Topic 7

Memory Management How to gain 30% performance improvement easily

資料結構與程式設計 Data Structure and Programming

Sep, 2010

Outline

- ◆Memory related problems
 - Illegal memory address access
 - Memory leaks
 - Fragmentation
 - Performance issues
- ◆Memory management
 - Basic concept
 - Categorization
 - How to implement

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Memory Related Problems

- 1. Illegal memory address access
- 2. Memory leaks
- 3. Fragmentation
- 4. Performance issues

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Illegal Memory Address Access

- 1. Uninitialized memory read/write
 - Access to the content of a pointer variable that is not yet allocated

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Illegal Memory Address Access 2. Array bound read/write Array index is greater than the bound void f() { size_t size; aaa[size] size = ...; otherVariable int aaa[size]; Stack XXX size_t idx = ...; Heap // error if idx >= size aaa[idx] = ...; Fixed → Compilation OK, but may get strange runtime bug **Data Structure and Programming** Prof. Chung-Yang (Ric) Huang

Illegal Memory Address Access

- Freed memory read/write
 - Access to the just freed memory allocation
 - May still get the expected content, but will become garbage when reallocated by others

```
void f() {
   int* p = new int;
   cout << p << endl;
   delete p;
   // may print out the same address
   cout << p << endl;
   *p = 30; // [NOTE] compilation & runtime OK;
   int j = *p;
   cout << j << endl;
   int* q = new int(20);
   int k = *p;
   cout << k << endl; // What's the value for k?
}</pre>
```

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Illegal Memory Address Access

- 4. Freeing mismatched memory
 - Mixed use of malloc/calloc/free and new/new[]/delete/delete[]

```
int *p = new int(10);
int *q = new int[10];
int **r = new int*;
int **s = new int*[10];
delete p or delete []p?
delete q or delete []q?
delete r or delete []r?
delete s or delete []s?
```

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How to avoid illegal memory access?

- Allocate and free memory of data members in constructor and destructor
 - Use object to wrap the pointer variables

```
class MyClass {
   A* _pp;
public:
   MyClass(int i = 0) { _pp = new A(i); }
   ~MyClass() { delete _pp; }
};
void f() {
   MyClass o; // o._pp is allocated
}// o._pp is deleted automatically
All the operations on _pp should go through class
```

- MyClass

 Can make class A a private class to MyClass (by "friend")
- What about copy constructor or assignment operator?
- Managed (as former as a second) to a confirm the former as
- May need "reference count" to avoid double-free error

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How to avoid illegal memory access?

- 2. Paired memory allocation/deletion functions
 - Don't allow too many functions to allocate and delete pointers

```
//[No good] hard to keep track of the memory allocation of _pp
class MyClass {
   int* _pp;
public:
   void f1(int i) {
      ...; _pp = new int(i); ... }
   void f2() {
      ...; delete _pp; ... }
   void f3() {
      ...; _pp = new int(j);
      ...; delete _pp; ... }
};
```

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How to avoid illegal memory access?

```
Customized array class
```

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```
• Check index whenever access
template <class T>
class MyArray {
    // how many elements in the array
    size_t _size;
    // how much memory is allocated
    size_t _capacity;
    T* _data;
public:
    T& operator [] (size_t i) {
        #ifndef NDEBUG
        if (i >= _size)
            throw ExceptionArraySize(i);
        #endif // NDEBUG
        return _data[i];
    }
};
```

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How to avoid illegal memory access?

- 4. Don't use malloc/calloc/free in C++
 - They won't call the constructors/destructors
 class Temp{
 public:
 string c;
 };
 Temp *test;
 int main()
 {
 test = (Temp*)malloc(sizeof(Temp));
 cout << test->c << endl; // Garbage...
 }</pre>

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How to avoid illegal memory access?

- Correctly use of new/new[] and delete/delete[]
- 6. Memory management

In short, create your own style and strictly abide by your disciplines

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What about the overhead generated by the above preventions?

- Minor overhead is OK; better than debugging tricky memory bugs
- Use "#ifndef NDEBUG" to bypass them in optimized mode compilation
 - "Debug build" --- for developer
 - q++ -q xxx.cpp

"Optimized build" --- for tool release

■ g++ -O3 -DNDEBUG xxx.cpp

==========

#ifndef NDEBUG

<codes for debug mode only>

#endif // NDEBUG

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Memory Related Problems

- 1. Illegal memory address access
- 2. Memory leaks
- 3. Fragmentation
- 4. Performance issues

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What is memory leak?

- ◆Not freeing allocated memory, so as the program runs, the total occupied memory is increasing and cannot be reclaimed
 - → Performance degradation due to thrashing
 - → Program terminated due to memory out

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Why do I have memory leaks?

```
    Pointer data members not freed

            class A { B *_b; ...};
            A a1; ... A a2 = a1; ...

    Local pointers not freed

            A *a; a = new ...;
            if (xxx) { ... return; }
            delete a;

    Freeing memory mismatch

            e.g. p = new MyClass[10]; ...; delete p;

    Overwrite on allocated pointer variables void f() {

                 int* p = new int;
                  p = g();
                  // original p cannot be deleted delete p;
                  }
```

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How do I know if I have memory leak?

- Well, as the program runs longer, the memory usage is increasing and doesn't seem to saturate.
- ◆ To diagnose
 - 1. Code review
 - 2. Using tools
 - Commercial: purify
 - GNU: valgrind (http://valgrind.org/)

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What is fragmentation?

 Like the fragmentation in your hard disk, the memory used in your program may have fragmentation too



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fragmentation too

delete a;

delete b;

What is fragmentation?

◆ Like the fragmentation in your hard disk, the memory used in your program may have

• MyClass12Byte* a = new MyClass12Byte ;

MyClass16Byte* b = new MyClass16Byte;
MyClassWhatever* c = new MyClassWhatever;

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How to avoid memory leaks?

- ◆Good practice makes it all !!
- ◆Memory management
 - Block allocation and deletion
- ◆Use "reference count" to keep track whether it is safe to delete an pointer
 - How??
 - $A^* p = q$;

// Who's ref count is incremented by 1?

• Constructor? Destructor? Object wrapper?

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MyClass16Byte* d = new MyClass16Byte;
MyClass16Byte* e = new MyClass16Byte;

→ Memory fragmentation of 12 Bytes (where??)

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How to avoid memory fragmentation?

- ◆ Memory fragmentation will make your program use more memory than necessary
- ♦ How to fix it?
 - Not easy, unless you use your own memory management and carefully allocate memory pieces with different sizes

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Performance Issues

- Overhead in system calls of memory allocation / deletion
- What's the runtime difference?

```
    int* a[1 << 20];
for (int i = 0; i < (1 << 20); i++) {
        a[i] = new int;
        *(a[i]) = i;
      }
    int* a[1 << 20];
      int* b = (int *)calloc(1 << 20, sizeof(int));
      for (int i = 0; i < (1 << 20); i++) {
        a[i] = b + i;
        *(a[i]) = i;
      }
```

→ But how about "A* a[1 << 20]"? Will A's constructors be called?

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Basic Concepts of Memory Management

- Allocate a big chunk of memory from the system at a time
 - Distribute memory to the pointer variables by the memory manager
- No need to free pointers one by one; free the whole chunk at once
 - Return memory to system when mission is completed
 - → Possibly memory leak-free
 - [Optional] Freed pointer memory is recorded in the recycle list (no deletion); can be used for later memory request

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Issues about Memory Manager

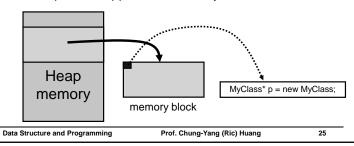
- 1. Number of memory blocks
 - Continuous or non-continuous
- 2. Overload of new/delete operators
 - Use new/delete or customized alloc()/free()
- 3. Memory manager association (by type or id)
- 4. Recycle or not
 - Garbage collection?

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Memory Blocks in Memory Manager

- How many memory should we claim from the system each time (i.e. 1 memory block)?
 - Too small: many system calls
 - Too big: waste of memory if not used up
 - → Depend on applications, usually 4K 1MB



1. Continuous Memory Block

Addresses are continuous; can access by index

- Only 1 memory block
 - When _size >= _capacity, reallocate a bigger block and copy the original data over
 - Difficult to work with pointer variables (why?)

size t numElm(size t t) const {

class MemoryBlock {
 #define S_SIZE_T sizeof(size_t)
public:
 MemoryBlock(size_t B) { // block size = B Bytes
 _begin = _next = (void*)malloc(B);
 _end = _begin + numElm(B);_
 end = _begin + numElm(B);_
}
void* alloc (size_t t) { // t is number of Bytes
 void* tmp = getNext(t);
 if (tmp >= _end) { /* allocate new memory and copy to it */ }
 void* ret = _next; _next = tmp;
 return ret;
}
private:
void * _begin, *_next, *_end;
void* _getNext(size_t t) const {
 size_t nt = numElm(t); return (size_t*)_next + nt; }

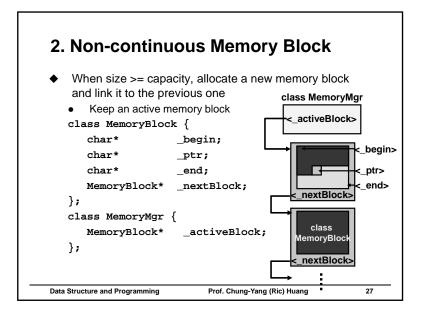
return (t + S_SIZE_T - 1) / S_SIZE_T; }

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};

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Overload of new/delete operators

- ♦ We can overload the new and delete operators of a class
 - void* operator new (size_t t);
 - void* operator new[] (size_t t);
 - void operator delete (void* p);
 - void operator delete[] (void* p);

(Can also be static functions)

[Note] The parameters 't' and 'p' are passed in by compiler with the "new/delete" calls

- Advantage
 - Memory manager is transparent to the programmer; can turn on and off easily
- For more information, please see (for example)
 - http://www.relisoft.com/book/tech/9new.html

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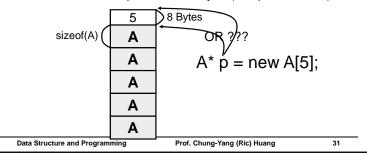
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```
Example: newOp.cpp
class A
                                               static void* operator new[](size t t) {
                                                cout << "new[] (inside A): " << endl;
 int
                                                 cout << ">> size = " << t << endl:
         _a;
 int
        _b;
                                                 A^* p = (A^*) malloc(t);
                                                 cout << ">> ptr = " << p << endl;
 int
        _c;
 short d;
                                                 return p;
 // sizeof(A) = 14 \rightarrow 16 Bytes
                                               static void operator delete(void* p) {
public:
                                                 cout << "delete (inside A): " << endl;
 A() {}
                                                 cout << ">> ptr = " << p << endl;
 ~A() {}
                                                 free(p);
 static void* operator new(size_t t) {
                                               static void operator delete[](void* p) {
   cout << "new (inside A): " << endl;
                                                cout << "delete[] (inside A): " << endl;
   cout << ">> size = " << t << endl:
                                                 cout << ">> ptr = " << p << endl;
   A^* p = (A^*) malloc(t):
                                                free(p);
   cout << ">> ptr = " << p << endl;
   return p:
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```

Example: newOp.cpp ===== Sample output ====== int main() new (inside A): >> size = 16 A^* a = new A; >> ptr = 0x502010cout << endl: cout << "new (in main): " << endl: new (in main): cout << ">> ptr = " << a << endl; >> ptr = 0x502010cout << endl; new[] (inside A): $A^* b = \text{new A}[10];$ >> size = 168 cout << endl; >> ptr = 0x502030cout << "new[] (in main): " << endl; cout << ">> ptr = " << b << endl; new[] (in main): cout << endl: >> ptr = 0x502038delete a: delete (inside A): cout << endl: >> ptr = 0x502010delete []b; cout << endl; delete[] (inside A): >> ptr = 0x502030Data Structure and Programming Prof. Chung-Yang (Ric) Huang 30

What did "newOp.cpp" tell you?

- Must have destructor... somehow....
 - Try comment out the destructor in newOp.cpp...
- 2. Size of "new[]" = array size + 8 // for 64-bit platform
 - How do we record the array size for delete?
 - → i.e. delete [] p; // what's the size?
- 3. Size of class A is promote to 16 Bytes (multiple of SIZE_T)



What did "newOp.cpp" tell you?

- Must have destructor... somehow....
 - Try comment out the constructor in newOp.cpp...
- 2. Size of "new[]" = array size + 8 // for 64-bit platform
- 3. Size of class A is promote to 16 Bytes (multiple of SIZE T)
- 4. The ptr in new[] () points to the "-8" address
- 5. The ptr in new[] caller points to the array begin
- 6. The ptr in delete[] () points to the "-8" address
- 7. The ptr in delete[] caller points to the array begin
- → In this example, memory is explicitly allocated by "malloc()" (or new char[numBytes])
 - (Will the constructor and destructor be called?)
- → What if we want to use a memory manager (for chunk alloc and delete)?
 - (Who returns the pointers of new and delete?)
- → Can the "new()", "delete()" be non-static member functions?

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Closer look at "new A" and "delete A"

- ♠ A *a = new A:
 - 1. A::operator new() is called
 - 2. Constructor of A is called
 - 3. The return pointer address is copied to 'a'
- ♠ A *a = new A[10];
 - Similar to "A *a = new A" except that 10 constructors are called
- delete a;
 - Destructor of A is called
 - 2. A::operator delete() is called
- ◆ delete []a;
 - Similar to "delete a" except that several destructors are called

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8/4-Byte Aligned

- ◆ In the previous example, the size of data members in A is 4 + 4 + 4 + 2 = 14. However...
 - sizeof(A) = 16
 - The parameters to new() and new[10] are 16 and 168
- ◆ But, if the class A is changed to:

```
class A {
   char _data[14];
};
```

- sizeof(A) = 14
- The parameters to new() and new[10] are 14 and 148
- → NOT 8-Byte aligned!!

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Issues about Memory Manager

- 1. Number of memory blocks
 - Continuous or non-continuous
- 2. Overload of new/delete operators
 - Use new/delete or customized alloc()/free()
- 3. Memory manager association (by type or id)
- 4. Recycle or not
 - Garbage collection?

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Memory Manager Association

Which memory manager to call when you allocate a memory in new/delete operator?

```
(i.e. instead of calling "malloc()" and "free()" directly...)
```

```
→ void* new(size_t t) {
```

```
... memMgr->alloc(t); ...}
```

→ void operator delete (void* p) { ... memMgr->free((T*)p);

Is "memMgr" a data member?

Is "memMgr" a global variable?

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1. Declared as "static" Data Member

```
class MyClass {
    static MemoryMgr *const _mem_s;
public:
    void* operator new(size_t t) {
        _mem_s->alloc(t); }
};
```

- → Each class is associated with an unique memory manager
- → What if new/delete operators are not overloaded?
- → What if we want to associate more than 1 memory managers for a class? (i.e. 1 class → n memMgr)
 - [Reason] Can have options to free portion of the memory
 - Swap with other memory manager (bookkeeping needed)
 - Who control this??

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2. Use a Global Map(class id, MemManager);

```
class MyClass {
    static int const _mem_id_s;
public:
    void* operator new(size_t t) {
        ::globalMemMap[mem_id_s]
        ->alloc(t);
    }
};
```

→ Memory manager association is controlled by a global function/class

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HW#4 Implementation of class MemMgr

```
template <class T>
                                    template <class T>
class MemMgr {
                                    class MemRecycleList {
private:
                                    friend class MemMgr<T>;
 size t
                   blockSize:
                                     // the array size of the recycled data
 MemBlock<T>*
                   activeBlock;
                                      size t arrSize;
 MemRecycleList<T>
                                      // the first recycled data
             recycleList[R_SIZE];
                                                first:
                                      // next MemRecycleList
                                          with _arrSize + n*R_SIZE
template <class T>
                                      MemRecycleList<T>* _nextList;
class MemBlock {
 friend class MemMgr<T>;
 char*
                   _begin;
 char*
                   _ptr;
 char*
                  _end;
 MemBlock<T>*
                   nextBlock:
```

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Using Memory Management

```
◆ Given a class "A" to be managed by class "MemMgr"
        // overload its new/new[]/delete/delete[] operators
        void* operator new(size_t t) {
              return (void*)(_memMgr->alloc(t)); }
        void* operator new[](size t t);
        void operator delete(void* p);
        void operator delete[](void* p);
        static void memReset(size_t b = 0);
        static void memPrint():
        // Declare _memMgr as a static data member
        static MemMgr* const _memMgr;
    class MemMgr {
        // Implement "alloc", "allocArr", "free", "freeArr", "print"
          functions
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```

Memory Manager Association

- ♦ We know...
 - Static data member must be initialized in .cpp code
 - e.g. MemoryMgr *const A::_mem_s = new ...
- ◆Can we associate the memory managers of 2 different classes to the same one?

(i.e. n classes → 1 memMgr)

- i.e. Share the same memory manager
- Any problem? (Answered later)

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Do you remember.... mem manager is

- Allocate a big chunk of memory from the system at a time
 - Distribute memory to the pointer variables by the memory manager
- No need to free pointers one by one; free the whole chunk at once
 - Return memory to system when mission is completed
 - → Possibly memory leak-free
 - [Optional] Freed pointer memory is recorded in the recycle list (no deletion); can be used for later memory request

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Why do we need to overload "delete"?

What does it do?

Can we NOT overload "delete"? (If so, will the destructor be called?)

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Recycling Memory

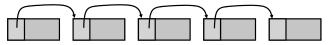
 Freed pointer memory is recorded in the recycle list (no deletion); can be used for later memory request

How?? Use a "linked list" container class? (No!! extra memory)

- In the memory manager, keep a recycleList that points to the first recycled memory
- Reuse the first 4 or 8 Bytes (why?) of each recycled memory, pointing to the address of the next recycled memory

[Restriction]

The size of the managed class should be >= 4 (or 8) Bytes



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In other words...

```
class MemoryMgr {
   RecycleList _rList;
public:
   void* alloc(size_t t) {
      void* p = _rList.popFront();
      if (P != 0) return p;
      ... // get memory from memory manager
   }
   void delete(void* p) {_rList.pushFront(p); }
};
class MemRecycleList {
   size_t _arrSize; // the array size of the recycle data
   T* _first; // the first recycled data
   MemRecycleList<T>* _nextList;
};
   Any problem?
```

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Recycling List Implementation

- ◆ [Note] Memory in recycling list is NOT continuous
- ♦ Should the size of the recycled elements in _rList be the same? (3) \rightarrow (1) \rightarrow (5) \rightarrow (1)...
- ♦ If same size → Simple implementation
 - void* _first; // "void* _last" is optional
 - All the elements in the list have the same size (e.g. = sizeof(A))
 - But how do we recycle "a = new A[n]"?
 - Just implement pushFront() and popFront()
 - Don't need to pass in "size_t t" for popFront()
- ♦ If not, how do you find the one you want?
 - For example, "a = new A[n]"?

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Recycling List with Different Mem Sizes

- Using linked list?
 - Finding the element of size S is O(n)
- ◆ Using map<size, linked list>?
 - Uh... extra memory
 - O(log(m)) time in "find()"
 - Using array<size, linked list>?
 - What are the indices? Dynamic or static?
 - 1. { 0, 1, 2, 3, 4, 5, 6, ..., n,... }
 - 2. { 0, 1, 2, 4, 8, 16, 32, 64,..., 2ⁿ,... }
 - 3. $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 16, 32, \dots, 2^n, \dots\}$
 - Decomposed? (e.g. 13 = 8 + 4 + 1)
- Any hybrid idea?

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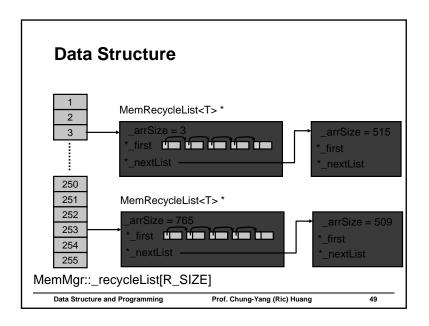
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Recycling List Implementation in HW#4

- ◆Observation
 - Most of the arrays are of small sizes
 - → RecycleList[0] ~ RecycleList[255] for new, new [1], new [2],..., new [255]
- ♦ What about new [n], $n \ge 256$?
 - → Use m = n % 256

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Source Code class RecycleList { // Go through this and nextList, find out a recycle list whose "_arrSize" == "n" MemRecycleList<T>* getList(size_t n) { // Find the recycle list whose _arrSize == n **}**; class MemMgr { size_t getRecycleIdx(size_t t) const{ // t Bytes to recycle assert(t >= S); // S: size of the recycled class element return (t-SIZE_T)/S;// subtract the size for storing 'n' MemRecycleList<T>* getMemRecycleList(size_t n) { size t m = n % R SIZE; return _recycleList(m).getList(n); **}**; [e.g.] delete p; // let t = the #Bytes to recycle → getMemRecycleList(getMemRecycleList(t)).push_front(p); Data Structure and Programming Prof. Chung-Yang (Ric) Huang

Recycling List with Different Classes

- ◆ What if we want to associate the same memory manager to different classes?
 (i.e. n classes → 1 memMgr)
 (e.g. class Inheritance?)
 - What would be the mem size in the recycling list? GCD of sizes of A & B? Multiple of sizeof(size_t)?
 - → More difficult to manage...!!
 - → Suggest to use memory management without recycling

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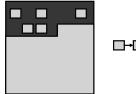
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Memory Management without Recycling

```
♦ Overload "new" to get memory from memMgr
♦ Overload "delete" to do nothing but calling destructor
    → No recycle
class MemoryBlock {
   char*
                  begin;
   char*
                  _ptr;
   char*
                  _end;
   MemoryBlock* _nextBlock;
   MemoryBlock(size_t B) { _begin = (char*)malloc(B); }
class MemoryMgr {
   MemoryBLock* activeBlock;
   void* alloc(size_t) {
      // get memory from _activeBlock;
      // If over the limit, new MemoryBlock as activeBlock }
};
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```

Garbage Collection

 After using memory management for a while, we may have many recycled memory pieces but not much required memory





Memory block

- ◆ Can we rearrange the pointers so that the freed memory can be put together and even returned to system earlier?
 - Pointer value changes? How to keep the associations?
 - Index or pointer?
 - Too many to cover; beyond the scope of this class...

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Conclusion

- ◆ Memory related problems are mostly runtime problems
 - You won't see them during compilation
 - Crash during runtime → difficult to debug
 - But please use debugger instead of "cout"
- Use memory manager to allocate a block of memory instead of piece by piece
 - Don't need to worry about freeing individual memory >
 no memory leak
 - Still need to properly issue "delete" if the callings of destructors are needed
 - Can achieve better memory locality and thus better performance

Data Structure and Programming

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