

Sábado Letivo

01) Calcular o volume da função $V: \pi \int_1^2 (x)^4 \cdot dx$

$$V: \pi \int_1^2 (x)^4 \cdot dx \rightarrow$$

$$\pi \int_1^2 \frac{x^5}{5} = \left[\frac{x^5}{5} \right]_1^2 \rightarrow$$

$$V: \pi \cdot \left[\frac{2^5}{5} - \frac{(1)^5}{5} \right]$$

$$V: \pi \cdot \left[\frac{32}{5} - \frac{1}{5} \right] \quad V: \frac{31\pi}{5} \quad \boxed{V: 19,47}$$

02) Calcular o volume gerado pela função $V: \pi \int_0^1 (y^{5/3})^2 \cdot dy$

$$V: \pi \int_0^1 (y)^{2/3} \cdot dy$$

$$V: \pi \int_0^1 \frac{y^{5/3}}{5/3}$$

$$V: \pi \left[\frac{y^{5/3}}{5/3} \right] \quad V: \pi \cdot \frac{3}{5} \left[y^{5/3} \right]_0^1$$

$$V = \frac{3\pi}{5} \left[\sqrt[3]{1^5} \right] - [0]$$

$$V = \frac{3\pi}{5} [1] = V = \frac{3\pi}{5} \mu V = \boxed{1,884 \mu V}$$

03) Calcule o volume gerado pela função

$$V = \pi \int_0^1 (x^2 + 2)^2 - \left(\frac{x}{2} + 1 \right)^2 dx$$

$$V = \pi \int_0^1 (x^4 + 4x^2 + 4) - \left(\frac{x^2}{4} + x + 1 \right) dx$$

$$V = \pi \int_0^1 \left(x^4 + 4x^2 - \frac{x^2}{4} - x + 4 - 1 \right) dx$$

$$V = \pi \int_0^1 \left(x^4 + \frac{15x^2}{4} - x + 3 \right) dx$$

$$V = \pi \int_0^1 \left(\frac{x^5}{5} + \frac{15}{4} \cdot \frac{x^3}{3} - \frac{x^2}{2} + 3x \right)$$

$$V = \pi \left[\frac{1^5}{5} + \frac{15}{4} \cdot \frac{1^3}{3} - \frac{1^2}{2} + 3 \cdot 1 \right] - [0]^0$$

$$V = \pi \left[\frac{1}{5} + \frac{5}{4} + \frac{1}{2} + 3 \right] \rightarrow V = \pi \left[\frac{29}{20} \right] = \boxed{12,40 \mu V}$$