

Q1 What are the components in a HAWT type wind turbine system? Describe the function of each component.
 Blade pitch system: control power output and protect the turbine in strong wind by adjusting the blade's angle of attack
 Yaw system: Adjust the direction of the wind rotor to face the wind
 Gearbox: Increase rotational speed, converting low-speed rotation to a speed suitable for the generator $\sim 1/100$
 Generator: Convert mechanical energy into electrical energy

Q2 Why are wind turbine rotor blades twisted towards the end?
 For a constant rotational speed, the speed of the rotor along the blade is proportional to the distance from the hub. The nearer to the tip (further from the hub), the stronger the apparent wind is. Blade must be twisted to keep the angles right to maximize the lift-to-drag force ratio

Q3 What is the specific power in wind at a location with wind speed of 5 m/s? Determine the theoretical maximum power output of a 40-m diameter wind turbine generator at this location. Assume density of air to be 1.225 kg/m³.
 $P_{\text{max}} = \frac{1}{2} \rho A v^3 = \frac{1}{2} \times 1.225 \times \pi \times 40^2 \times 5^3 = 176.5 \text{ kW}$
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Q4 The wind speed in a city area is 5 m/s at a height of 10m. The location has a friction coefficient of 0.4. What is the specific power at a height of 50m? Assume density of air to be 1.225 kg/m³.
 $\left(\frac{v}{v_0}\right)^a = \left(\frac{z}{z_0}\right)^b \Rightarrow v = v_0 \left(\frac{z}{z_0}\right)^{\frac{1}{b}}$
 $\left(\frac{v}{5}\right)^{0.14} = \left(\frac{50}{10}\right)^{0.14} \Rightarrow v = 9.52 \text{ m/s}$
 $P_{\text{max}} = \frac{1}{2} \rho A v^3 = \frac{1}{2} \times 1.225 \times \pi \times 40^2 \times 9.52^3 = 1.225 \text{ kW}$

Q5 At tip-speed-ratio of 5, what is the rpm of the wind turbine rotor with a diameter of 40m, if the wind speed is 10 m/s?
 $\text{Tip speed ratio} = \frac{\text{Rotor tip speed}}{\text{Wind speed}} = \frac{v_{\text{tip}} \times r}{v_{\text{wind}}} = 5$
 $v_{\text{tip}} = \frac{5 \times v_{\text{wind}}}{r} = \frac{5 \times 10}{20} = 2.5 \text{ m/s}$
 $\omega = \frac{v_{\text{tip}}}{r} = \frac{2.5}{20} = 0.125 \text{ rad/s}$
 $\text{rpm} = \frac{\omega \times 60}{2\pi} = \frac{0.125 \times 60}{2\pi} = 1.19 \text{ rpm}$

Example: A wind turbine with a 30-m rotor diameter is mounted with its hub at 50 m above a ground surface that is characterized by shrubs and hedges. Estimate the ratio of specific power in the wind at the highest point that a rotor blade tip reaches to the lowest point that it falls to.
 $\left(\frac{v}{v_0}\right)^a = \left(\frac{z}{z_0}\right)^b \Rightarrow v = v_0 \left(\frac{z}{z_0}\right)^{\frac{1}{b}}$
 $\left(\frac{v}{5}\right)^{0.14} = \left(\frac{80}{50}\right)^{0.14} \Rightarrow v = 6.0 \text{ m/s}$

Q6 Explain how the rotor blades in a wind turbine get the required thrust to rotate.
 Air moving over top of airfoil has more distance to travel \rightarrow Air pressure on top is lower than under airfoil \rightarrow Lift is created

Q7 What are the various methods used for varying the main components of wind turbine rotor speed based on wind speed?
 • Adjust angle of attack at the turbine blades
 • Stall or pitch control
 • Mechanical parts: Gear box, yaw control, Turbine blade

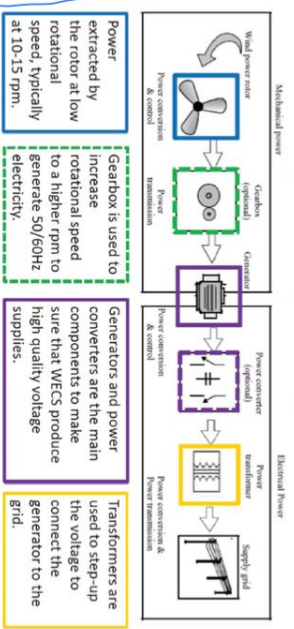
Q8 Draw the complete block diagram of the wind energy conversion system to convert wind energy to electricity for the grid. Briefly explain the function of each block.

Q9 Using appropriate equations explain why it is economical to increase the size of the wind turbine rotor.
 The larger the diameter of its blades, the more power it is capable of extracting from the wind. Doubling the diameter increases the power available by a factor of 4. The cost of a turbine increases roughly in proportion to blade diameter, but power is proportional to diameter squared so bigger machines have proven to be more cost effective.

Q10 Explain the cause of rotor stress in large wind turbines.
 As seen in the previous example, the blade at the top of its rotation can experience much higher wind speeds than at the bottom of its rotation. This results in flexing of the blade. It can also:
 • Increase noise.
 • Contribute to blade fatigue, which can lead to blade failure.

Q11 From first principle, derive Betz's Law for retrieving maximum energy from wind using a wind turbine.
 Define Rotor efficiency as,
 $C_p = \frac{1}{2} (1 + \lambda) (1 - \lambda^2)$
 Fundamental relationship for power delivered by the rotor,
 $P_b = \frac{1}{2} \rho A v^3 \cdot C_p$

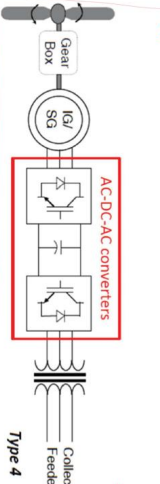
Main Components of Wind Energy Conversion Systems (WECS)



Rotor Efficiency

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Type 4: Indirect Grid Connection



Q12 What is the tip speed ratio (TSR) of wind turbine? How does TSR affect the rotor efficiency of a wind turbine?
 For a given wind speed, the rotor efficiency depends on the speed of rotation of the blades.
 TSR is the speed at rotor tip divided by the wind speed.
 $\text{TSR} = \frac{\text{Rotor tip speed}}{\text{Wind speed}} = \frac{v_{\text{tip}} \times r}{v_{\text{wind}}}$
 If TSR is high, it means that the blade spins too fast, and that the blade will experience turbulent wind.
 If TSR is low, it means that the blade spins too slowly, and it can't efficiently capture wind energy.

Q13 Describe the various types of wind turbine generators based on type of speed control.
 WTGs Classification by Speed Control
 Wind turbine generators can be divided into 5 types.
 1. Type 1: Fixed speed (1-2% variation)
 2. Type 2: Limited variable speed (10% variation)
 3. Type 3: Variable speed with partial power electronic conversion (30% variation)
 4. Type 4: Variable speed with full power electronic conversion (full variation)
 5. Type 5: Variable speed with mechanical torque converter to control synchronous speed (full variation)

Q14 Using block diagram, describe the various types of variable speed wind turbine generator systems with electrical control on generator side.
 Type 2: Variable Speed Systems
 Type 3: Doubly Fed Induction Generator (DFIG)
 Type 4: Indirect Grid Connection

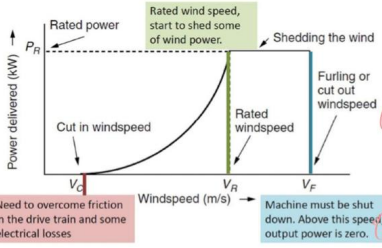
Q15 Using block diagram, explain the operation of wind turbine system with a doubly fed induction generator (DFIG).
 Instead of variable resistors in Type 2, this Type 3 design adds AC-DC-AC converters to the rotor circuit.
 Rotor frequency is decoupled from grid frequency.
 The machine can still be synchronized with the grid while the wind speed varies.

Q16 Using block diagram, explain the operation of variable turbine speed, type 4 wind turbine system with a Synchronous generator.
 Q17 Draw the ideal power delivered vs wind speed curve for a wind turbine generator. Clearly explain the operation at different wind speed.

Q18 What is meant by wind shedding?
 Explain the various methods for shedding wind power?

Wind shedding refers to the intentional reduction of power output to protect the turbine during high winds. Methods include:
 Pitch-controlled turbines
 - Active control by reducing 'angle of attack'
 Stall-controlled turbines.
 - Passive control using pure aerodynamic design.
 Active stall control.
 - Induce stall for large wind turbine by increasing 'angle of attack'.
 Passive yaw control
 - Small kW size turbine, causing axis of turbine to move off the wind.

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Average Wind Speed Calculation

Miles of wind = 3 h · 0 mile/hr + 3 h · 5 mile/hr + 4 h · 10 mile/hr
Total hours = 3 + 3 + 4 h
 $v_{avg} = \left(\frac{3 \text{ h}}{10 \text{ h}}\right) \times 0 \text{ mph} + \left(\frac{3 \text{ h}}{10 \text{ h}}\right) \times 5 \text{ mph} + \left(\frac{4 \text{ h}}{10 \text{ h}}\right) \times 10 \text{ mph} = 5.5 \text{ mph}$
A more general expression for the above two equations would be:
$$v_{avg} = \frac{\sum_i [v_i \cdot (\text{hours @ } v_i)]}{\sum_i \text{hours}} = \sum_i [v_i \cdot \left(\frac{\text{fraction of hours @ } v_i}{1}\right)]$$

$$(v^3)_{avg} = \frac{\sum_i [v_i^3 \cdot (\text{hours @ } v_i)]}{\sum_i \text{hours}} = \sum_i [v_i^3 \cdot \left(\frac{\text{fraction of hours @ } v_i}{1}\right)]$$

$$(v^3)_{avg} = \sum_i [v_i^3 \cdot \text{probability}(v = v_i)]$$

The table below gives the measurement of wind speed during one day. Calculate the total energy generated for the day using a 40-m diameter rotor wind turbine generator with rotor efficiency 0.40 and generator efficiency 0.85. The cut-in speed is 3 m/s and cut-out speed is 9 m/s. Assume there is no wind shedding.

$D = 40 \text{ m}$
 $\rho = 1.225 \text{ kg/m}^3$
 $A = \frac{\pi}{4} D^2 = 1256.64 \text{ m}^2$

Wind speed (m/s)	Number of hours recorded during the day
1	5
2	3
4	4
7	6
8	3
10	2

$P_w = \frac{1}{2} \rho A v^3$
 $P_{w1} = 49.16 \text{ kW}$
 $P_{w2} = 26.4 \text{ kW}$
 $P_{w3} = 399.08 \text{ kW}$
 $P_{act} = P_w \cdot 0.4 \cdot 0.85$
 $P_{act1} = 16.74 \text{ kW}$
 $P_{act2} = 8.76 \text{ kW}$
 $P_{act3} = 131.79 \text{ kW}$
 $E = P_{act} \cdot \text{hours}$
 $E_{tot} = \sum E_i = 1141.51 \text{ kWh}$

Rayleigh PDF: Average Wind Speed

From $f(v) = \frac{2v}{c^3} \exp\left[-\left(\frac{v}{c}\right)^2\right]$
 $\bar{v} = \int_0^\infty v \cdot f(v) dv = \int_0^\infty v \cdot \frac{2v}{c^3} \exp\left[-\left(\frac{v}{c}\right)^2\right] dv$
 $= \frac{\sqrt{\pi}}{2} c \approx 0.886c$
Or, we can write: $c = \frac{2}{\sqrt{\pi}} \bar{v} \approx 1.128 \bar{v}$

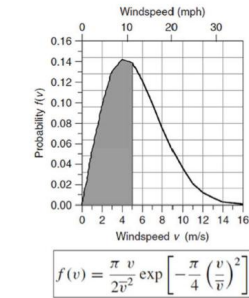
The Rayleigh probability density function can be written as follows in terms of average wind speed.

Rayleigh PDF: Average Power

Coupling average windspeed with the assumption that the wind speed distribution follows Rayleigh statistics enables us to find the average power in the wind.

$P_{avg} = \frac{1}{2} \rho A (v^3)_{avg}$
 $(v^3)_{avg} = \int_0^\infty v^3 \cdot f(v) dv$
 $= \int_0^\infty v^3 \cdot \frac{2v}{c^3} \exp\left[-\left(\frac{v}{c}\right)^2\right] dv = \frac{3}{4} c^3 \sqrt{\pi}$
Substitute $c = \frac{2}{\sqrt{\pi}} \bar{v} \Rightarrow (v^3)_{avg} = \frac{3}{4} \sqrt{\pi} \left(\frac{2\bar{v}}{\sqrt{\pi}}\right)^3$
 $= \frac{6}{\pi} \bar{v}^3 = 1.91 \bar{v}^3$
 $\bar{P} = \frac{6}{\pi} \cdot \frac{1}{2} \rho A \bar{v}^3$

Probability Approximation



at 6 m/s the NEG Micon 1000/60 generates 150 kW the Rayleigh p.d.f. at 6 m/s in a regime with 7-m/s average windspeed is

$f(v) = \frac{\pi v}{2\bar{v}^2} \exp\left[-\frac{\pi}{4} \left(\frac{v}{\bar{v}}\right)^2\right]$
 $= \frac{\pi \cdot 6}{2 \cdot 7^2} \exp\left[-\frac{\pi}{4} \left(\frac{6}{7}\right)^2\right] = 0.10801$

In a year with 8760 h, our estimate of the hours the wind blows at 6 m/s is

Hours @ 6 m/s = 8760 h/yr × 0.10801 = 946 h/yr

So the energy delivered by 6-m/s winds is

Energy (@ 6 m/s) = 150 kW × 946 h/yr = 141,929 kWh/yr

Do this for all speeds and add them up!

The overall average efficiency of this turbine

Windspeed (m/s)	Power (kW)	Probability f(v)	Hs/yr at v	Energy (kWh/yr)
0	0	0.000	0	0
1	0	0.002	276	0
2	0	0.060	527	0
3	0	0.083	729	0
4	31	0.099	869	28,683
5	86	0.107	941	80,885
6	150	0.108	946	141,929
7	248	0.102	896	222,271
8	385	0.092	805	310,076
9	535	0.079	690	360,126
10	670	0.065	565	378,785
11	780	0.051	444	346,435
12	864	0.038	335	289,551
13	924	0.028	243	224,707
14	964	0.019	170	163,779
15	989	0.013	114	113,103
16	1000	0.008	74	74,218
17	998	0.005	46	46,371
18	987	0.003	28	27,708
19	968	0.002	16	15,853
20	944	0.001	9	8,709
21	917	0.001	5	4,604
22	889	0.000	3	2,347
23	863	0.000	1	1,158
24	840	0.000	1	554
25	822	0.000	0	257
26	0	0.000	0	0
Total:				2,851,109

average power in the wind for a 60-m rotor diameter

$\bar{P} = \frac{6}{\pi} \cdot \frac{1}{2} \rho A \bar{v}^3$
 $= \frac{6}{\pi} \times 0.5 \times 1.225 \times \frac{\pi}{4} (60)^2 \times (7)^3$
 $= 1.134 \times 10^6 \text{ W} = 1134 \text{ kW}$

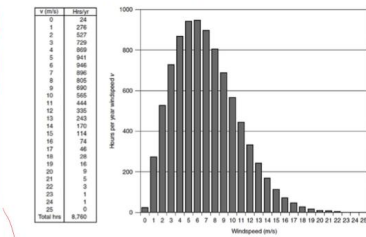
In a year with 8760 h, the energy in the wind is

Energy in wind = 8760 h/yr × 1134 kW = 9,938 × 10⁶ kWh

Average efficiency = $\frac{2.85 \times 10^6 \text{ kWh/yr}}{9.938 \times 10^6 \text{ kWh/yr}} = 0.29 = 29\%$

Example

Using the data given below, find the average windspeed and the average power in the wind (W/m²). Assume air density = 1.225 kg/m³.



Solution

The average windspeed is

$v_{avg} = \sum_i [v_i \cdot (\text{Fraction of hours @ } v_i)] = 7.0 \text{ m/s}$

The average value of v³ is

$(v^3)_{avg} = \sum_i [v_i^3 \cdot (\text{Fraction of hours @ } v_i)] = 653.24$

The average power in the wind is

$P_{avg} = \frac{1}{2} \rho (v^3)_{avg} = 0.5 \times 1.225 \times 653.24 = 400 \text{ W/m}^2$

If we had miscalculated average power in the wind using the 7 m/s average windspeed, we would have found:

$P_{average}(\text{WRONG}) = \frac{1}{2} \rho (v_{avg})^3$
 $= 0.5 \times 1.225 \times 7^3 = 210 \text{ W/m}^2$

Example

A wind turbine system with a DFIG mainly includes a wind turbine, a gearbox, a DFIG, and a control system. The wind turbine converts wind energy into mechanical rotation. The gearbox adjusts the speed. The DFIG has its stator directly connected to the grid and its rotor connected to the grid via a power converter. The control system monitors parameters like wind speed and rotor speed, and sends signals to the power converter to adjust the rotor excitation for optimal operation.

Example

Estimate the average power in the wind at a height of 50 m when the wind speed at 10 m averages 6 m/s.

Assume Rayleigh statistics;

Standard friction coefficient $\alpha = \frac{1}{7}$;

Standard air density $\rho = 1.225 \frac{\text{kg}}{\text{m}^3}$.

Solution

We first adjust the winds at 10 m to those expected at 50 m

$\bar{v}_{50} = \bar{v}_{10} \left(\frac{H_{50}}{H_{10}}\right)^{\alpha} = 6 \cdot \left(\frac{50}{10}\right)^{1/7} = 7.55 \text{ m/s}$

the average wind power density would be

$\bar{P}_{50} = \frac{6}{\pi} \cdot \frac{1}{2} \rho \bar{v}^3$
 $= \frac{6}{\pi} \cdot \frac{1}{2} \cdot 1.225 \cdot (7.55)^3 = 504 \text{ W/m}^2$

Average Efficiency

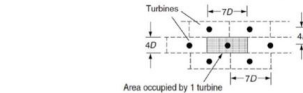
Average power in the wind (W/m²) → Power extracted from the wind (W/m²), depending turbine blade (rotor) efficiency → Electrical power output (W/m²), depending on the gearbox and generator efficiency

$P_{wind} = \frac{1}{2} \rho A \omega^3$
 $P_{blade} = \frac{1}{2} \rho A \omega^3 \cdot C_p$
(Assume $C_p = 0.45$)

Overall efficiency = $\frac{P_{electrical}}{P_{wind}} = 0.45 \times \frac{2}{3} = 0.3 = 30\%$

Example

Suppose that a wind farm has 4-rotor-diameter tower spacing along its rows, with 7-diameter spacing between rows (4D × 7D). Assume 30% wind turbine efficiency and an array efficiency of 80%.



Find the annual energy production per unit of land area in an area with 400-W/m² winds at hub height (the edge of 50 m, Class 4 winds).

$\frac{\text{Energy}}{\text{Land area}} = \frac{\text{Power density of wind turbine} \times \text{swept area of rotor} \times \text{turbine efficiency} \times \text{array efficiency} \times \text{hours per year}}{\text{land area for one turbine}}$

Solution

The land area occupied by one turbine is 4D × 7D = 28D².

The rotor area $\frac{\pi}{4} D^2$.

The yearly energy produced by one turbine =

$= \text{Wind power density} \times \text{rotor area} \times \text{turbine efficiency} \times \text{array efficiency} \times \text{hours per year}$
 $= 400 \times \frac{\pi}{4} D^2 \times 0.3 \times 0.8 \times 8760 = 660153.6 D^2$
 $\frac{\text{Energy}}{\text{Land Area}} = \frac{660153.6 D^2}{28 D^2} = 23.58 \text{ kWh/m}^2$

Example

Suppose that a NEG Micon 60-m diameter wind turbine having a rated power of 1000 kW is installed at a site having Rayleigh wind statistics with an average wind speed of 7m/s at the hub height. The generator output for various wind speeds are given on the right.

- a) Find the annual energy generated.
- b) From the result, find the overall average efficiency of this turbine in these winds.
- c) Find the productivity in terms of kWh/yr delivered per m² of swept area.

	Manufacturer	NEG
	Rated Power (kW)	Micon
	Diameter (m)	60
Avg. Windspeed		
v (m/s)	(cmph)	kW
0	0	0
1	2.2	0
2	4.5	0
3	6.7	0
4	8.9	33
5	11.2	80
6	13.4	150
7	15.7	248
8	17.9	385
9	20.1	535
10	22.4	690
11	24.6	780
12	26.8	864
13	29.1	924
14	31.3	964
15	33.6	980
16	35.8	987
17	38.0	988
18	40.3	987
19	42.5	968
20	44.7	944
21	47.0	917
22	49.2	889
23	51.5	863
24	53.7	840
25	55.9	822
26	58.2	0

$CF = \frac{\text{Actual Energy}}{\text{Rated Power} \times 8760}$

Solution

Assumption: Rayleigh wind statistics with average wind speed of 7m/s at hub height.

Step 1: Find the probability of each wind speed. How?

Step 2: Find the energy produced at each wind speed.

Step 3: Annual energy generated = summation of energy produced at each wind speed

Annual Energy Production: Capacity Factor Method

Capacity factor is a measure of the fraction of actual energy delivered to the rated energy output in one year.

$CF = \frac{\text{Actual energy delivered}}{\text{Rated power} \times 8760}$

Annual energy (kWh/yr) = P_R (kW) × 8760 (h/yr) × CF

where P_R is the rated power (kW) and CF is the capacity factor

$CF = \frac{\text{Actual energy delivered}}{P_R \times 8760}$

another way to express it is

$CF = \frac{\text{Actual energy delivered}/8760 \text{ h/yr}}{P_R} = \frac{\text{Average power}}{\text{Rated power}}$

- Dimensionless quantity between 0 and 1.
- CF is meant for calculating 'actual energy delivered' given that we know the rated power.

Estimate of energy delivered from a turbine of diameter D:

Annual energy (kWh/yr) = 8760 · P_R (kW) $\left\{ 0.087 \bar{V} (\text{m/s}) - \frac{P_R (\text{kW})}{[D (\text{m})]^2} \right\}$