

Q1 What are the components in a HAWT type wind turbine system? Describe the function of each component.
 Yaw system: Adjust the direction of the wind rotor to face the wind
 Gearbox: Increase rotational speed converting low-speed rotation to a speed suitable for the generator
 Generator: Convert mechanical energy into electrical energy

Q2 Why are wind turbine rotor blades twisted towards the end?
 For a constant rotational speed, the speed of the rotor along the blade is proportional to the distance from the hub. The nearer the tip (further from the hub), the stronger the apparent wind is. Blade must be twisted to keep the angles right to maximize the lift-to-drag force ratio

Q3 What is the specific power in wind at a location with wind speed of 5 m/s? Determine the theoretical maximum power output of a 40-m diameter wind turbine generator at this location. Assume density of air to be 1.225 kg/m³.

$P_w = \frac{1}{2} \rho A v^3$

$$P_w = \frac{1}{2} \pi D^2 \times \frac{1}{2} \times 1.225 \times 5^3 = 76.55W$$

$$\text{specific power} = P_{\text{power per meter}} = \frac{P}{L} = \frac{P}{V \cdot A \cdot H}$$

$$V \cdot A \cdot H = A = \frac{1}{4} \pi D^2 \cdot H$$

$$= 9421.1 \cdot 5^3 = 1921.1 \cdot 5^3 = 1921.1 \cdot 125 = 24013.75W$$

Q4 The wind speed in a city area is 5 m/s at a height of 10m. The location has a friction coefficient of 0.4. What is the specific power at a height of 50m? Assume density of air to be 1.225 kg/m³.

$$\left(\frac{V}{V_0}\right) = \left(\frac{H}{H_0}\right)^{\alpha} \Rightarrow \frac{V}{V_0} = \left(\frac{H}{H_0}\right)^{0.4} \Rightarrow V = 9.52 \cdot V_0$$

$$\left(\frac{P}{P_0}\right) = \left(\frac{H}{H_0}\right)^{\alpha} \Rightarrow \frac{P}{P_0} = \left(\frac{H}{H_0}\right)^{0.4} = \left(\frac{H}{H_0}\right)^{0.4} = \left(\frac{H}{H_0}\right)^{0.4}$$

$$P_0 = \frac{1}{2} \rho A v^3 \Rightarrow P = \frac{1}{2} \rho A \left(9.52 \cdot V_0\right)^3 = 538.47W$$

$$\text{tip speed ratio} = \frac{\text{Rotor tip speed rpm} \times \pi D}{\text{Wind speed}} = \frac{60 \times 5}{60 \times 10} = 5$$

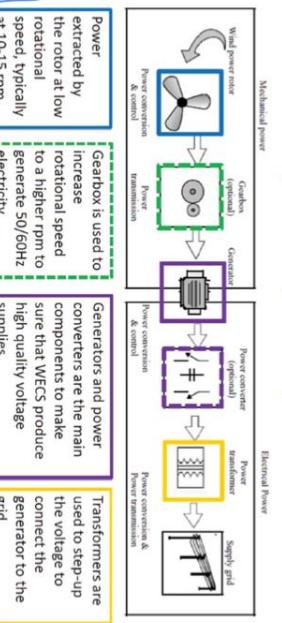
Q5 At tip-speed-ratio of 5, what is the rpm of the wind turbine rotor with a diameter of 40m, if the wind speed is 10 m/s?

$$10 \times 40 \times \pi = 1257 \text{ rpm}$$

Q6 Explain how the rotor blades in a wind turbine get the required thrust to rotate. Air moving over top of airfoil has more distance to travel \rightarrow Air pressure on top is lower than under airfoil \rightarrow Lift is created

Q7 What are the various methods used for varying the wind turbine rotor speed based on wind speed?

Main Components of Wind Energy Conversion Systems (WECS)



Q8 Draw the complete block diagram of the wind energy conversion system to convert wind energy to electricity for the grid. Briefly explain the function of each block.

Mechanical parts: Gear box, Yaw control, Turbine blade

• Stall or pitch control

Q9 Using appropriate equations, explain why it is economical to increase the size of the wind turbine.

The larger the diameter of its blades, the more power it is capable of extracting from the wind. Doubling the diameter increases the power available by a factor of 4. The cost of a turbine increases roughly in proportion to blade diameter but power is proportional to diameter squared, so bigger machines have proven to be more cost effective.

Q10 Explain the cause of rotor stress in large wind turbines.

As seen in the previous example, the blade at the top of its rotation can experience much higher wind speeds than at the bottom of its rotation. This results in flexing of the blade. It can also:

- Increase noise.
- Contribute to blade fatigue, which can lead to blade failure.

$$P_w = \frac{1}{2} \rho A v^3$$

$$C_p = \frac{1}{2} (1 + \lambda) (1 - \lambda^2)$$

Fundamental relationship for power delivered by the rotor,

$$P_b = \frac{1}{2} \rho A v^3 \cdot C_p$$

Define Rotor efficiency as,

$$\eta = \frac{P_b}{P_w} = \frac{1}{2} (1 + \lambda) (1 - \lambda^2)$$

From first principle, derive Betz's Law for retrieving maximum energy from wind using a wind turbine.

Q11 From first principle, derive Betz's Law for retrieving maximum energy from wind using a wind turbine.

Q12 What is the tip speed ratio (TSR) of wind turbine? How does TSR affect the rotor efficiency of a wind turbine?

• For a given wind speed, the rotor efficiency depends on the speed of rotation of the blades.

• TSR is the speed at rotor tip divided by the wind speed.

$$\text{Rotor tip speed} = \frac{\text{rpm} \times \pi D}{60 \text{ s}} \quad \text{D: diameter (m)} \quad \text{v: wind speed (m/s)}$$

- If TSR is high, it means that the blade spins too fast, and that the blade will experience turbulent wind.

- If TSR is low, it means that the blade spins too slowly, and it can't fully capture wind energy.

The optimal TSR gives the maximum efficiency that a turbine can extract wind energy.

Q13 Describe the various types of wind turbine generators based on type of speed control used.

WTGs Classification by Speed Control

Wind turbine generators can be divided into 5 types.

1. Type 1: Fixed speed (1-2% variation)
2. Type 2: Limited variable speed (10% variation)
3. Type 3: Variable speed with partial power electronic conversion (30% variation)
4. Type 4: Variable speed with full power electronic conversion (full variation)
5. Type 5: Variable speed with mechanical torque converter to control synchronous speed (full variation)

$$(a) \text{Tip-Speed-Ratio (TSR)} = \frac{\text{Rotor tip speed}}{\text{Wind speed}} = \frac{\text{rpm} \times \pi D}{60 v}$$

$$(b) \text{The tip of each blade is moving at}$$

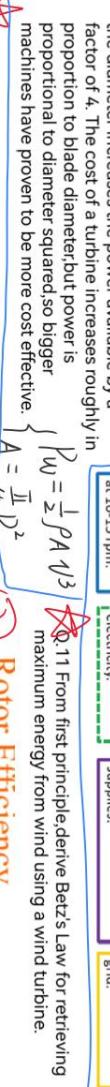
$$\text{Tip speed} = \frac{26.7 \text{ rev/min} \times \pi 40 \text{ m}}{60 \text{ s/min}} = 55.9 \text{ m/s}$$

Out of the generator is given as 600 kW.

$$\text{Overall efficiency} = \frac{600 \text{ kW}}{2112 \text{ kW}} = 0.284 = 28.4\%$$

Q14 Using block diagram, describe the various types of variable speed wind turbine generator systems with electrical control on generator side.

Type 2: Variable Speed Systems (VSIS)

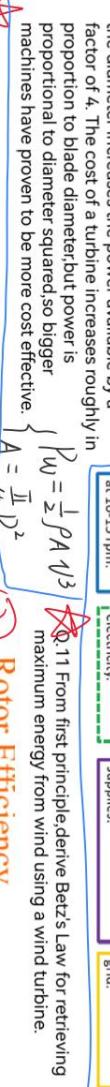


Induction generators

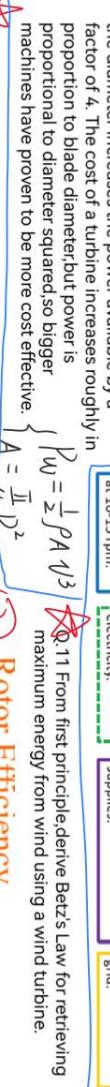
• For a given wind speed, rotor efficiency is a function of the rate at which a rotor turns.

- If Rotor turns too slow letting too much wind to pass \Rightarrow efficiency drops.

- If Rotor turns too fast causing turbulence \Rightarrow efficiency drops.



Q15 Using block diagram, explain the operation of wind turbine system with a doubly fed induction generator (DFIG).



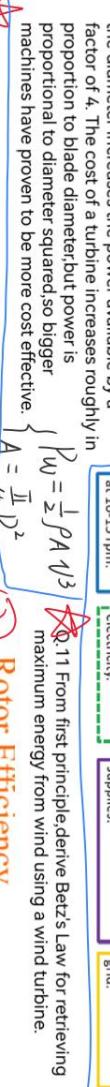
Type 3: Doubly Fed Induction Generator (DFIG)

Instead of variable resistors in Type 2, this Type 3 design adds AC-DC-AC converters to the rotor circuit.

Rotor frequency is decoupled from grid frequency.

The machine can still be synchronized with the grid while the wind speed varies.

Q16 Using block diagram, explain the operation of variable speed, type 4 wind turbine system with Synchronous generator.



Type 4: Indirect Grid Connection

Allows the turbine to rotate at its optimal speed. AC output from generator frequency is different and decoupled from grid frequency.

Full control and flexibility in the design and operation of wind turbine. The ratings of power electronics are higher than Type 3.

Q17 Draw the ideal power delivered vs wind speed curve for a wind turbine generator. Clearly explain the operation at different wind speeds.

Q18 What is meant by wind shedding? Explain the various methods for shedding wind power?

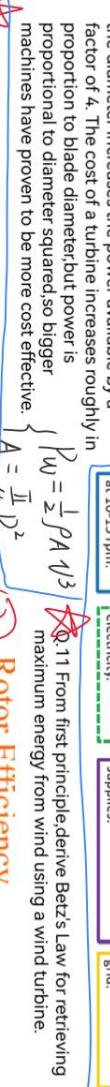
Wind shedding refers to the intentional reduction of power output to protect the turbine during high winds. Methods include:

Pitch-controlled turbines

- Active control by reducing 'angle of attack'
- Passive control using pure aerodynamic design.

Active stall control

- Induce stall for large wind turbine by increasing 'angle of attack'.
- Small kW size turbine, causing axis of turbine to move off the wind.



Need to overcome friction in the drive train and some electrical losses

Rated wind speed, start to shed some of wind power.

Cutting in wind speed

Rated power

Shedding the wind

Rated wind speed

Furling or cut out wind speed

Machine must be shut down. Above this speed, output power is zero.

Average Wind Speed calculation

$$v_{avg} = \frac{\text{Miles of wind}}{\text{Total hours}} = \frac{3 \text{ h} \cdot 0 \text{ mile/hr} + 3 \text{ h} \cdot 5 \text{ mph} + 4 \text{ h} \cdot 10 \text{ mile/hr}}{3 + 3 + 4 \text{ h}}$$

$$v_{avg} = \left(\frac{3 \text{ h}}{10 \text{ h}} \right) \times 0 \text{ mph} + \left(\frac{3 \text{ h}}{10 \text{ h}} \right) \times 5 \text{ mph} + \left(\frac{4 \text{ h}}{10 \text{ h}} \right) \times 10 \text{ mph} = 5.5 \text{ mph}$$

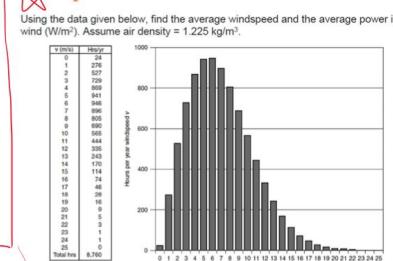
A more general expression for the above two equations would be:

$$v_{avg} = \frac{\sum_i [v_i \cdot (\text{hours} @ v_i)]}{\sum_i \text{hours}} = \sum_i [v_i \cdot (\text{fraction of hours} @ v_i)]$$

$$(v^3)_{avg} = \frac{\sum_i [v_i^3 \cdot (\text{hours} @ v_i)]}{\sum_i \text{hours}} = \sum_i [v_i^3 \cdot (\text{fraction of hours} @ v_i)]$$

$$(v^3)_{avg} = \sum_i [v_i^3 \cdot \text{probability}(v = v_i)]$$

Example



The table below gives the measurement of wind speed during one day. Calculate the total energy generated for the day using a 40-m diameter rotor wind turbine generator with rotor efficiency 40% and generator efficiency 85%. The cut-in speed is 3 m/s and cut-out speed is 9 m/s. Assume there is no wind shedding.

Wind speed (m/s)	Number of hours recorded during the day
1	5
2	3
4	4
7	6
8	4
10	2

$$P_{wind} = \frac{1}{2} \rho A v^3 \quad P_{avg} = 49.26 \text{ kW} \quad P_{cut} = 26.4 \text{ kW} \quad P_{out} = 394.08 \text{ kW}$$

$$P_{out} = P_{cut} \cdot 0.4 - 0.85 \quad P_{out} = 16.73 \text{ kW} \quad P_{out} = 87.76 \text{ kW} \quad P_{out} = 133.94 \text{ kW}$$

$$E = P_{out} \cdot \text{hours} \quad E_{all} = \sum E_b = 114.13 \text{ kWh}$$

Weibull PDF: Average Wind Speed

From $f(v) = \frac{2v}{c^2} \exp\left[-\left(\frac{v}{c}\right)^2\right]$

$$\bar{v} = \int_0^\infty v \cdot f(v) dv = \int_0^\infty \frac{2v^2}{c^2} \exp\left[-\left(\frac{v}{c}\right)^2\right] dv$$

$$= \frac{\sqrt{\pi}}{2} c \cong 0.886c$$

Or, we can write: $c = \frac{2}{\sqrt{\pi}} \bar{v} \cong 1.128 \bar{v}$

The Rayleigh probability density function can be written as follows in terms of average wind speed.

$$f(v) = \frac{\pi}{2\bar{v}^2} \exp\left[-\frac{\pi}{4}\left(\frac{v}{\bar{v}}\right)^2\right]$$

Rayleigh PDF: Average Power

Coupling average windspeed with the assumption that the wind speed distribution follows Rayleigh statistics enables us to find the average power in the wind.

$$P_{avg} = \frac{1}{2} \rho A (v^3)_{avg}$$

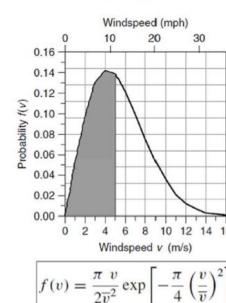
$$(v^3)_{avg} = \int_0^\infty v^3 \cdot f(v) dv$$

$$= \int_0^\infty v^3 \cdot \frac{2v}{c^2} \exp\left[-\left(\frac{v}{c}\right)^2\right] dv = \frac{3}{4} c^3 \sqrt{\pi}$$

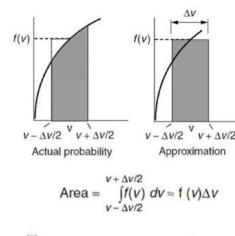
Substitute $c = \frac{2}{\sqrt{\pi}} \bar{v}$ $\Rightarrow (v^3)_{avg} = \frac{3}{4} \sqrt{\pi} \left(\frac{2\bar{v}}{\sqrt{\pi}}\right)^3 = \frac{6}{\bar{v}^3} = 1.91 \bar{v}^3$

$$\bar{P} = \frac{6}{\pi} \frac{1}{2} \rho A \bar{v}^3$$

Probability Approximation



We can discretize a continuous PDF and say that the probability that the wind blows at v is just $f(v)$.



at 6 m/s the NEG Micon 1000/60 generates 150 kW
the Rayleigh p.d.f. at 6 m/s in a regime with 7-m/s average windspeed is

$$f(v) = \frac{\pi v}{2\bar{v}^2} \exp\left[-\frac{\pi}{4}\left(\frac{v}{\bar{v}}\right)^2\right]$$

$$= \frac{\pi \cdot 6}{2 \cdot 7^2} \exp\left[-\frac{\pi}{4}\left(\frac{6}{7}\right)^2\right] = 0.10801$$

In a year with 8760 h, our estimate of the hours the wind blows at 6 m/s is

$$\text{Hours @ 6 m/s} = 8760 \text{ h/yr} \times 0.10801 = 946 \text{ h/yr}$$

So the energy delivered by 6-m/s winds is

$$\text{Energy (@6 m/s)} = 150 \text{ kW} \times 946 \text{ h/yr}$$

$$= 141,929 \text{ kWh/yr}$$

Do this for all speeds and add them up!

The overall average efficiency of this turbine

Windspeed (m/s)	Power (kW)	Probability $f(v)$	Hrs/yr at v	Energy (kWh/yr)
0	0	0.000	0	0
1	0	0.032	276	0
2	0	0.083	527	0
3	0	0.083	729	0
4	33	0.099	869	28.683
5	86	0.107	941	80.885
6	160	0.107	640	141.929
7	248	0.102	896	222.271
8	385	0.092	805	310.076
9	535	0.079	690	366.126
10	680	0.065	563	378.786
11	780	0.051	444	346.435
12	864	0.038	335	289.551
13	924	0.028	243	224.707
14	944	0.020	179	165.799
15	989	0.013	114	113.101
16	1000	0.008	74	74.218
17	998	0.005	46	46.371
18	968	0.002	20	27.769
19	988	0.002	16	15.853
20	944	0.003	9	8.709
21	917	0.001	5	4.604
22	854	0.000	3	2.347
23	863	0.000	1	1.158
24	840	0.000	1	0.554
25	822	0.000	0	0.257
26	0	0.000	0	0
Total:				2,851,109

average power in the wind for a 60-m rotor diameter

$$\bar{P} = \frac{6}{\pi} \frac{1}{2} \rho A \bar{v}^3$$

$$= \frac{6}{\pi} \times 0.5 \times 1.225 \times \frac{\pi}{4} (60)^2 \times (7)^3$$

$$= 1.134 \times 10^6 \text{ W} = 1134 \text{ kW}$$

In a year with 8760 h, the energy in the wind is

$$\text{Energy in wind} = 8760 \text{ h/yr} \times 1134 \text{ kW}$$

$$= 9.938 \times 10^6 \text{ kWh}$$

$$\text{Average efficiency} = \frac{2.85 \times 10^6 \text{ kWh/yr}}{9.938 \times 10^6 \text{ kWh/yr}}$$

$$= 0.29 = 29\%$$

Overall Efficiency

CF = $\frac{P_{electrical}}{P_{wind}}$

Average power extracted from the wind (W/m^2)

Power extracted from the wind (W/m^2), depending turbine blade (rotor) efficiency

Electrical power output (W/m^2), depending on the gearbox and generator efficiency

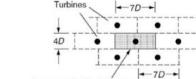
$$P_{wind} = \frac{1}{2} \rho A \omega^3 \quad P_{blade} = \frac{1}{2} \rho A \omega^3 \cdot C_p \quad (\text{Assume } C_p = 0.45)$$

$$\text{Overall efficiency} = \frac{P_{electrical}}{P_{wind}} = 0.45 \times \frac{2}{3} = 0.3 = 30\%$$

Example

Suppose that a wind farm has 4-rotor-diameter tower spacing along its rows, with 7-diameter spacing between rows ($4D \times 7D$).

Assume 30% wind turbine efficiency and an array efficiency of 80%.



Find the annual energy production per unit of land area in an area with 400-W/m² winds at hub height (the edge of 50 m, Class 4 winds).

$$\text{Energy} = \frac{\text{Power density of wind turbine} \times \text{swept area of rotor} \times \text{turbine efficiency} \times \text{array efficiency}}{\text{land area for one turbine}} \times \text{hours}$$

Solution

annual energy $\text{Y}_{\text{年}} = \text{CF} \times \text{Annual Energy}$

The land area occupied by one turbine is $4D \times 7D = 28D^2$.

$$\text{The rotor area} = \frac{\pi}{4} D^2$$

The yearly energy produced by one turbine =

$$\begin{aligned} &= \text{Wind power density} \times \text{rotor area} \times \text{turbine efficiency} \times \text{array efficiency} \times \text{hours per year} \\ &= 400 \times \frac{\pi}{4} D^2 \times 0.3 \times 0.8 \times 8760 = 660153.6D^2 \\ &\frac{\text{Energy}}{\text{Land Area}} = \frac{660153.6D^2}{28D^2} = 23.58 \text{ kWh/m}^2 \end{aligned}$$

Example

Metric	Value	NEC Rating (kW)	Micon (kW)	Avg. Windspeed (m/s)	kW
1	2.2	0	0	0	0
2	4.5	0	0	0	0
3	6.7	33	33	33	33
4	8.9	56	56	56	56
5	11.2	80	80	80	80
6	13.4	150	150	150	150
7	17.9	248	248	248	248
8	22.3	335	335	335	335
9	24.6	780	780	780	780
10	28.6	1000	1000	1000	1000
11	29.3	924	924	924	924
12	31.3	964	964	964	964
13	33.6	1000	1000	1000	1000
14	35.8	1000	1000	1000	1000
15	37.5	987	987	987	987
16	40.3	987	987	987	987
17	43.2	984	984	984	984
18	44.3	984	984	984	984
19	47.0	917	917	917	917
20	49.2	863	863	863	863
21	51.5	863	863	863	863
22	53.7	822	822	822	822
23	55.9	822	822	822	822
24	58.2	0	0	0	0

CF = 容量系数 $\times 8760$

Solution

Assumption: Rayleigh wind statistics with average wind speed of 7 m/s at hub height.

Step 1: Find the probability of each wind speed. How?

Step 2: Find the energy produced at each wind speed.

Step 3: Annual energy generated = summation of energy produced at each wind speed

Annual Energy Production: Capacity Factor Method

Capacity factor is a measure of the fraction of actual energy delivered to the rated energy output in one year.

$$CF = \frac{\text{Actual energy delivered}}{\text{Rated power} \times 8760}$$

another way to express it is

$$CF = \frac{\text{Actual energy delivered}/8760 \text{ h/yr}}{P_R} = \frac{\text{Average power}}{\text{Rated power}}$$

• Dimensionless quantity between 0 and 1.

• CF is meant for calculating 'actual energy delivered' given that we know the rated power.

CF =

$$0.087 \bar{V} - \frac{P_R(\text{kW})}{[D(\text{m})]^2}$$



CF =

$$\frac{P_{electrical}}{P_{wind}}$$

The overall average efficiency of this turbine

Windspeed (m/s)	Power (kW)	Probability $f(v)$	Hrs/yr at v	Energy (kWh/yr)
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