- 27. SELECT dept_id FROM Departments EXCEPT SELECT dept_id FROM Projects;** Finds department IDs that are in Departments but not associated with any project in Projects.
- **Minimum Tuples:** 0 (if every department is associated with a project)
 - **Maximum Tuples:** Number of unique dept_id in Departments
- 28. SELECT proj_id FROM Projects EXCEPT SELECT proj_id FROM Works_On;** Finds project IDs that are in Projects but have no employees working on them in Works_On.
- **Minimum Tuples:** 0 (if every project has employees working on it)
 - **Maximum Tuples:** Number of unique proj_id in Projects

29. SELECT emp_id FROM Employees EXCEPT SELECT emp_id FROM Salaries; Finds employee IDs that are in Employees but have no salary record in Salaries.

- **Minimum Tuples:** 0 (if every employee has a salary record)
- **Maximum Tuples:** Number of unique emp_id in Employees

GROUP BY and HAVING (continued)

- 31. SELECT dept_id, COUNT(emp_id) FROM Employees GROUP BY dept_id;** Counts the number of employees in each department.
- **Minimum Tuples:** 0 (if Employees table is empty)
 - **Maximum Tuples:** Number of unique dept_id in Employees
- 32. SELECT proj_id, SUM(budget) FROM Projects GROUP BY proj_id;** Sums the budgets of projects, grouped by project ID.
- **Minimum Tuples:** 0 (if Projects table is empty)
 - **Maximum Tuples:** Number of unique proj_id in Projects
- 33. SELECT location, COUNT(dept_id) FROM Departments GROUP BY location;** Counts the number of departments in each location.
- **Minimum Tuples:** 0 (if Departments table is empty)
 - **Maximum Tuples:** Number of unique location in Departments
- 34. SELECT dept_id, AVG(salary) FROM Employees GROUP BY dept_id HAVING AVG(salary) > 70000;** Calculates the average salary per department and only returns departments with an average salary greater than 70,000.
- **Minimum Tuples:** 0 (if no department's average salary exceeds 70,000)
 - **Maximum Tuples:** Number of unique dept_id in Employees
- 35. SELECT proj_id, COUNT(emp_id) FROM Works_On GROUP BY proj_id HAVING COUNT(emp_id) > 5;** Counts the number of employees working on each project and returns only projects with more than 5 employees.

- **Minimum Tuples:** 0 (if no project has more than 5 employees)
- **Maximum Tuples:** Number of unique proj_id in Works_On

Aggregation Functions

36. **SELECT COUNT(*) FROM Employees;** Counts the total number of employees.
 - **Minimum Tuples:** 0 (if Employees table is empty)
 - **Maximum Tuples:** 1 (always returns a single count)
37. **SELECT AVG(salary) FROM Employees;** Calculates the average salary of all employees.
 - **Minimum Tuples:** 0 (if Employees table is empty)
 - **Maximum Tuples:** 1 (always returns a single average value)
38. **SELECT MAX(salary) FROM Employees;** Finds the maximum salary among all employees.
 - **Minimum Tuples:** 0 (if Employees table is empty)
 - **Maximum Tuples:** 1 (always returns a single maximum value)
39. **SELECT MIN(salary) FROM Employees;** Finds the minimum salary among all employees.
 - **Minimum Tuples:** 0 (if Employees table is empty)
 - **Maximum Tuples:** 1 (always returns a single minimum value)
40. **SELECT SUM(budget) FROM Projects;** Sums the budgets of all projects.
 - **Minimum Tuples:** 0 (if Projects table is empty)
 - **Maximum Tuples:** 1 (always returns a single sum value)

Subqueries

41. **SELECT * FROM Employees WHERE salary > (SELECT AVG(salary) FROM Employees);** Retrieves all employees with a salary above the average salary.
 - **Minimum Tuples:** 0 (if no employee's salary is above the average)
 - **Maximum Tuples:** Total number of rows in Employees (if all employees earn above the average)
42. **SELECT * FROM Projects WHERE budget > (SELECT MAX(budget) FROM Projects) - 50000;** Retrieves all projects with a budget greater than the maximum budget minus 50,000.
 - **Minimum Tuples:** 0 (if no project meets the criteria)
 - **Maximum Tuples:** Total number of rows in Projects
43. **SELECT * FROM Employees WHERE dept_id = (SELECT dept_id FROM Departments WHERE dept_name = 'HR');** Retrieves all employees in the HR department.
 - **Minimum Tuples:** 0 (if there are no employees in the HR department)
 - **Maximum Tuples:** Total number of rows in Employees
44. **SELECT * FROM Employees WHERE emp_id IN (SELECT emp_id FROM Works_On WHERE proj_id = 'P123');** Retrieves all employees who are working on project P123.
 - **Minimum Tuples:** 0 (if no employee works on P123)
 - **Maximum Tuples:** Total number of rows in Employees
45. **SELECT * FROM Projects WHERE dept_id IN (SELECT dept_id FROM Departments WHERE location = 'New York');** Retrieves all projects associated with departments located in New York.

- **Minimum Tuples:** 0 (if no projects are associated with New York departments)
- **Maximum Tuples:** Total number of rows in `Projects`

EXISTS and NOT EXISTS

46. **SELECT * FROM Employees WHERE EXISTS (SELECT 1 FROM Works_On WHERE Employees.emp_id = Works_On.emp_id);** Retrieves all employees who are assigned to at least one project.
 - **Minimum Tuples:** 0 (if no employee is assigned to any project)
 - **Maximum Tuples:** Total number of rows in `Employees`
47. **SELECT * FROM Departments WHERE NOT EXISTS (SELECT 1 FROM Projects WHERE Departments.dept_id = Projects.dept_id);** Retrieves all departments that do not have any associated projects.
 - **Minimum Tuples:** 0 (if every department has at least one project)
 - **Maximum Tuples:** Total number of rows in `Departments`
48. **SELECT * FROM Projects WHERE EXISTS (SELECT 1 FROM Works_On WHERE Projects.proj_id = Works_On.proj_id);** Retrieves all projects that have employees working on them.
 - **Minimum Tuples:** 0 (if no project has employees working on it)
 - **Maximum Tuples:** Total number of rows in `Projects`
49. **SELECT * FROM Employees WHERE NOT EXISTS (SELECT 1 FROM Salaries WHERE Employees.emp_id = Salaries.emp_id);** Retrieves all employees who do not have a salary record.
 - **Minimum Tuples:** 0 (if every employee has a salary record)
 - **Maximum Tuples:** Total number of rows in `Employees`
50. **SELECT * FROM Departments WHERE EXISTS (SELECT 1 FROM Employees WHERE Departments.dept_id = Employees.dept_id);** Retrieves all departments that have employees.
 - **Minimum Tuples:** 0 (if no department has employees)
 - **Maximum Tuples:** Total number of rows in `Departments`

Complex Queries with Multiple Clauses

51. **SELECT dept_name, AVG(salary) FROM Employees JOIN Departments ON Employees.dept_id = Departments.dept_id GROUP BY dept_name HAVING AVG(salary) > 70000;** Calculates the average salary per department and returns departments with an average salary greater than 70,000.
 - **Minimum Tuples:** 0 (if no department has an average salary over 70,000)
 - **Maximum Tuples:** Number of unique `dept_name` in `Departments`
52. **SELECT emp_id, COUNT(proj_id) FROM Works_On GROUP BY emp_id HAVING COUNT(proj_id) > 3;** Finds employees working on more than 3 projects.
 - **Minimum Tuples:** 0 (if no employee works on more than 3 projects)
 - **Maximum Tuples:** Number of unique `emp_id` in `Works_On`
53. **SELECT proj_id, MAX(budget) FROM Projects GROUP BY proj_id HAVING MAX(budget) > 100000;** Finds projects with a budget greater than 100,000.
 - **Minimum Tuples:** 0 (if no project has a budget over 100,000)
 - **Maximum Tuples:** Number of unique `proj_id` in `Projects`

- 54. SELECT dept_name, COUNT(emp_id) FROM Departments JOIN Employees ON Departments.dept_id = Employees.dept_id GROUP BY dept_name;** Counts the number of employees in each department.
- **Minimum Tuples:** 0 (if no department has employees)
 - **Maximum Tuples:** Number of unique dept_name in Departments
- 55. SELECT proj_name, SUM(budget) FROM Projects GROUP BY proj_name HAVING SUM(budget) > 500000;** Sums the budget of projects and returns those with a total budget greater than 500,000.
- **Minimum Tuples:** 0 (if no project's total budget exceeds 500,000)
 - **Maximum Tuples:** Number of unique proj_name in Projects

Queries with ORDER BY

- 56. SELECT * FROM Employees ORDER BY salary DESC;** Retrieves all employees, ordered by salary in descending order.
- **Minimum Tuples:** 0 (if Employees table is empty)
 - **Maximum Tuples:** Total number of rows in Employees
- 57. SELECT * FROM Projects ORDER BY budget ASC;** Retrieves all projects, ordered by budget in ascending order.
- **Minimum Tuples:** 0 (if Projects table is empty)
 - **Maximum Tuples:** Total number of rows in Projects
- 58. SELECT * FROM Departments ORDER BY dept_name;** Retrieves all departments, ordered alphabetically by department name.
- **Minimum Tuples:** 0 (if Departments table is empty)
 - **Maximum Tuples:** Total number of rows in Departments
- 59. SELECT * FROM Works_On ORDER BY emp_id, proj_id;** Retrieves all work assignments, ordered first by employee ID and then by project ID.
- **Minimum Tuples:** 0 (if Works_On table is empty)
 - **Maximum Tuples:** Total number of rows in Works_On
- 60. SELECT * FROM Employees ORDER BY dept_id, salary DESC;** Retrieves all employees, ordered first by department ID and then by salary in descending order.
- **Minimum Tuples:** 0 (if Employees table is empty)
 - **Maximum Tuples:** Total number of rows in Employees

Queries with DISTINCT

- 61. SELECT DISTINCT dept_id FROM Employees;** Retrieves unique department IDs from the Employees table.
- **Minimum Tuples:** 0 (if Employees table is empty)
 - **Maximum Tuples:** Number of unique dept_id in Employees
- 62. SELECT DISTINCT location FROM Departments;** Retrieves unique locations from the Departments table.
- **Minimum Tuples:** 0 (if Departments table is empty)
 - **Maximum Tuples:** Number of unique location in Departments
- 63. SELECT DISTINCT proj_id FROM Works_On;** Retrieves unique project IDs from the Works_On table.
- **Minimum Tuples:** 0 (if Works_On table is empty)
 - **Maximum Tuples:** Number of unique proj_id in Works_On

64. SELECT DISTINCT emp_id FROM Salaries; Retrieves unique employee IDs from the `Salaries` table.

- **Minimum Tuples:** 0 (if `Salaries` table is empty)
- **Maximum Tuples:** Number of unique `emp_id` in `Salaries`

65. SELECT DISTINCT dept_name FROM Departments; Retrieves unique department names from the `Departments` table.

- **Minimum Tuples:** 0 (if `Departments` table is empty)
- **Maximum Tuples:** Number of unique `dept_name` in `Departments`

Queries with IN and NOT IN

66. SELECT * FROM Employees WHERE dept_id IN (SELECT dept_id FROM Departments WHERE location = 'New York'); Retrieves all employees in departments located in New York.

- **Minimum Tuples:** 0 (if no employees are in New York departments)
- **Maximum Tuples:** Total number of rows in `Employees`

67. SELECT * FROM Projects WHERE dept_id NOT IN (SELECT dept_id FROM Departments WHERE location = 'San Francisco'); Retrieves all projects not associated with departments in San Francisco.

- **Minimum Tuples:** 0 (if all projects are associated with San Francisco departments)
- **Maximum Tuples:** Total number of rows in `Projects`

68. SELECT * FROM Employees WHERE emp_id IN (SELECT emp_id FROM Works_On WHERE proj_id = 'P123'); Retrieves all employees who work on project P123.

- **Minimum Tuples:** 0 (if no employees work on P123)
- **Maximum Tuples:** Total number of rows in `Employees`

69. SELECT * FROM Departments WHERE dept_id NOT IN (SELECT dept_id FROM Projects); Retrieves all departments that have no associated projects.

- **Minimum Tuples:** 0 (if every department has at least one project)
- **Maximum Tuples:** Total number of rows in `Departments`

70. SELECT * FROM Employees WHERE emp_id IN (SELECT emp_id FROM Salaries WHERE annual_salary > 100000); Retrieves all employees who have an annual salary greater than 100,000.

- **Minimum Tuples:** 0 (if no employees have an annual salary over 100,000)
- **Maximum Tuples:** Total number of rows in `Employees`

Queries with BETWEEN

71. SELECT * FROM Employees WHERE salary BETWEEN 50000 AND 100000; Retrieves all employees with salaries between 50,000 and 100,000.

- **Minimum Tuples:** 0 (if no employees have a salary in this range)
- **Maximum Tuples:** Total number of rows in `Employees`

72. SELECT * FROM Projects WHERE budget BETWEEN 100000 AND 500000; Retrieves all projects with a budget between 100,000 and 500,000.

- **Minimum Tuples:** 0 (if no projects have a budget in this range)
- **Maximum Tuples:** Total number of rows in `Projects`

73. SELECT * FROM Departments WHERE dept_id BETWEEN 1 AND 10; Retrieves all departments with IDs between 1 and 10.

- **Minimum Tuples:** 0 (if no department IDs fall in this range)
- **Maximum Tuples:** Total number of rows in `Departments`

74. SELECT * FROM Works_On WHERE proj_id BETWEEN 'P100' AND 'P200'; Retrieves all work assignments for projects with IDs between P100 and P200.

- **Minimum Tuples:** 0 (if no project IDs fall in this range)
 - **Maximum Tuples:** Total number of rows in Works_On
- 75. SELECT * FROM Salaries WHERE annual_salary BETWEEN 60000 AND 120000;;** Retrieves all salary records where the annual salary is between 60,000 and 120,000.
- **Minimum Tuples:** 0 (if no salary records fall in this range)
 - **Maximum Tuples:** Total number of rows in Salaries

Queries with LIKE

- 76. SELECT * FROM Employees WHERE name LIKE 'A%';** Retrieves all employees whose names start with the letter 'A'.
- **Minimum Tuples:** 0 (if no employee names start with 'A')
 - **Maximum Tuples:** Total number of rows in Employees
- 77. SELECT * FROM Projects WHERE proj_name LIKE '%Research%';** Retrieves all projects whose names contain the word 'Research'.
- **Minimum Tuples:** 0 (if no project names contain 'Research')
 - **Maximum Tuples:** Total number of rows in Projects
- 78. SELECT * FROM Departments WHERE location LIKE 'New%';** Retrieves all departments located in places starting with 'New' (e.g., New York, New Delhi).
- **Minimum Tuples:** 0 (if no department locations start with 'New')
 - **Maximum Tuples:** Total number of rows in Departments
- 79. SELECT * FROM Employees WHERE emp_id LIKE '_23';** Retrieves all employees with IDs ending in '23'.
- **Minimum Tuples:** 0 (if no employee IDs end in '23')
 - **Maximum Tuples:** Total number of rows in Employees
- 80. SELECT * FROM Projects WHERE proj_name LIKE 'Project%';** Retrieves all projects whose names start with 'Project'.
- **Minimum Tuples:** 0 (if no project names start with 'Project')
 - **Maximum Tuples:** Total number of rows in Projects

Queries with CASE

- 81. SELECT name, salary, CASE WHEN salary > 100000 THEN 'High' WHEN salary BETWEEN 50000 AND 100000 THEN 'Medium' ELSE 'Low' END AS salary_range FROM Employees;;** Categorizes employees' salaries into 'High', 'Medium', or 'Low' ranges.
- **Minimum Tuples:** 0 (if Employees table is empty)
 - **Maximum Tuples:** Total number of rows in Employees
- 82. SELECT proj_name, budget, CASE WHEN budget > 500000 THEN 'Large' WHEN budget BETWEEN 100000 AND 500000 THEN 'Medium' ELSE 'Small' END AS budget_category FROM Projects;;** Categorizes projects' budgets into 'Large', 'Medium', or 'Small'.
- **Minimum Tuples:** 0 (if Projects table is empty)
 - **Maximum Tuples:** Total number of rows in Projects
- 83. SELECT dept_name, location, CASE WHEN location = 'New York' THEN 'East Coast' WHEN location = 'San Francisco' THEN 'West Coast' ELSE 'Other' END AS region FROM Departments;;** Categorizes departments based on their location into regions.
- **Minimum Tuples:** 0 (if Departments table is empty)
 - **Maximum Tuples:** Total number of rows in Departments

84. **SELECT emp_id, proj_id, CASE WHEN proj_id LIKE 'P1%' THEN 'Phase 1' WHEN proj_id LIKE 'P2%' THEN 'Phase 2' ELSE 'Other' END AS project_phase FROM Works_On;** Categorizes work assignments based on the project phase.
- **Minimum Tuples:** 0 (if Works_On table is empty)
 - **Maximum Tuples:** Total number of rows in Works_On
85. **SELECT emp_id, CASE WHEN salary > 100000 THEN salary * 0.1 ELSE salary * 0.05 END AS bonus FROM Employees;** Calculates a bonus for each employee based on their salary.
- **Minimum Tuples:** 0 (if Employees table is empty)
 - **Maximum Tuples:** Total number of rows in Employees

Queries with JOIN (advanced)

86. **SELECT e.name, d.dept_name FROM Employees e JOIN Departments d ON e.dept_id = d.dept_id WHERE d.location = 'New York';** Retrieves the names of employees working in departments located in New York.
- **Minimum Tuples:** 0 (if no employees work in New York departments)
 - **Maximum Tuples:** Total number of rows in Employees
87. **SELECT p.proj_name, e.name FROM Projects p JOIN Works_On w ON p.proj_id = w.proj_id JOIN Employees e ON w.emp_id = e.emp_id WHERE p.budget > 100000;** Retrieves the names of employees working on projects with a budget greater than 100,000.
- **Minimum Tuples:** 0 (if no employees work on high-budget projects)
 - **Maximum Tuples:** Total number of rows in Works_On
88. **SELECT d.dept_name, COUNT(e.emp_id) FROM Departments d LEFT JOIN Employees e ON d.dept_id = e.dept_id GROUP BY d.dept_name;** Counts the number of employees per department, including departments with no employees.
- **Minimum Tuples:** 0 (if Departments table is empty)
 - **Maximum Tuples:** Number of unique dept_name in Departments
89. **SELECT p.proj_name, COUNT(w.emp_id) FROM Projects p LEFT JOIN Works_On w ON p.proj_id = w.proj_id GROUP BY p.proj_name;** Counts the number of employees working on each project, including projects with no employees.
- **Minimum Tuples:** 0 (if Projects table is empty)
 - **Maximum Tuples:** Number of unique proj_name in Projects
90. **SELECT e.name, s.annual_salary FROM Employees e RIGHT JOIN Salaries s ON e.emp_id = s.emp_id;** Retrieves employee names along with their salaries, including salary records without matching employees.
- **Minimum Tuples:** 0 (if Salaries table is empty)
 - **Maximum Tuples:** Total number of rows in Salaries

Queries with Self-JOIN

91. **SELECT e1.name, e2.name AS manager FROM Employees e1 JOIN Employees e2 ON e1.manager_id = e2.emp_id;** Retrieves employee names along with their manager's name.

- **Minimum Tuples:** 0 (if no employees have managers)
 - **Maximum Tuples:** Total number of rows in Employees
92. **SELECT e1.name, e2.name AS colleague FROM Employees e1 JOIN Employees e2 ON e1.dept_id = e2.dept_id WHERE e1.emp_id <> e2.emp_id;** Retrieves pairs of employees who work in the same department.
- **Minimum Tuples:** 0 (if no employees work in the same department)
 - **Maximum Tuples:** Number of pairs in Employees with matching dept_id but different emp_id
93. **SELECT e1.name, e2.name AS teammate FROM Works_On w1 JOIN Works_On w2 ON w1.proj_id = w2.proj_id JOIN Employees e1 ON w1.emp_id = e1.emp_id JOIN Employees e2 ON w2.emp_id = e2.emp_id WHERE e1.emp_id <> e2.emp_id;** Retrieves pairs of employees who work on the same project.
- **Minimum Tuples:** 0 (if no employees work on the same project)
 - **Maximum Tuples:** Number of pairs in Works_On with matching proj_id but different emp_id
94. **SELECT e1.name, e2.name AS senior FROM Employees e1 JOIN Employees e2 ON e1.manager_id = e2.emp_id WHERE e1.salary < e2.salary;** Retrieves employees who earn less than their managers.
- **Minimum Tuples:** 0 (if no employees earn less than their managers)
 - **Maximum Tuples:** Total number of rows in Employees
95. **SELECT e1.name, e2.name AS junior FROM Employees e1 JOIN Employees e2 ON e1.manager_id = e2.emp_id WHERE e1.salary > e2.salary;** Retrieves employees who earn more than their managers.
- **Minimum Tuples:** 0 (if no employees earn more than their managers)
 - **Maximum Tuples:** Total number of rows in Employees

Complex Queries with Subqueries, Joins, and Aggregates

96. **SELECT dept_name, (SELECT AVG(salary) FROM Employees WHERE dept_id = d.dept_id) AS avg_salary FROM Departments d;** Retrieves department names along with the average salary of their employees.
- **Minimum Tuples:** 0 (if Departments table is empty)
 - **Maximum Tuples:** Number of unique dept_name in Departments
97. **SELECT proj_name, (SELECT COUNT(*) FROM Works_On WHERE proj_id = p.proj_id) AS num_employees FROM Projects p;** Retrieves project names along with the number of employees working on them.
- **Minimum Tuples:** 0 (if Projects table is empty)
 - **Maximum Tuples:** Number of unique proj_name in Projects
98. **SELECT name, (SELECT COUNT(*) FROM Works_On WHERE emp_id = e.emp_id) AS num_projects FROM Employees e WHERE EXISTS (SELECT 1 FROM Works_On WHERE emp_id = e.emp_id);** Retrieves employee names along with the number of projects they are working on, for employees working on at least one project.
- **Minimum Tuples:** 0 (if no employees work on any projects)
 - **Maximum Tuples:** Total number of rows in Employees
99. **SELECT dept_name, (SELECT COUNT(*) FROM Employees WHERE dept_id = d.dept_id) AS num_employees FROM Departments d WHERE EXISTS (SELECT 1 FROM Employees WHERE dept_id =**

d.dept_id); Retrieves department names along with the number of employees, for departments that have employees.

- **Minimum Tuples:** 0 (if no departments have employees)
- **Maximum Tuples:** Number of unique dept_name in Departments

100.SELECT proj_name, (SELECT SUM(salary) FROM Employees e JOIN Works_On w ON e.emp_id = w.emp_id WHERE w.proj_id = p.proj_id) AS total_salary FROM Projects p; Retrieves project names along with the total salary of employees working on each project.

- **Minimum Tuples:** 0 (if Projects table is empty)
- **Maximum Tuples:** Number of unique proj_name in Projects