

Sistemas digitais

19/09/2018 - T

→ Álgebra de Boole

variável lógica $A \rightarrow \{0, 1\}$

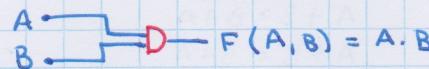
$$A \rightarrow \square \rightarrow F(A)$$

i) Negação ou inversão

$$A \rightarrow \text{---} F(A) = \bar{A}$$

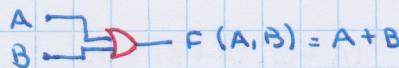
A	\bar{A}
0	1
1	0

ii) Interseção ou produto lógico



A	B	$A \cdot B$
0	0	0
0	1	0
1	0	0
1	1	1

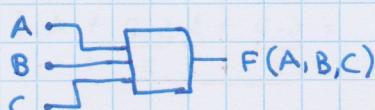
iii) Reunião ou soma lógica



A	B	$A + B$
0	0	0
0	1	1
1	0	1
1	1	1

Exemplo

Entradas



$$F(A, B, C) = \bar{A} \cdot B + C$$



Postulados

P1 $x = 0$ $x = 1$

P2 $0 \cdot 0 = 0$ $1 \cdot 1 = 1$

P3 $0 \cdot 1 = 1 \cdot 0 = 0$ $0 + 1 = 1 + 0 = 1$

P4 $1 + 1 = 1$ $0 + 1 = 0$

P5 $\bar{0} = 1$ $\bar{1} = 0$

Teoremas

T1 $A \cdot 0 = 0$ $A + 1 = 1$

T2 $A \cdot 1 = A$ $A + 0 = A$

T3 $A \cdot A = A$ $A + A = A$

T4 $A \cdot \bar{A} = 0$ $A + \bar{A} = 1$

T5 $\bar{\bar{A}} = A$

T6 $A \cdot B = B \cdot A$ $A + B = B + A$

T7 $A \cdot B \cdot C = A \cdot (B \cdot C) = (A \cdot B) \cdot C$ $A + B + C = A + (B + C) = (A + B) + C$

T8 $A \cdot (B + C) = A \cdot B + A \cdot C$ $A + B \cdot C = (A + B) \cdot (A + C)$

T9 $\overline{A \cdot B} = \bar{A} + \bar{B}$ $\overline{A + B} = \bar{A} \cdot \bar{B}$

T10 $A + A \cdot B = A$ $A \cdot (A + B) = A$

T11 $A + \bar{A} \cdot B = A + B$ $A \cdot (\bar{A} + B) = A \cdot B$

T12 $A \cdot B + A \cdot \bar{B} = A$ $(A + B) \cdot (A + \bar{B}) = A$

T13 $A \cdot B + \bar{A} \cdot C + B \cdot C = A \cdot B + \bar{A} \cdot C$ $(A + B) \cdot (\bar{A} + C) \cdot (B + C) = (A + B) \cdot (\bar{A} + C)$

Simplificação de expressões pelos teoremas

T1 $A \cdot 0 = 0 \Rightarrow \begin{cases} 0 \cdot 0 = 0 \\ 1 \cdot 0 = 0 \end{cases}$

T10 $A + AB = A$
 $\underline{x + xy = x}$

$$\begin{aligned}
 F(A, B, C) &= C \cdot D + A \cdot \bar{B} \cdot \bar{C} + B \cdot C \cdot D \\
 &= \underbrace{C \cdot D}_{x} + \underbrace{B \cdot C \cdot D}_{y} + \underbrace{A \cdot \bar{B} \cdot \bar{C}}_{x} + \dots \\
 &= \textcolor{red}{C \cdot D} + A \cdot \bar{B} \cdot \bar{C}
 \end{aligned}$$

T6
 T10