

CSE-221
Assignment 1+2

Answer to the Question.1

1. In this example the edge is going from node A to node B and it is a directed graph therefore A is adjacent to B but B is not adjacent to A because we can not go to A from node B.



2. If there is n amount of vertices we can create n_2 or $\frac{n(n-1)}{2}$ number of edges in an undirected graph without creating allowing loops and multiple edges between pairs.

3. In case of directed graph :- ~~$n(n-1)$~~ $n(n-1)$.

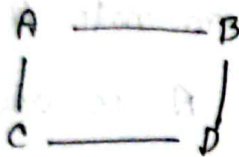
4. We can construct $(n-1)$ edges.

5. For directed graph we can construct $(n-1)$ edges avoiding cycle.

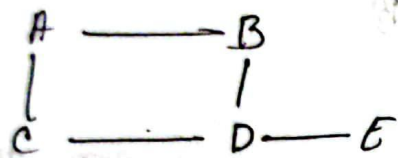
6. The property is Eulerian ~~property~~ Path. Where every edge is visited exactly once.

7. The property is Hamiltonian path where every node is visited exactly once and some edges may remain unvisited.

Eulerian:-

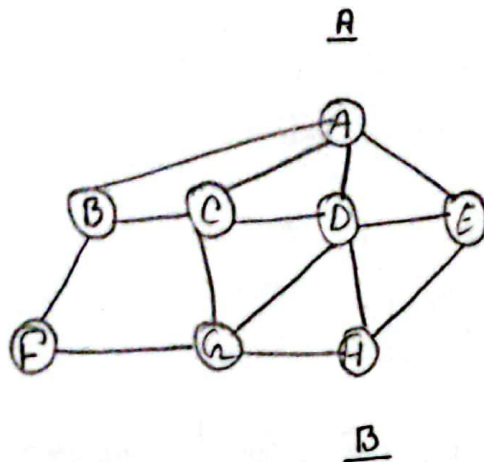


Hamiltonian:-



8) Adjacency list is usually more space efficient compared to adjacency matrix. For example adjacency matrix uses $O(V^2)$ space of undirected and sparse graph while adjacency list uses $O(V+E)$ space for those graph. Similarly in weighted, unweighted, Dense, graph adjacency list uses less memory compared to adjacency matrix.

Answer to the Question. 2



Adjacency list:-

- | | | |
|---|---|---------------------|
| 0 | A | → B → C → D → E |
| 1 | B | → A → C → F |
| 2 | C | → A → B → D → G |
| 3 | D | → A → C → E → G → H |
| 4 | E | → A → D → H |
| 5 | F | → B → G |
| 6 | G | → C → D → F → H |
| 7 | H | → D → E → G |

Adjacency Matrix:-

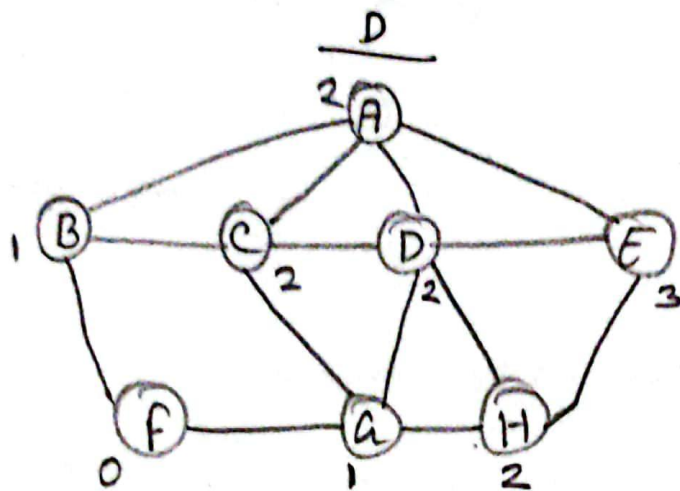
	A	B	C	D	E	F	G	H
A	0	1	1	1	1	0	0	0
B	1	0	1	0	0	1	0	0
C	1	1	0	1	0	0	1	0
D	1	0	1	0	1	0	1	1
E	1	0	0	1	0	0	0	1
F	0	1	0	0	0	0	1	0
G	0	0	1	1	0	1	0	1
H	0	0	0	1	1	0	1	0

C

AB - 1
AC - 2
AD - 2
AE - 1
AF - 1
AG - 2
AH - 2
BC - 1
BD - 2
BE - 1
BF - 0

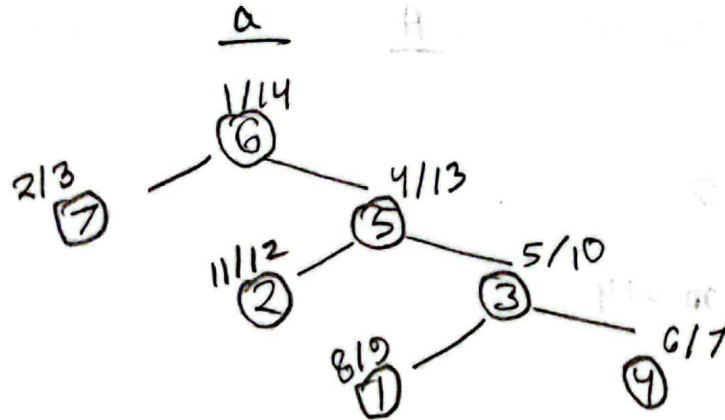
BA - 2
BH - 0
CD - 2
CE - 2
CF - 2
CA - 1
CH - 2
DE - 2
DF - 1
DA - 2
DH - 2

EF - 0
EG - 2
EH - 1
FG - 0
FH - 1
GH - 1



Here if consider F as the root & E is 3 degree connection away from it therefore F will not be able to see E's posts.

Answer to the Question. 3



b

Nodes	1	2	3	4	5	6	7
Parent	3	5	5	3	6	-1	6
Starting time	8	11	5	6	4	1	2
Finish time	9	12	10	7	13	14	3
Distance from Root	3	2	2	3	1	0	1

Answer to the Question. 4

A

Here,

$$\text{Vertex} = 9$$

$$\text{edge, } m = 14$$

Now,

degree of,

$$\begin{array}{l|l} A = 3 & E = 3 \\ B = 4 & F = 3 \\ C = 4 & G = 4 \\ \hline D = 3 & H = 2 \\ & I = 2 \end{array}$$

$$\therefore \text{Total Degree} = (3+4+4+3+3+3+4+2+2)$$

$$= 28$$

$$\therefore \sum \text{deg} = 28 = 2 \times m \quad | \quad m = 14$$

[Proved]

B

Maximum of edges possible in ^{this} undirected graph = $\frac{n(n-1)}{2}$

$$= \frac{9(9-1)}{2}$$
$$= \frac{72}{2}$$

$$= 36$$

∴ We can add more (36-14) edges

= 22 edges.

Answer to the Question. 5

A

DFS (socks)



DFS (Nagna)



DFS (Watch)



DFS (Engagement ring)



DFS (Glasses)

~~DFS~~

DFS (turban)



DFS (broach)

DFS (Undengarmdet)

DFS (Padama)

DFS (shenwani)

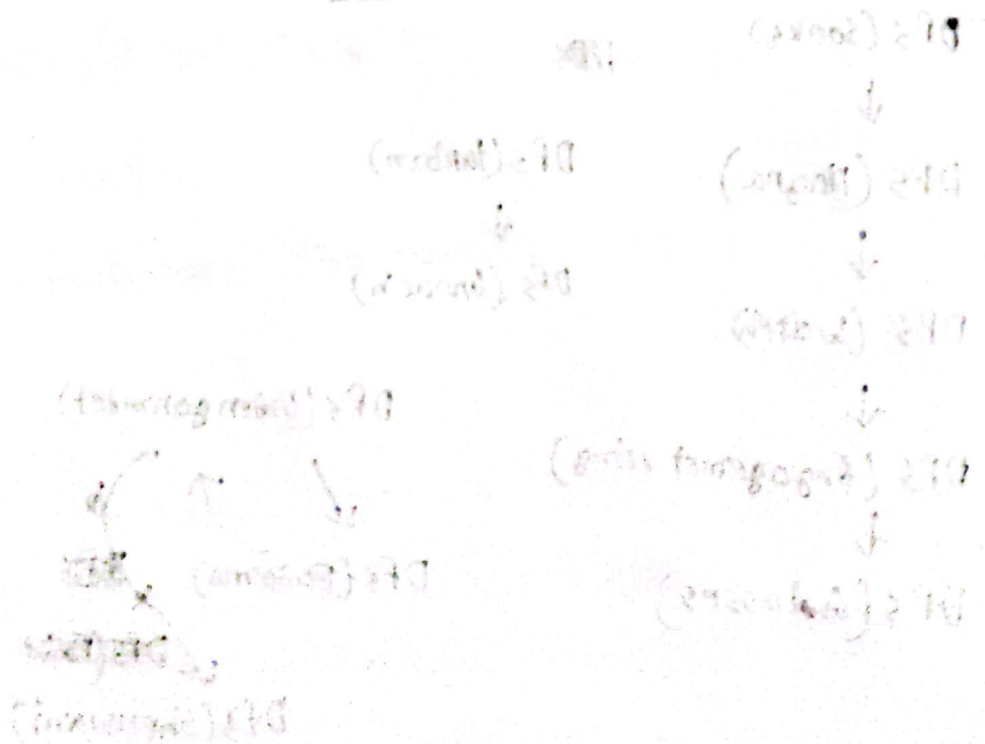
Undengarmdet
shenwani
Padama
turban
broach
Socks
Nagna
Watch
Engagement ring
Glasses

His dressing order should be:-

Undergarments → shenwani → Palamas → tanban → broach → socks →
→ Nagna → watch → Engagement ring → Glasses.

D

No all of my classmates will not have the same ordering because we can all start from different point but the every object will come after some specific objects. For example Nagna will always come after socks event if the start from any other point.

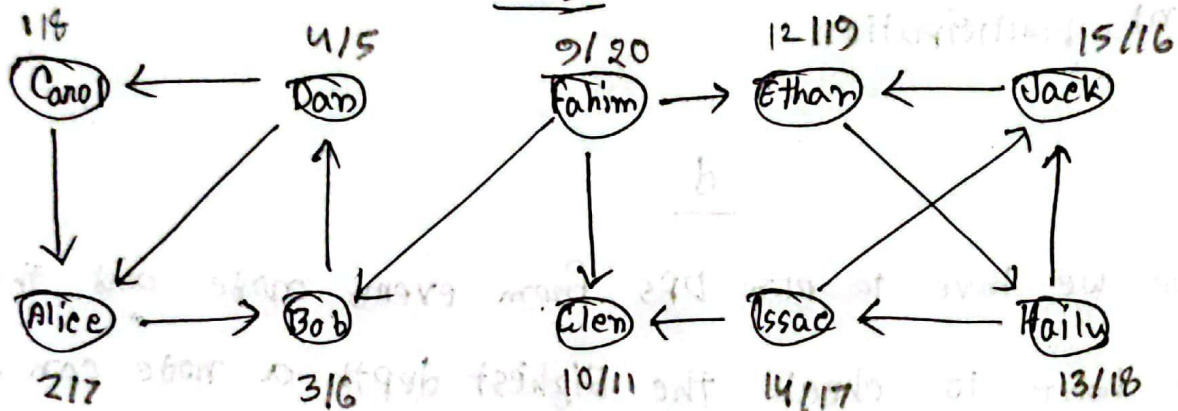


Answer to the Question. 6

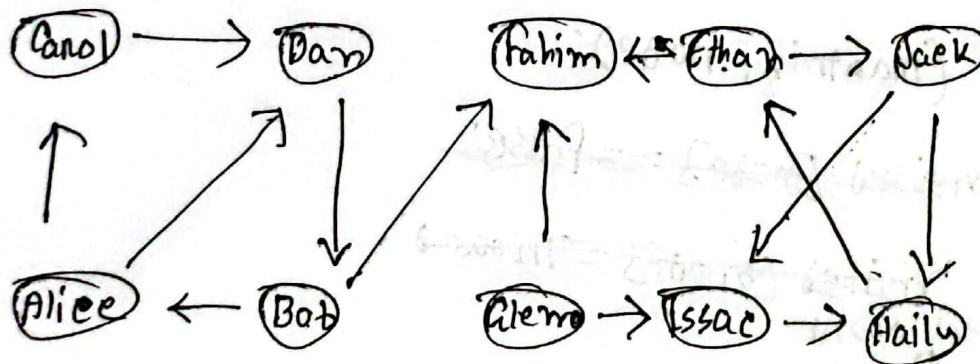
a

The algorithm tailored for this situation is kasaraju algorithm.

a b



Reverse:-



Fahim
Ethan
Haily
Issac
Jack
Glen
Carol
Alice
Bob
Dan
stack

Group 1: ~~Fahim~~

Group 2: ~~Ethan, Jack~~ Haily, Issac, Jack, Ethan

Group 3: ~~Glen~~

Group 4: Alice, Bob, Dan, Carol

∴ 2 groups can be formed.

c
Fakim and ~~Alan~~ Glen will be ineligible for ~~town~~ tournament participation.

d

Here we have to run DFS from every node and then we have to check the highest depth a node can reach.

count = 0

for ~~node~~ i in nodes:
temp = DFS(~~node~~)

def DFS (matrix, node):

~~visited [node] = false~~

~~visited [node] = true~~

global count

for child in matrix [node]:

if visited [child] == false:

visited [child] = true

DFS (matrix, child)

count++

return count, DFS (matrix, child)

```
max = 0  
name = ""  
for i in nodes:
```

```
temp =
```

```
    global count
```

```
    count = 0
```

```
    temp = DFS(rooti)
```

```
    if count > max:
```

```
max
```

```
    max = count
```

```
    name = node.
```