Daily Coding Problem #121

Problem

This problem was asked by Google.

Given a string which we can delete at most k, return whether you can make a palindrome.

For example, given 'waterrfetawx' and a k of 2, you could delete f and x to get 'waterretaw'.

Solution

Notice the recursive structure of this problem:

- If the string is already a palindrome, then we can just return true.
- If the string is not already a palindrome, then try getting rid of the first or last character that does not contribute to its palindromicity.

For example, say we're looking at the example string waterrfetawx. Since the string is not already a palindrome, we'll try removing the first character or the last character. We'll take the happy path and remove the last character, leaving us with waterrfetaw. We can remove wate off both ends, leaving us with rrf. Then we try removing the first and last character again, and we find that we can remove two characters (x and f) to get a palindrome.

This leads itself to the following code:

```
def k_palindrome(s, k):
    # If s is already a palindrome, return true
    if len(s) <= 1:</pre>
```

```
return True

# Get rid of matching ends
while s[0] == s[-1]:
    s = s[1:-1]
    if len(s) <= 1:
        return True

if k == 0:
    return False

# Try getting rid of the first and last character to see if we
# can make a palindrome by removing k - 1 chars.
return k_palindrome(s[:-1], k - 1) or k_palindrome(s[1:], k - 1)</pre>
```

This takes $O(2^{\min(n, k)})$ time, where n is the length of the original string. This is because we call k_palindrome twice on each subproblem, and on each call, either k or the string gets reduced by at least 1.

We can do this faster, though. If we can find the longest palindromic subsequence of a string, then we can reduce this problem to finding it by checking the difference in string lengths. If it's greater than k, we return false, otherwise true.

```
def k_palindrome(s, k):
    return len(s) - longest_palindromic_subsequence(s) < k</pre>
```

How do we find the longest palindromic subsequence, though? We can use dynamic programming to do this in $O(n^2)$ time:

A[i][j] = max(A[i + 1][j], A[i][j - 1])

return A[0][n - 1]

We define an N by N table A, and A[i][j] will represent the length of the longest palindromic substring starting at i and ending at j. The relationship is as follows:

- If i == j:1
- If s[i] == s[j]: take the longest palindromic subsequence from s[i + 1] to j[i 1] and add two (since we have two more characters at the ends)
- Else (s[i] != s[j]): take the maximum of the longest palindromic subsequences of ranges
 i + 1 to j, or i to j 1.

Thus we are building the palindrome from the inside out by trying to match all characters at the ends, ignoring characters that don't help. This will take $O(N^2)$ time and space.

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