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$$a) (1-3x^2-y)dx = (x-3y^2)dy$$

$$y(x) = -\frac{\sqrt[3]{2}x}{\sqrt[3]{(27C_1-27x^3+27x)^2-108x^3+27C_1-27x(x^2-1)}}$$

$$= \frac{\sqrt{(27C_1-27x^3+27x)^2-108x^3+27C_1-27x(x^2-1)}}{3^2\sqrt{2}}$$

$$y(x) = \frac{(1+i\sqrt{3})x}{2^{1/3}\sqrt{(27C_1-27x^3+27x)^2-108x^3+27C_1-27x(x^2-1)}}$$

$$\frac{(1-i\sqrt{3})\sqrt{(27C_1-27x^3+27x)^2-108x^3+27C_1-27x(x^2-1)}}{6\sqrt{2}}$$

$$-3x^2-y(x)+1 = (x-3y(x)^2) \frac{dy(x)}{dx}$$

$$1-3x^2-y(x) + (-x+3y(x)^2) \frac{dy(x)}{dx} = 0$$

$$P(x,y) = -3x^2-y+1 \quad Q(x,y) = -x+3y^2$$

$$f(x,y) = \int (-3x^2-y+1)dx = x-3-yx+g(y)$$

$$\frac{\partial f(x,y)}{\partial y} = \frac{\partial}{\partial y} (x-3-yx+g(y)) = -x + \frac{dg(y)}{dy}$$

$$-x + \frac{dg(y)}{dy} = -x + 3y^2 \quad \frac{\partial f(x,y)}{\partial y} = \frac{\partial}{\partial y} (x-3-yx+g(y))$$

$$\frac{dg(y)}{dy} = 3y^2 \quad \frac{dg(y)}{dy}$$

$$g(y) = \int 3y^2 dy = y^3$$

$$f(x,y) = -x^3 + x + y^3 - yx$$

$$-x^3 + x + y^3 - yx = C_1$$

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$$a) 2xy dx = (x^2 - 2y^3) dy$$

$$y(x) = \sqrt[3]{\frac{2}{3} C_1}$$

$$\sqrt[3]{\frac{3}{2} \sqrt{3 \sqrt{4C_1^3 + 27x^3 + 9x^2}} - \frac{3\sqrt{3} \sqrt{4C_1^3 + 27x^3 + 9x^2}}{32 - 3^{1/3}}}$$

$$y(x) = \frac{(1-i\sqrt{3})\sqrt[3]{\sqrt{3} \sqrt{4C_1^3 + 27x^3 + 9x^2}}}{2\sqrt{2} \cdot 3^{2/3}} - \frac{(1+i\sqrt{3})C_1}{2\sqrt[3]{3} \sqrt{4C_1^3 + 27x^3 + 9x^2}}$$

$$y(x) = \frac{(1+i\sqrt{3})\sqrt[3]{\sqrt{3} \sqrt{4C_1^3 + 27x^3 + 9x^2}}}{2\sqrt{2} \cdot 3^{2/3}} - \frac{(1-i\sqrt{3})C_1}{2\sqrt[3]{3} \sqrt{4C_1^3 + 27x^3 + 9x^2}}$$

$$2xy(x) = (x^2 - 2y(x)^3) \frac{dy(x)}{dx} = 0$$

$$R(x, y) = 2xy \quad S(x, y) = -x^2 + 2y^3$$

$$2y \frac{dy}{dx} R(x, y) = \frac{dy}{dx} S(x, y) - 2y(x) \cdot x$$

$$\frac{dy}{dx} \frac{dy}{dy} = -\frac{2}{y}$$

$$\log(u(y)) = -2 \log(y)$$

$$u(y) = \frac{1}{y^2}$$

$$P(x, y) = \frac{2x}{y}$$

$$Q(x, y) = 2y - \frac{x^2}{y^2}$$

$$\frac{2x}{y^2} + \left(2y(x) - \frac{x^2}{y^2}\right) \frac{dy(x)}{dx} = 0$$

$$\frac{\partial f(x, y)}{\partial x}$$

$$f(x, y) = \int \frac{2x}{y} dx = \frac{x^2}{y} + g(y)$$

$$\frac{\partial f(x, y)}{\partial y} = \frac{\partial}{\partial y} \left(\frac{x^2}{y} + g(y) \right) = -\frac{x^2}{y^2} + \frac{dg(y)}{dy}$$

$$-\frac{x^2}{y^2} + \frac{dg(y)}{dy} = 2y - \frac{x^2}{y^2}$$

$$\frac{dg(y)}{dy} = 2y$$

$$g(y) = \int 2y \, dy = y^2$$

$$f(x, y) = y^2 + \frac{x^2}{y}$$

$$f(x, y) = C_1$$

$$y^2 + \frac{x^2}{y} = C_1$$

$$y' + \frac{x}{y} = c_1$$

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a)

$$y' = \ln \frac{y}{y-1}$$

$$y'(y'-1) \ln \left(\frac{y}{y-1} \right) (y'-1)$$

$$y'(y'-1) = y \ln \left(\frac{y}{y-1} \right) \quad z = y' \quad y'' = \frac{dz}{dx}$$

$$z(z-1) = y \ln \left(\frac{y}{y-1} \right)$$

$$y = z \cdot w \quad y' = z + z'w$$

$$y'' = z''w + 2z'w' + zw''$$

$$z(z-1) = z \cdot w \ln \left(\frac{z-w}{z-1} \right)$$

$$w = z - 1$$

$$y' = z \quad w = \frac{y}{z}$$

$$\frac{dw}{dz} = \frac{d}{dz} \left(\frac{y}{z} \right)$$

$$\frac{dw}{dz} = \frac{z \left(\frac{y}{z} \right) - y}{z^2}$$

$$\frac{dw}{dz} = \frac{y-y}{z} = 0$$

$$w = C \quad \text{and} \quad y = z \cdot w$$

$$y = z \cdot C$$

$$y = C \cdot z \quad y' = \frac{y}{z}$$

$$\frac{dw}{dz} = 0$$

$$z(z-1) = z \cdot w \ln \left(\frac{z \cdot w}{z-1} \right)$$

$$z(z-1) = z \cdot C \cdot \ln \left(\frac{z \cdot C}{z-1} \right)$$

$$z(z-1) = C z \ln \left(\frac{z \cdot C}{z-1} \right)$$

$$y = x y' - e^{y'}$$

$$\frac{dy}{dx} = x \frac{dy'}{dx} \quad u = x \quad v = y'$$

$$y = x y' - e^{y'} \quad y' = \frac{dy}{dx}$$

$$y = x \frac{dy}{dx} - e^{\frac{dy}{dx}}$$

$$y = x (y')^2 - \frac{1}{y'}$$

$$y = x y' - \frac{x}{y'}$$

$$y' = \left(\frac{y + \frac{x}{y'}}{x} \right)$$