CDSF04, CDSF05, CDSF06

# Recap

**DS Academy** 













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4		

<u>Files</u>

pd.read\_csv(), pd.read\_json(), pd.read\_pickle(), ...

DB's and DW's

pd.read\_sql(), pd.read\_gbq(), ...

**Python Objects** 

pd.DataFrame.from\_dict(), pd.DataFrame.from\_records()

#### **Indexing**

Integer, Range, Slice

df[start:end:step], df.iloc[], df.loc[]

List

df[[1,2,4,5]], s.reindex([1,2,3])

**Boolean Array** 

df[(df['col\_a']=='foo') & df['col\_b']=='bar')]

#### **Transform**

Groupby

df.groupby('col').sum(), .apply(), .agg(), .transform(), ...

Pivot, Stack, Unstack

df.pivot(), df.stack(), df.unstack()

#### Merge

Merge

df1.merge(df2, left\_on='pk', right\_on='fk', how='left')

**Join** 

df1.join(df2, how='inner')

Concat

pd.concat([df1, df2, df3])











pandas.pydata.org/pandas-docs/stable/user\_quide

#### **Table Of Contents**

What's New in 0.25.0

Installation

Getting started

User Guide

- IO tools (text, CSV, HDF5, ...)
- Indexing and selecting data
- Multilndex / advanced indexing
- Merge, join, and concatenate
- Reshaping and pivot tables
- Working with text data
- Working with missing data
- Categorical data
- Nullable integer data type
- Visualization
- Computational tools
- Group By: split-apply-combine
- Time series / date functionality
- Time deltas
- Styling
- Options and settings
- Enhancing performance
- Sparse data structures
- Frequently Asked Questions (FAQ)
- Cookbook

Pandas ecosystem

API reference

Development

Release Notes









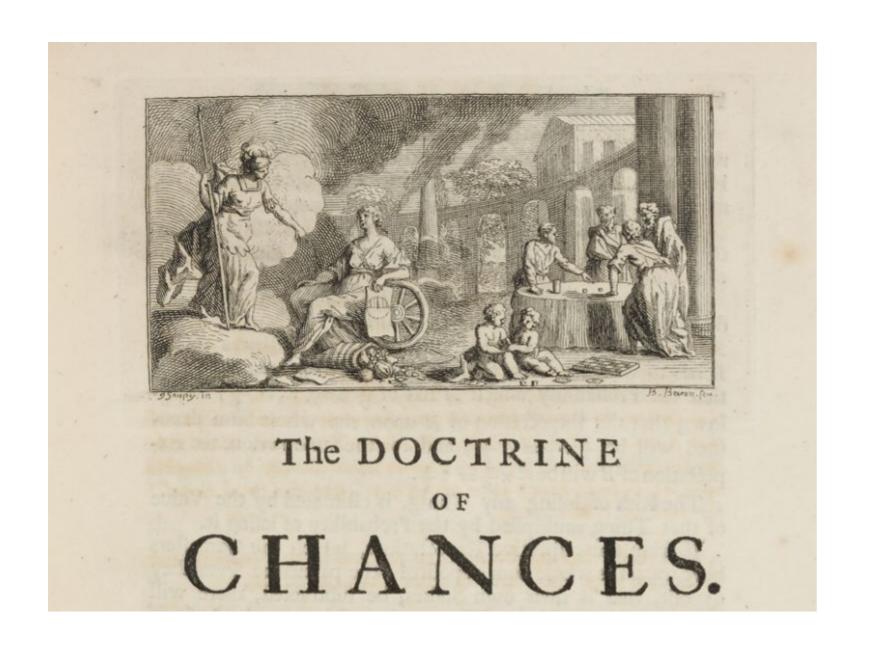


## Agenda

- What is probability?
- Multiplication rule
- Independence
- Addition rule
- Mutually Exclusive
- PDF and CDF
- Mean, Median and Mode
- Standard error
- Variance
- The law of large numbers
- The Central Limit Theorem



#### What is Probability?







The frequency theory was originally designed to solve gambling problems



ELANO



## LIKELIHOOD

0 1



ELANO

MANDALAY BAY

# P(event) =

# OCCURRENCES EVENT

# ALL POSSIBLE OUTCOMES



PELANO

MANDALAY BAY





## P(throw=6) =





## P(throw not 6) =

56

= 1 - P(throw = 6)





The chance that **both** two things will happen

The chance that the **first** thing will happen

The chance the **second** will happen

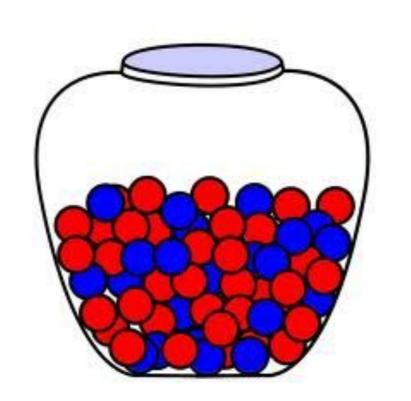
\*



Two things are **independent** if the chances for the second, given the first are the <u>same</u>, no matter how the first one turns out. Otherwise, the two things are **dependent**.

WITH REPLACEMENT

INDEPENDENT



WITHOUT REPLACEMENT

DEPENDENT

#### **INDEPENDENDT**

**DEPENDENT** 

The chance that **both** two things will happen

The chance that the **first** thing will happen

The chance the **second** will happen



## What is P(BBB)?

## WITH REPLACEMENT

**INDEPENDENT** 

30/55 \* 30/55 \* 30/55

## WITHOUT REPLACEMENT

**DEPENDENT** 

30/55 \* 29/54 \* 28/53

**30** BLUES **25** RED





#### What is P(BRR)?

## WITH REPLACEMENT

WITHOUT REPLACEMENT

**INDEPENDENT** 

**DEPENDENT** 

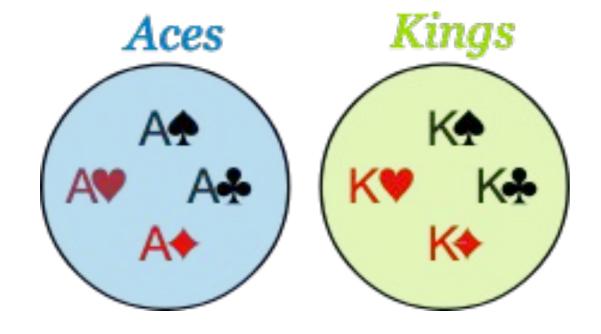
30/55 \* 25/55 \* 25/55

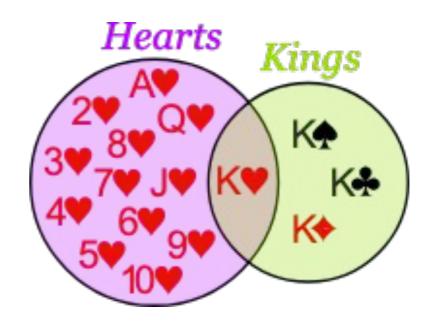
30/55 \* 25/54 \* 24/53

**30** BLUES **25** RED



Two things are mutually exclusive if the occurrence of one prevents the occurrence of the other.





#### **MUTUALLY EXCLUSIVE**

$$P(A \text{ or } B) = P(A) + P(B)$$

#### NOT MUTUALLY EXCLUSIVE

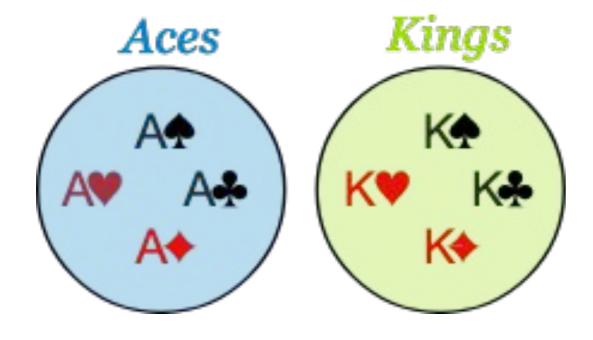
$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

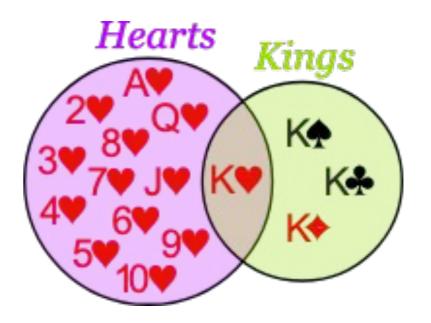


P(Aces or Kings) =

$$4/52 + 4/52 = 8/52$$

$$4/52 + 13/52 - 1/52 = 16/52$$







$$P(A \mid B) = \frac{P(A \cap B)}{P(B)}$$

$$P(B \mid A) = \frac{P(A \cap B)}{P(A)}$$



$$P(A \mid B) = \frac{P(A \mid B)}{P(B)}$$

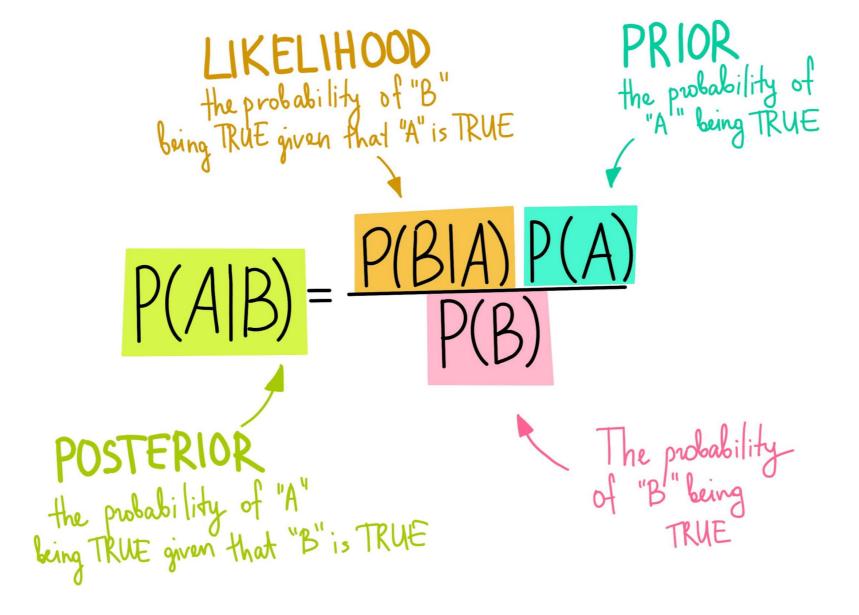
$$P(B \mid A) = \frac{P(A \mid B)}{P(A)}$$



$$P(A \mid B) = \frac{P(A \cap B)}{P(B)}$$

$$P(A) P(B | A) = P(A \cap B)$$

#### **Conditional Probability and Bayes Theorem**







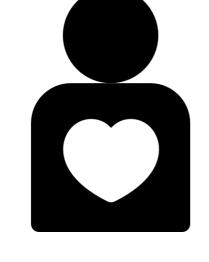


99

+

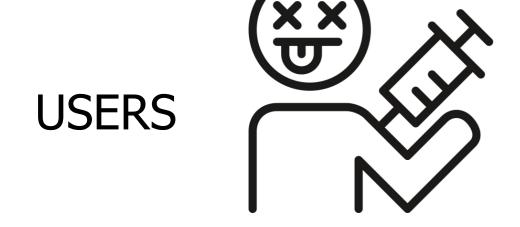
•

NON USERS



99.5%

 $P(User \mid +) = P(+|User)P(User)$  P(+)



0.5%

P(+) = P(+|User)P(User) + P(+|NotUser)P(NotUser)

$$P(+) = .99*.005 + .01*.995$$

$$P(+) = 0.0149$$





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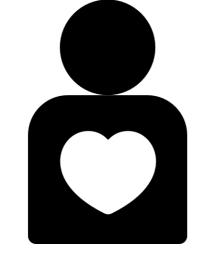
99

1

1

99





**Example Bayes Theorem - Drug Testing** 

99.5%

$$P(User \mid +) = P(+|User)P(User)$$

$$P(+)$$



0.5%

$$P(User | +) = \frac{.99 * .005}{0.0149}$$

NON

**USERS** 



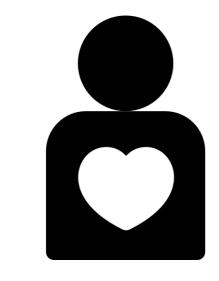


99

1

1

99



99.5%

$$P(User \mid +) = P(+|User)P(User)$$

$$P(+)$$

0.5%

$$P(User | +) = \sim$$

33.2%

### Summary

Event	Probability		
Α	$P(A) \in [0,1]$		
not A	$P(A^{\complement}) = 1 - P(A)$		
A or B	$P(A \cup B) = P(A) + P(B) - P(A \cap B)$ $P(A \cup B) = P(A) + P(B)$ if A and B are mutually exclusive		
A and B	$P(A \cap B) = P(A B)P(B) = P(B A)P(A)$ $P(A \cap B) = P(A)P(B)$ if A and B are independent		
A given B	$P(A \mid B) = \frac{P(A \cap B)}{P(B)} = \frac{P(B A)P(A)}{P(B)}$		

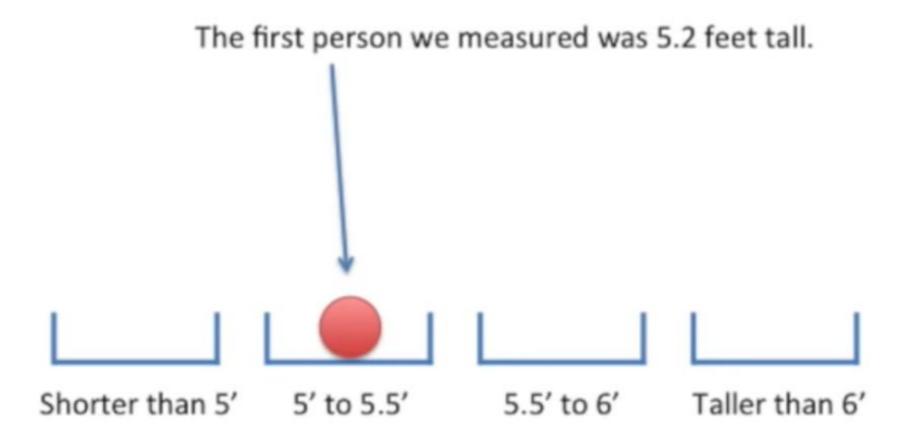




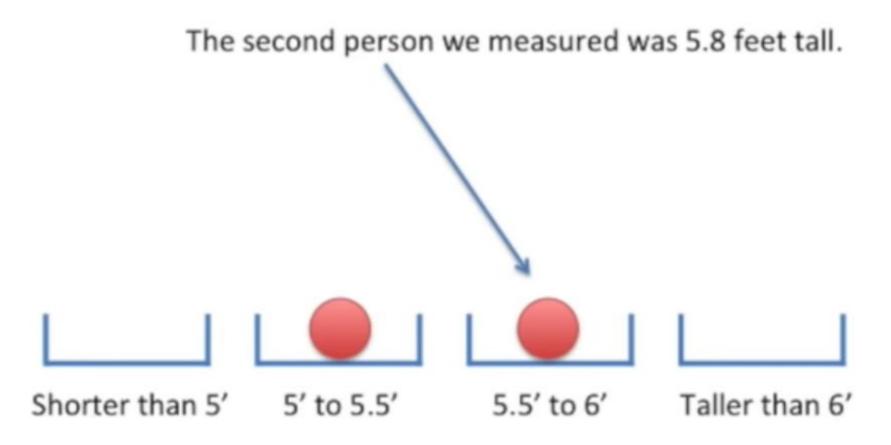
Imagine we measured the height of a lot of people.



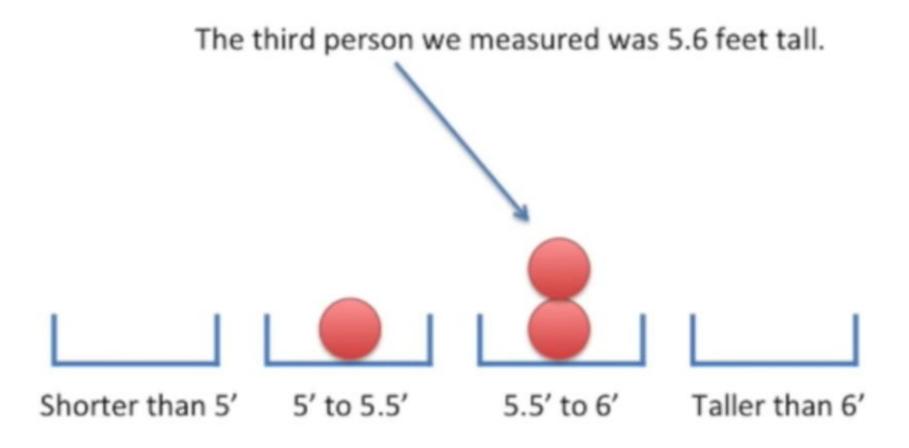
### **PDF and Distributions**



### **PDF and Distributions**

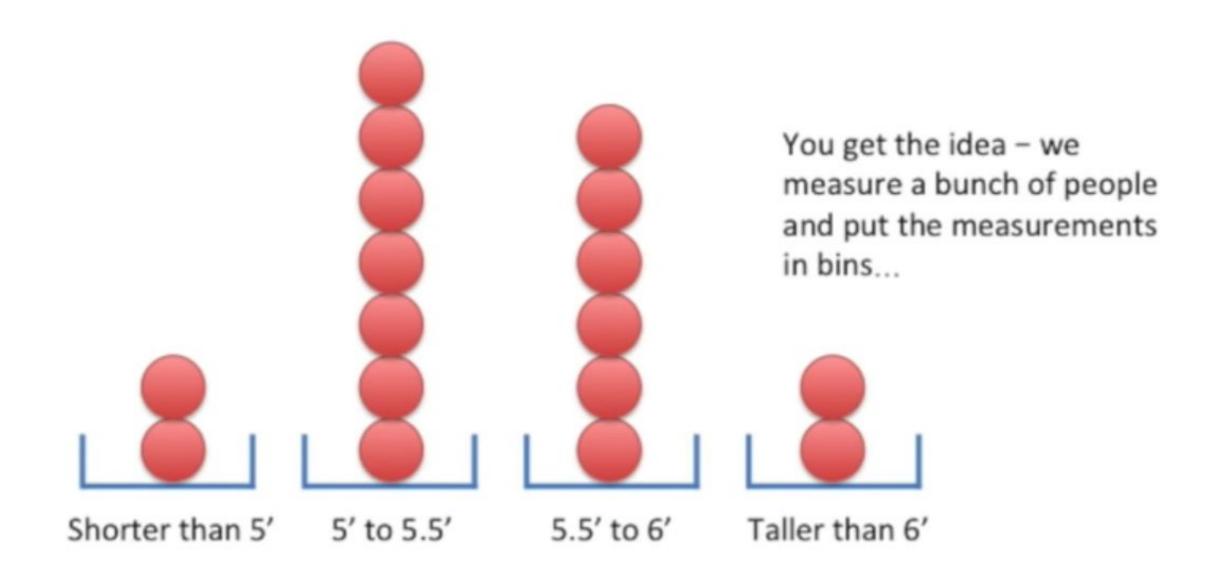


#### **PDF and Distributions**



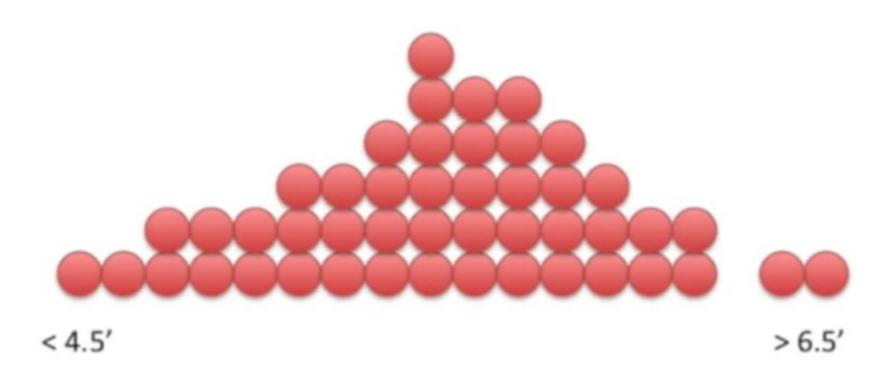








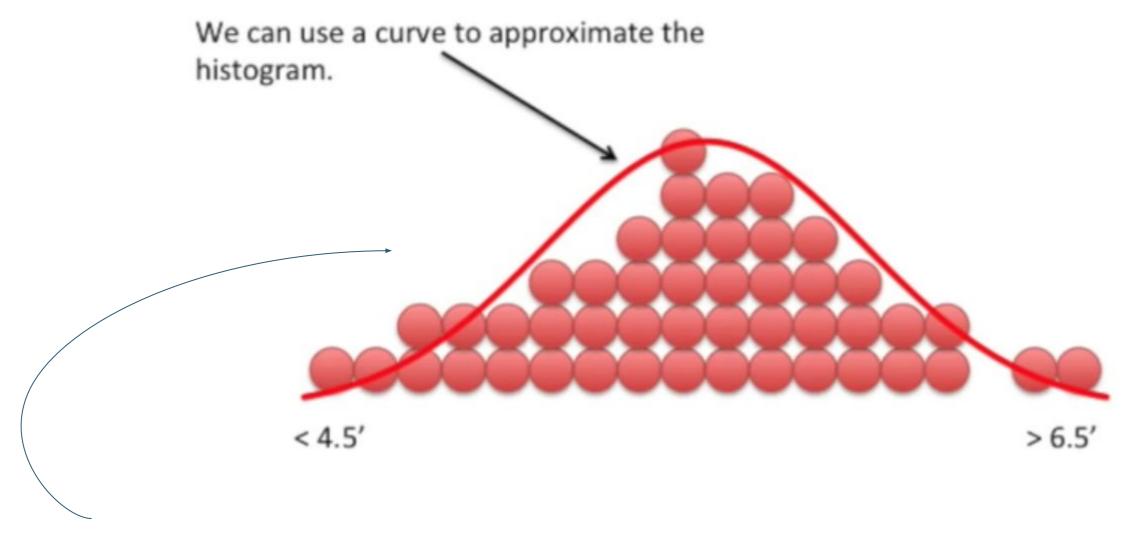




By measuring more people and using smaller bins, we get a more accurate and more precise estimate of how heights are distributed.

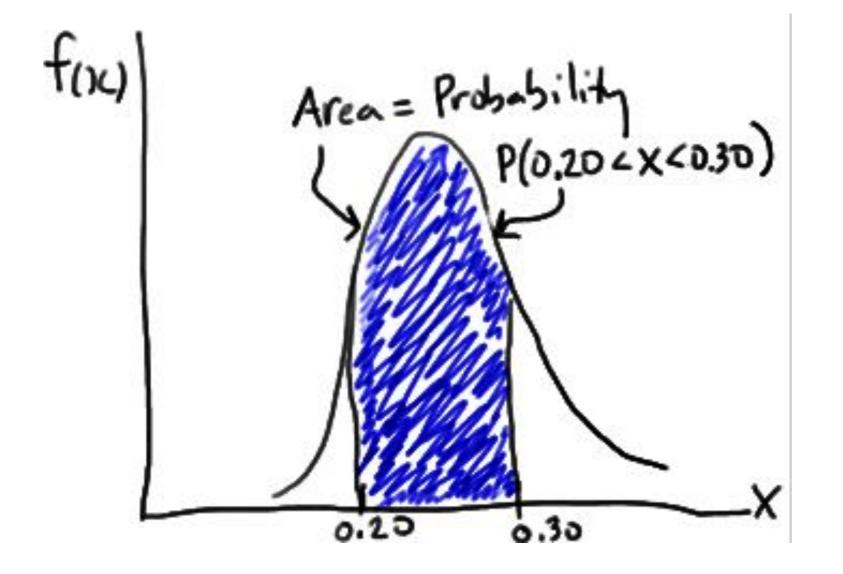


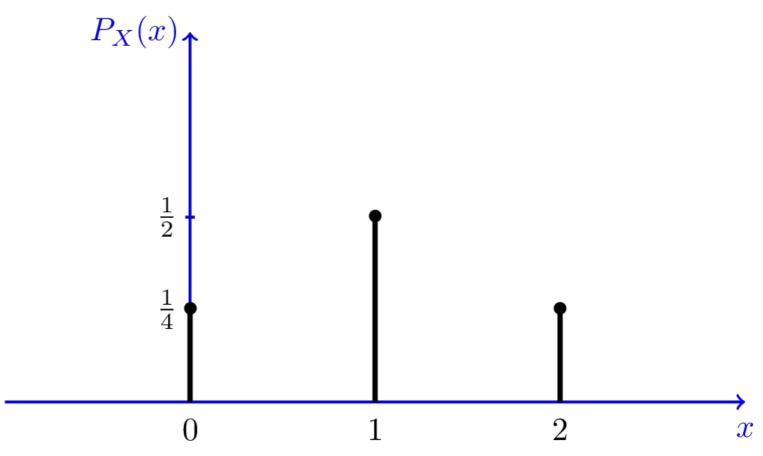




It is a function!

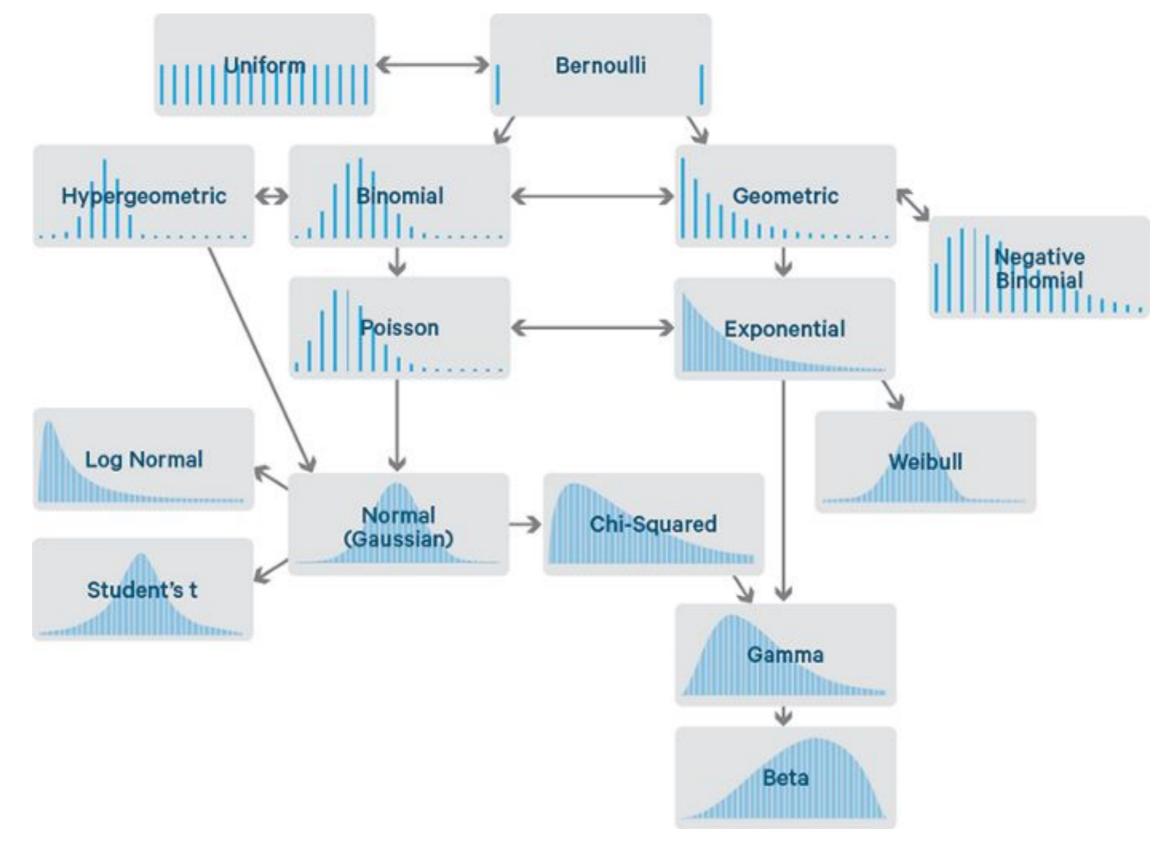






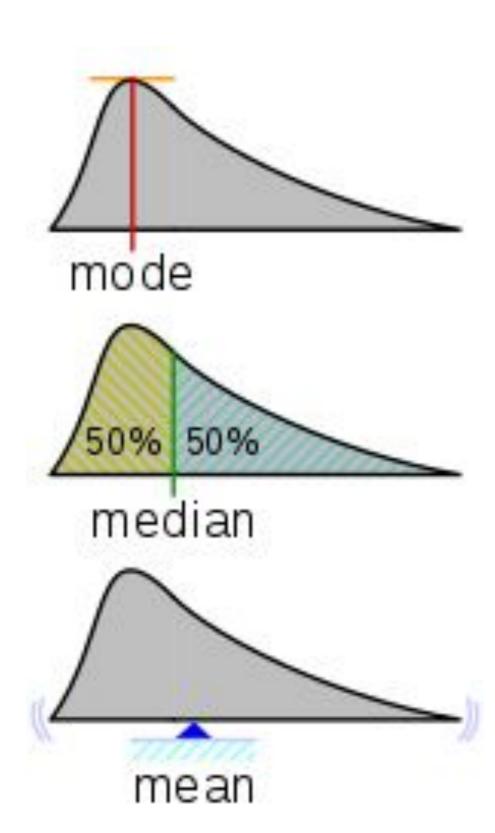


### **Distributions**

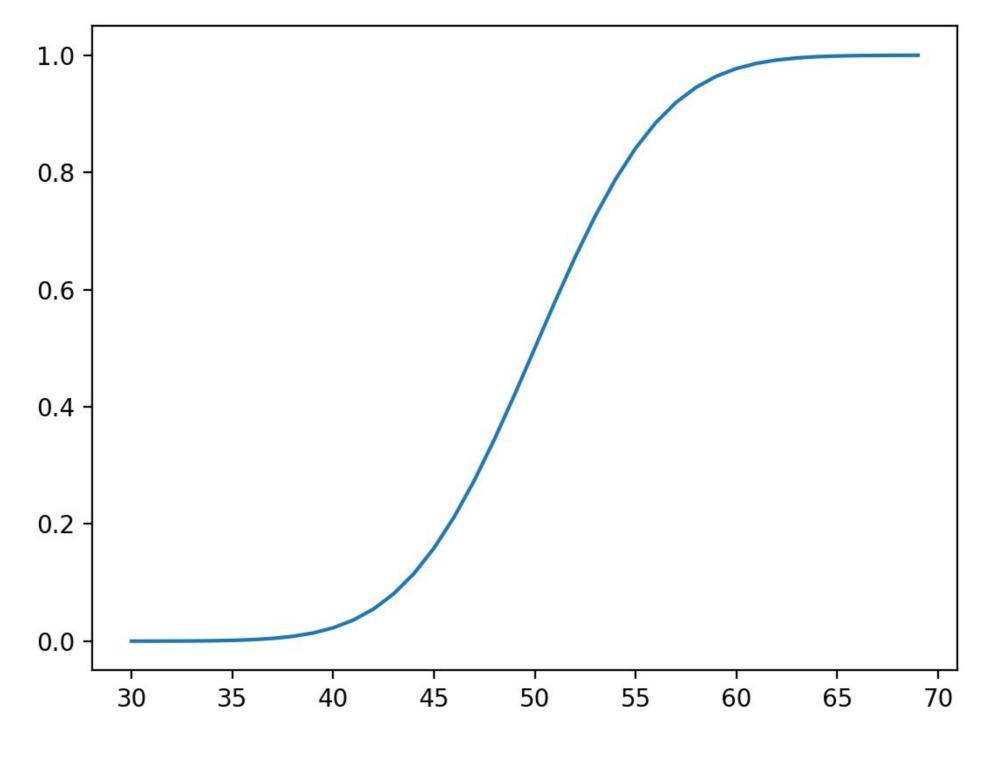




### **PDF and Descriptive Parameters**









## **STANDARD DEVIATION**

$$\sigma = \sqrt{\frac{\sum (X - \overline{X})^2}{n - 1}}$$

**VARIANCE** 

$$\sigma^2 = \frac{\sum (\chi - \mu)^2}{N}$$

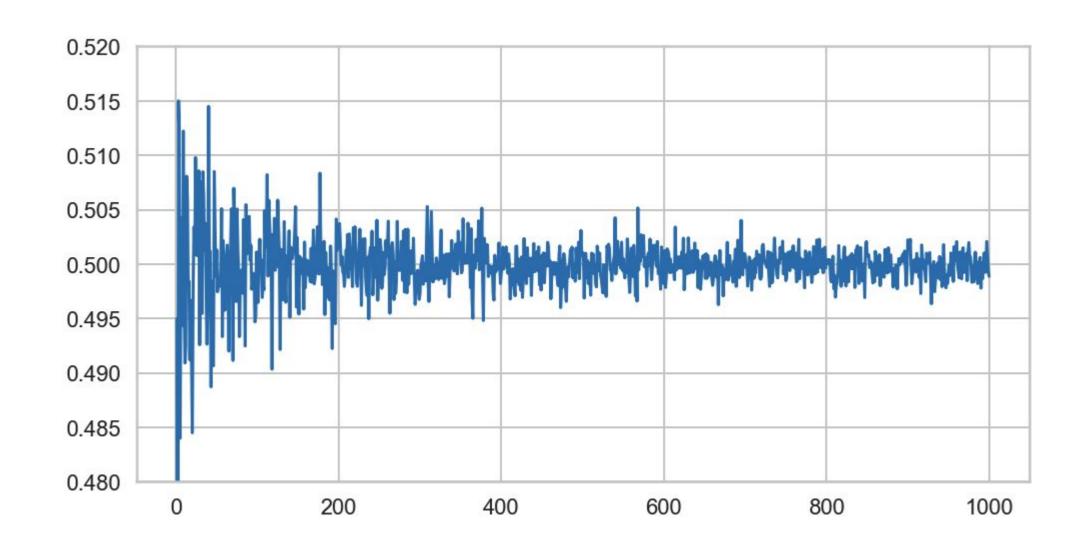




$$SE = \frac{\sigma}{\sqrt{n}}$$
 Standard deviation Number of samples

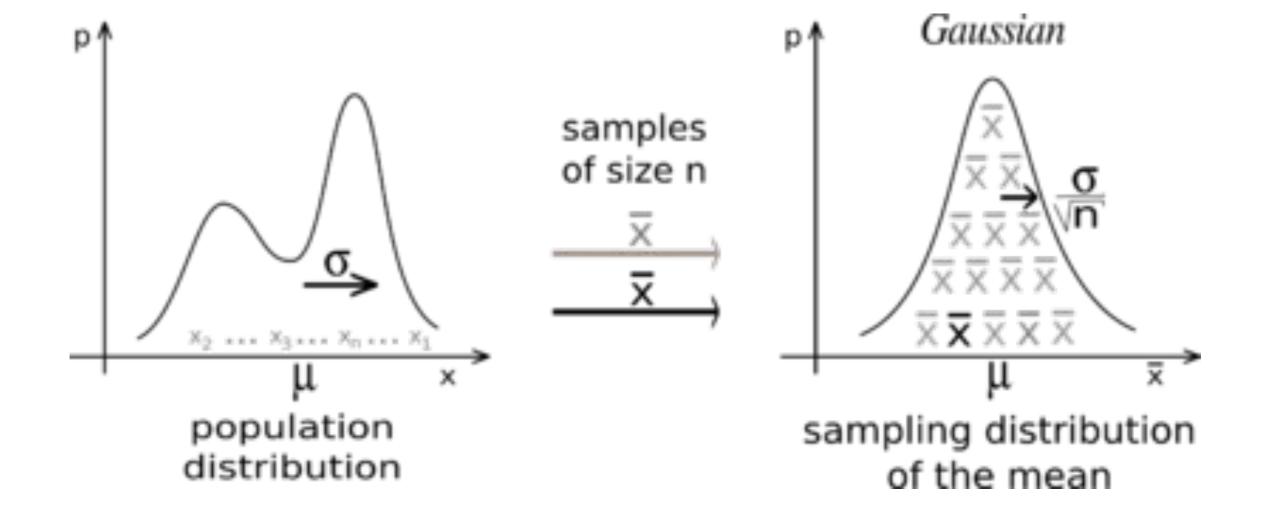


# The Law of Large Numbers





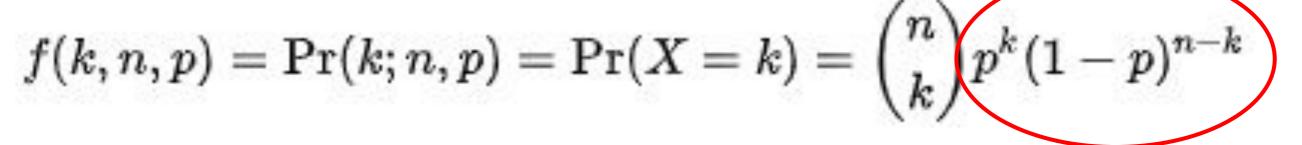






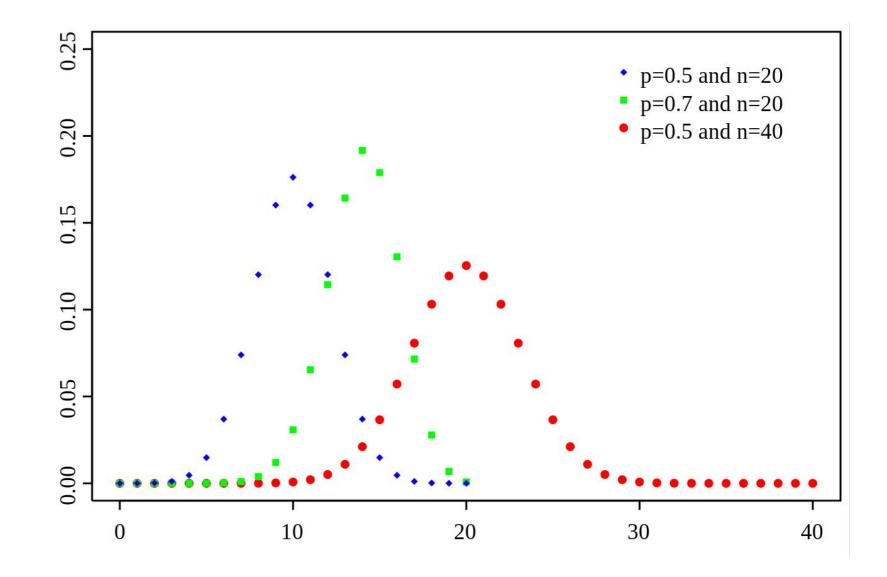




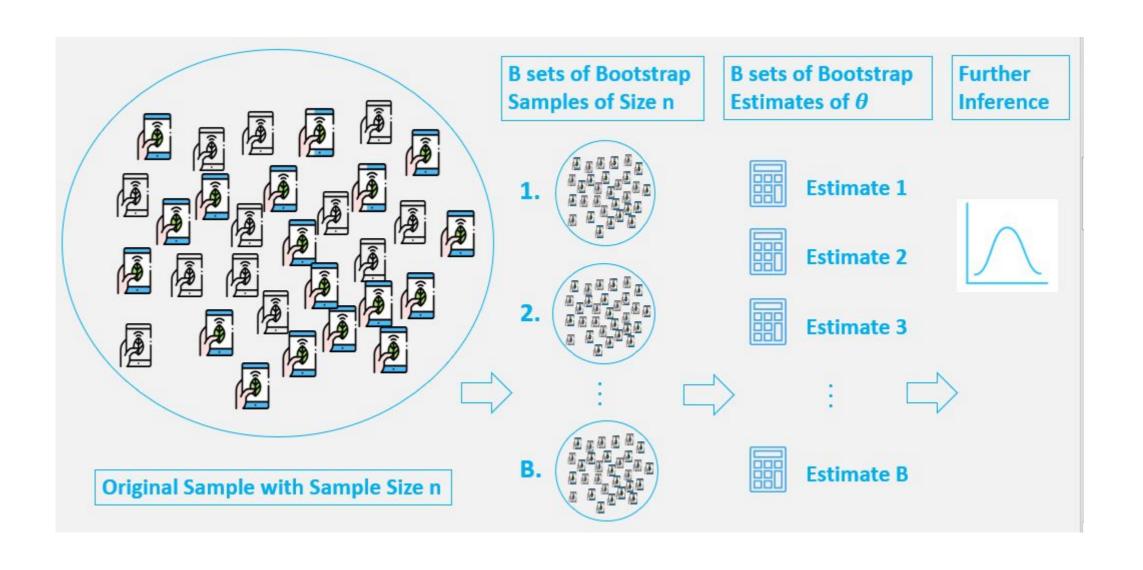


for k = 0, 1, 2, ..., n, where

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$



### **Bootstrapping**



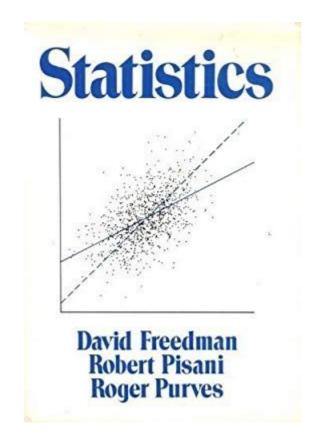








Stat Quest



## THANK YOU



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