Algorithm Complexity II

Sorting Algorithms

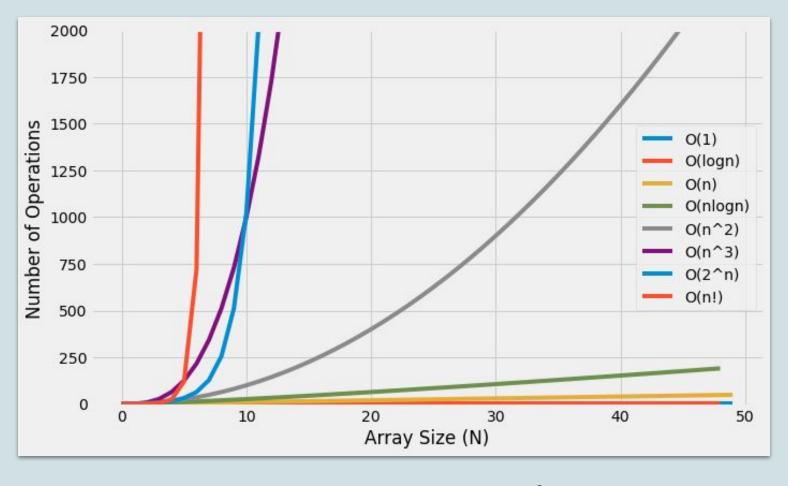
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 $O(1) < O(logn) < O(n) < O(nlogn) < O(n^2) < O(2^n) < O(n!)$

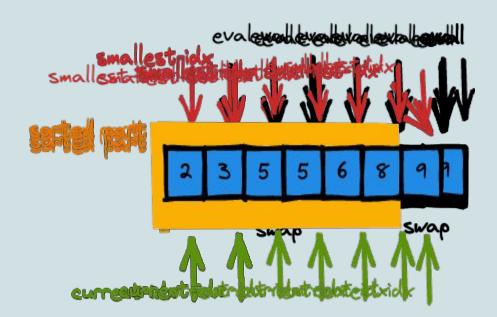
Sorting Algorithm	Time Complexity			Space Complexity		
	Best Case	Average Case	Worst Case	Worst Case		
Insertion sort	0(n)	0(n^2)	0(n^2)	0(1)		
Bubble sort	0(n)	0(n^2)	0(n^2)	0(1)		
Selection sort	0(n^2)	0(n^2)	0(n^2)	0(1)		
Merge sort	O(nlogn)	O(nlogn)	O(nlogn)	0(n)		
Heapsort	O(nlogn)	O(nlogn)	O(nlogn)	0(1)		
Quicksort	O(nlogn)	O(nlogn)	0(n^2)	O(logn)		
Counting sort	0(n+k)	0(n+k)	0(n+k)	0(n+k)		
Radix sort	0(d(n+b))	0(d(n+b))	0(d(n+b))	0(n+b)		
Bucket sort	0(n+k)	0(n+k)	0(n^2)	0(n+k)		
Shell sort	O(nlogn)	O(nlogn)^2	O(nlogn)^2	0(1)		

Sorting Algorithm	Comparison Based	Stable	Recursive	In-place	Adaptive	Online
Insertion sort	√	✓	X	✓	√	√
Bubble sort	\checkmark	\checkmark	X	\checkmark	✓	X
Selection sort	\checkmark	X	×	1	X	×
Merge sort	\checkmark	\checkmark	\checkmark	X	×	X
Heapsort	√	×	X	\checkmark	×	×
Quicksort	\checkmark	X	\checkmark	\checkmark	×	X
Counting sort	X	√	×	×	X	X
Radix sort	×	✓	X	×	×	×
Bucket sort	X	√	X	×	×	×
Shell sort	✓	×	X	\checkmark	\checkmark	X

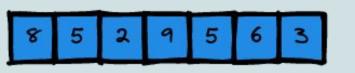
Selection Sort



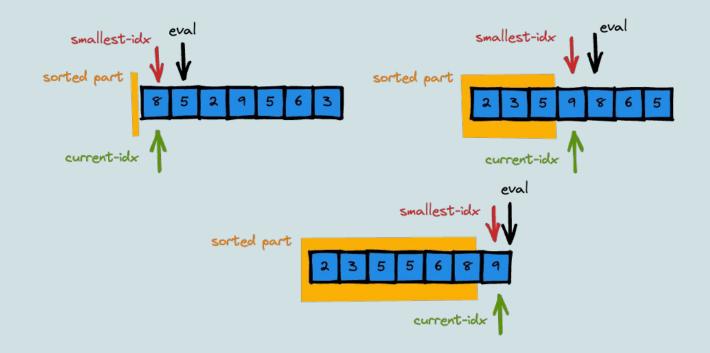
sorted part unsorted part swap



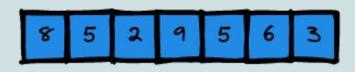
Selection Sort

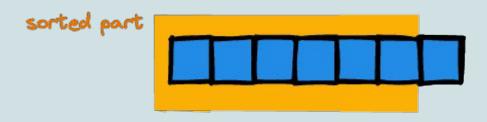


sorted part unsorted part swap



Selection Sort Calc of complexity





$$egin{aligned} T(n) &= N \ T(n) &= N + (N-1) \ T(n) &= N + (N-1) + \ldots + 1 \ S_n &= rac{N(N+1)}{2} \ O(N^2) \end{aligned}$$

```
1:def selectionSort(array):
      currentIdx = 0
      while currentIdx < len(array) - 1:</pre>
          smallestIdx = currentIdx
          for i in range(currentIdx + 1, len(array)):
              if array[smallestIdx] > array[i]:
                  smallestIdx = i
          swap(currentIdx, smallestIdx, array)
          currentIdx += 1
10:
    return array
12:def swap(i, j, array):
       array[i], array[j] = array[j], array[i]
```