

# Key derivation

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## Key derivation

### **Cipher algorithms require fixed dimension keys**

- 56, 128, 256... bits

### **We may derive keys from multiple sources**

- Shared secrets
- Passwords generated by humans
- PIN codes and small length secrets

### **Original source may have low entropy**

- Reduces the difficulty of a brute force attack
- Although we must have some strong relation into a useful key

### **Sometimes we need multiple keys from the same material**

- While not allowing to find the material (a password, another key) from the new key

# Key derivation: purposes

## **Key reinforcement: increase the security of a password**

- Usually defined by humans
- Making dictionary attacks impractical

## **Key expansion: increase the dimension of a key**

- Expansion to a size that suits an algorithm
- Eventually derive other related keys for other algorithms (e.g. MAC)

# Key derivation

## **Key derivation requires the existence of:**

- A salt which makes the derivation unique
- A difficult problem
- A chosen level of complexity

## **Computational difficulty**

- Transformation requires relevant computational resources

## **Memory difficulty**

- Transformation requires relevant storage resources
- Limits attacks using dedicated hardware accelerators

# Key derivation: PKBDF2

## Password Based Key Derivation Function 2

**Produces a key from a password, with a chosen difficulty**

**$K = \text{PBKDF2}(\text{PRF}, \text{Salt}, \text{rounds}, \text{dim}, \text{password})$**

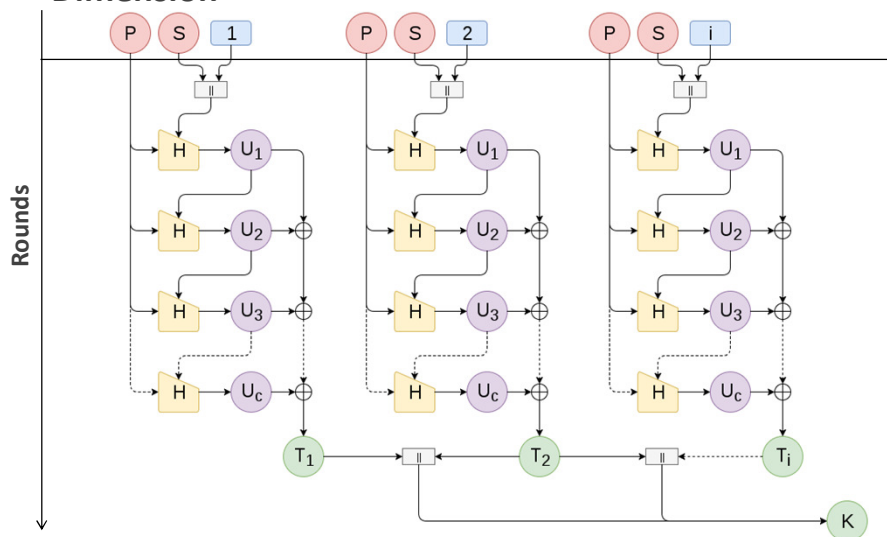
- PRF: Pseudo-Random-Function: a digest function
- Salt: a random value
- Rounds: the computational cost (tens or hundreds of thousands)
- Dim: the size of the result required

**Operation: calculates  $\text{ROUNDS} \times \text{DIM}$  operations from the PRF using the SALT and PASSWORD**

- Larger number of rounds will increase the cost

# Key Derivation: PBKDF2

## Dimension



# Key Derivation: scrypt

Produces a key with a chosen storage cost

**$K = \text{scrypt}(\text{password}, \text{salt}, n, p, \text{dim}, r, \text{hLen}, \text{Mflen})$**

- Password: a secret
- Salt: a random value
- N: the cost parameter
- P: the parallelization parameter.  $p \leq (2^{32} - 1) * \text{hLen} / \text{Mflen}$
- Dim: the size of the result
- R: the size of the blocks to use (default is 8)
- hLen: the size of the digest function (32 for SHA256)
- Mflen: bytes in the internal mix (default is  $8 \times R$ )

# Key Derivation: scrypt

$\text{scrypt}(P, S, N, r, p, \text{dkLen})$

Parameters:  
N (CPU/Memory Cost Parameter)  
r (Block Size)  
p (Parallelization Parameter)  
dkLen (Output Length)

