

ASSIGNMENT 5 RAFAEL VILLASMIL

PROBLEM 14.8

$$f(x,y) = -8x + x^2 + 12y + 4y^2 - 2xy$$

DO ONE ITERATION OF OPTIMAL GRADIENT
STARTING AT $x=0$ $y=0$

$$\frac{\partial f}{\partial x} = -8 + 2x - 2y = -8 + 2(0) - 2(0) = \boxed{-8}$$

$$\frac{\partial f}{\partial y} = 12 + 8y - 2x = 12 + 8(0) - 2(0) = \boxed{12}$$

$$H_x = 0 - 8h = -8h$$

$$H_y = 0 + 12h = 12h$$

$$f(x,y) = -8(-8h) + (-8h)^2 + 12(12h) + 4(12h)^2 - 2(-8h)(12h)$$

$$f(x,y) = 64h + 64h^2 + 144h + 576h^2 - 192h^2$$

$$f(x,y) = 208h + 448h^2 = g(h) \Rightarrow$$

$$-g'(h) = 208 + 896h$$

$$\textcircled{a} g'(h) = 0 = 208 + 896h \Rightarrow h = 0.2321$$

$$\boxed{\begin{array}{l} x = 0 - 8(0.2321) = -1.857 \\ y = 0 + 12(0.2321) = 2.7857 \end{array}}$$

$$f(x,y) \text{ MINIMUM} = (-1.857, 2.786)$$

$$\text{CHECK } f(0,0) = 0$$

$$f(-1.857, 2.786) = -3.44$$

ASSIGNMENT 5 PART 2

PROVE THE EXPRESSION FOR 2nd ORDER DERIVATIVE

$$\frac{\partial^2 f}{\partial x \partial y} ?$$

$$\frac{\partial^2 f}{\partial x \partial y} = \frac{\partial^2 f}{\partial y \partial x}$$

$$f(x, y) = -8x + x^2 + 12y + 4y^2 - 2xy \Rightarrow$$

$$\frac{f'_{x,y}}{dx} = -8 + 2x - 2y \Rightarrow \left| \frac{f'_{(x,y)}}{dy} = 12 + 8y - 2x \Rightarrow \right.$$

$$\frac{f''_{x,y}}{dx dy} = -2$$

$$\frac{f''_{(x,y)}}{dy dx} = -2$$

$$\boxed{\frac{f''_{xy}}{dx dy} = -2 = \frac{f''_{xy}}{dy dx}}$$