COMILLA UNIVERSITY CoU_Expecto_Patronum

NUMBER THEORY

Binary Exponentiation.cpp

```
// (a^b)%mod without overflow
#define long long II
Il bin_expo(Il a, Il b, Il mod) {
  Il result = 1;
  while (b > 0) {
    if (b % 2 == 1) result = (result * a) % mod;
    a = (a * a) \% mod;
    b /= 2;
  }
  return result % mod;
}
```

Fibonacchi in Logn.cpp

```
vector<vector<ll>> identityMatrix({
  \{1, 0\},\
  \{0, 1\}
});
vector<vector<II>> result({
  \{0, 0\},\
  \{0, 0\}
});
void multiply(vector<vector<ll>> a, vector<vector<ll>>
b){
  for(auto &i : result){
    for(auto &j:i){
       j = 0;
    }
  }
  for(int i = 0; i < 2; i++){
    for(int j = 0; j < 2; j++){
       for(int k = 0; k < 2; k++){
         result[i][k] += a[i][j] * b[j][k];
         result[i][k] %= MOD;
       }
    }
  }
```

```
void matrixExpo(vector<vector<II>> matrix, II n){
  if(n == 0){
    result = identityMatrix;
    return;
  matrixExpo(matrix, n / 2);
  multiply(result, result);
  if(n & 1){
    multiply(result, matrix);
  }
II nthFibonacciNumber(II n){
// n <= 1e18, F0 = 0, F1 = 1, F2 = 1
  if(n \le 1)
    return n;
  vector<vector<II>> baseMatrix({
    \{1, 1\},\
    \{1, 0\}
  });
  multiply(baseMatrix, identityMatrix);
  matrixExpo(baseMatrix, n - 1);
  return result[0][0];
}
```

Gcd.cpp

```
int gcd (int a, int b) {
  while (b) {
    a \% = b;
    swap(a, b);
  }
  return a;
```

Miller Rabin Test.cpp

```
ull modmul(ull a, ull b, ull M) {
  II ret = a * b - M * ull(1.L / M * a * b);
  return ret + M * (ret < 0) - M * (ret >= (II)M);
ull modpow(ull b, ull e, ull mod) {
```

```
ull ans = 1;
  for (; e; b = modmul(b, b, mod), e \neq 2)
  if (e & 1) ans = modmul(ans, b, mod);
  return ans;
bool isPrime(ull n) {
  if (n < 2 \mid | n \% 6 \% 4 \mid = 1) return (n \mid 1) == 3;
  ull A[] = {2, 325, 9375, 28178, 450775, 9780504,
1795265022},
    s = builtin ctzll(n-1), d = n >> s;
  for (ull a : A) {
    ull p = modpow(a\%n, d, n), i = s;
    while (p!= 1 && p!= n - 1 && a % n && i--)
       p = modmul(p, p, n);
    if (p!= n-1 && i!= s) return 0;
  }
  return 1;
}
```

Number of Divisor for test case.cpp

```
const II N = 10000004;
bool mark[N];
vector<II> prime;
void siv() {
  // Initialize the sieve
  for (II i = 2; i < N; i++) {
     mark[i] = true;
  for (II i = 2; i * i < N; i++) {
     if (mark[i]) {
       for (|| j = i * i; j < N; j += i) {
          mark[j] = false;
       }
    }
  // Store all primes
  for (II i = 2; i < N; i++) {
     if (mark[i]) prime.push back(i);
  }
}
void solve() {
```

```
Il n; cin >> n;
  II ans = 1;
  for (II i = 0; i < prime.size(); i++) {
    II p = prime[i];
     if (p * p * p > n) break;
    Il count = 1;
     while (n \% p == 0) \{
       n = p;
       count++;
     ans *= count;
  if (n > 1) {
     Il sqrt n = sqrt(n);
     if (sqrt n * sqrt n == n \&\&
binary_search(prime.begin(), prime.end(), sqrt_n))
ans *=3;
     else if (binary_search(prime.begin(), prime.end(),
n))
                ans *=2;
     else ans *= 4;
  cout << ans << endl;
}
```

Number of divisor.cpp

return total; }

Sum of divisor.cpp

```
long long SumOfDivisors(long long num) {
  long long total = 1;
  for (int i = 2; (long long)i * i <= num; i++) {
    if (num % i == 0) {
       int e = 0;
       do {
         e++;
         num /= i;
       } while (num % i == 0);
       long long sum = 0, pow = 1;
       do {
         sum += pow;
         pow *= i;
      \} while (e-- > 0);
       total *= sum;
    }
  if (num > 1) total *= (1 + num);
  return total;
}
```

Phi function.cpp

```
result -= result / i;
}
if (n > 1)
    result -= result / n;
return result;
}
```

Sieve of eratosthenes.cpp

```
const int N = 1e6 + 9;
vector<int> primes;
bool is prime[N];
// use bitset<N> is_prime; to have O(N/64) memory
complexity
void sieve_v0() {
 for (int i = 2; i < N; i++) {
  is_prime[i] = true;
 for (int i = 2; i * i < N; i++) {
  if (is_prime[i]) {
   for (int j = i * i; j < N; j += i) {
     is_prime[j] = false;
   }
 for (int i = 2; i < N; i++) {
  if (is_prime[i]) {
   primes.push_back(i);
  }
 }
}
```

Sieve with smallest prime factors (spf):

```
int spf[N];
void sieve() {
  for (int i = 2; i < N; i++) {
    spf[i] = i;
  }
  for (int i = 2; i * i < N; i++) {
    if (spf[i] == i) {
      for (int j = i * i; j < N; j += i) {
    }
}</pre>
```

```
spf[j] = min(spf[j], i);
}
}
for (int i = 2; i < N; i++) {
  if (spf[i] == i) {
    primes.push_back(i);
  }
}</pre>
```

Dynamic Programming

0/1 Knapsack: complexity O(n*w)

```
int n, w; cin >> n >> w;
  int weight[n], val[n];
  for (int i = 0; i < n; i++) cin >> weight[i];
  for (int i = 0; i < n; i++) cin >> val[i];
  int dp[w + 1] = {};
  for (int i = 0; i < n; i++)
     for (int j = w; j >= weight[i]; j--)
        dp[j] = max(dp[j], dp[j - weight[i]] + val[i]);
  cout << dp[w] << "\n";</pre>
```

Coin Change: Time complexity: O(nx)

```
int n, x; cin >> n >> x;
  int arr[n];
  for (int i = 0; i < n; i++) cin >> arr[i];
  //1) Find the number of distinct ways to sum up to x
  vector<int> dp(x + 1, 0);
  dp[0] = 1;
  for (int i = 1; i <= x; i++)
      for (int j : arr)
        if (i - j >= 0)
            dp[i] = (dp[i] + dp[i - j]) % MOD;
  cout << dp[x] << "\n";
  // 2) Find the number of distinct ordered ways to
  sum up to x
  vector<int> dp(x + 1, 0);
  dp[0] = 1;
```

```
for (int j : arr)
    for (int i = 1; i <= x; i++)
        if (i - j >= 0)
            dp[i] = (dp[i] + dp[i - j]) % MOD;
cout << dp[x] << "\n";
    // 3) Find the minimum number of coins required to
sum up to x
    vector<int> dp(x + 1, INF);
    dp[0] = 0;
    for (int i = 1; i <= x; i++)
        for (int j : arr)
        if (i - j >= 0)
            dp[i] = min(dp[i], dp[i - j] + 1);
cout << (dp[x] == INF ? -1 : dp[x]) << "\n";</pre>
```

DIGIT DP: O(log^2(n))

```
// Find the sum of the digits of the numbers between
a and b (0 <= a <= b <= 1e9)
vector<int> num;
II dp[10][9 * 10][2];
Il memo(int pos, int sum, int flag) {
  if (pos == num.size()) return sum;
  if (dp[pos][sum][flag] != -1) return
dp[pos][sum][flag];
  II res = 0;
  int lmt = (flag) ? 9 : num[pos];
  for (int i = 0; i \le Imt; i++) {
    int next flag = (i < Imt)? 1: flag;
    res += memo(pos + 1, sum + i, next flag);
  return dp[pos][sum][flag] = res;
}
Il calc(int n) {
  num.clear();
  while (n) {
    num.push_back(n % 10);
    n /= 10;
  }
  reverse(num.begin(), num.end());
  memset(dp, -1, sizeof dp);
  return memo(0, 0, 0);
```

```
}
void solve() {
  int a, b; cin >> a >> b;
  if (a == -1 && b == -1) return;
  cout << calc(b) - calc(a - 1) << "\n";
}</pre>
```

FROG2

```
int no_of_stones, no_of_steps, nnn;
  cin >> no_of_stones >> no_of_steps;
  vector <int> height(no_of_stones + 1, 0);
  for(int i = 1; i \le no of stones; i++)
    cin >> height[i];
  const int oo = 1e9;
  vector <int> minimum_cost(no_of_stones + 1, oo);
  minimum cost[1] = 0;
  for(int i = 2; i \le no of stones; i++)
  {
    for(int j = i - 1; j \ge max(1, i - no of steps); <math>j--)
    {
       minimum cost[i] = min(minimum cost[i],
minimum_cost[j] + abs(height[i] - height[j]));
    }
  }
  cout << minimum cost[no of stones];</pre>
```

LCS: Time complexity: O(nm)

```
// Given 2 strings x and y of length n and m, find the
the longest common subsequence (LCS)
string x, y; cin >> x >> y;
int n = x.size(), m = y.size();
int dp[n + 1][m + 1] = {};
for (int i = 1; i <= n; i++) {
    for (int j = 1; j <= m; j++) {
        if (x[i - 1] == y[j - 1])
            dp[i][j] = max(dp[i][j], dp[i - 1][j - 1] + 1);
        else
            dp[i][j] = max({dp[i][j], dp[i - 1][j], dp[i][j - 1]});
}</pre>
```

```
}
cout << dp[n][m];
```

LIS: Time complexity: O(nlogn)

```
// Find the longest increasing subsequence (LIS) in the
array of length n
int n; cin >> n;
vector<int> dp;
for (int i = 0; i < n; i++)
{
   int x;
   cin >> x;
   auto it = lower_bound(dp.begin(), dp.end(), x);
   if (it == dp.end())
       dp.push_back(x);
   else
      *it = x;
}
cout << dp.size() << "\n";</pre>
```

MIN cost to go 1,1 to x,y and Number of ways ways

```
int X, Y; cin>>X>>Y;
  vec<vi> Cost(X,
vector<int>(Y)),dp(x,y),Numway(x,y);
  for (int i = 0; i < X; ++i)
     for (int j = 0; j < Y; ++j)
       cin >> Cost[i][j];
  dp[0][0] = Cost[0][0];
  NumWays[0][0] = 1;
  for (int j = 1; j < Y; ++j) {
     dp[0][j] = dp[0][j - 1] + Cost[0][j];
     NumWays[0][j] = 1;
  }
  for (int i = 1; i < X; ++i) {
     dp[i][0] = dp[i - 1][0] + Cost[i][0];
     NumWays[i][0] = 1;
  }
```

```
for (int i = 1; i < X; ++i) {
    for (int j = 1; j < Y; ++j) {
        dp[i][j] = min(dp[i - 1][j], dp[i][j - 1]) + Cost[i][j];
        NumWays[i][j] = NumWays[i - 1][j] +
NumWays[i][j - 1];
    }
}
cout << dp[X - 1][Y - 1] << endl;
cout << NumWays[X - 1][Y - 1] << endl;</pre>
```

VACATION:

```
// given ai,bi,ci
      ai,bi,ci
// find max
int main() {
  int n;
  cin >> n;
  int a[n], b[n], c[n];
  for (int i = 0; i < n; i++) cin >> a[i] >> b[i] >> c[i];
  int dp[n][3];
  dp[0][0] = a[0];
  dp[0][1] = b[0];
  dp[0][2] = c[0];
  for (int i = 1; i < n; i++) {
     dp[i][0] = a[i] + max(dp[i - 1][1], dp[i - 1][2]);
    dp[i][1] = b[i] + max(dp[i - 1][0], dp[i - 1][2]);
    dp[i][2] = c[i] + max(dp[i - 1][1], dp[i - 1][0]);
  }
  cout << \max(\{dp[n-1][0], dp[n-1][1], dp[n-1][2]\});
  return 0;
}
```

GRAPH/TREE BELLMAN FORD

```
vector<int> bellman_ford(int V, vector<vector<int>>&
edges, int S) {
  vector<int> dist(V, 1e8);
  dist[S] = 0;
  for (int i = 0; i < V - 1; i++) {
    for (auto it : edges) {</pre>
```

```
int u = it[0];
       int v = it[1];
       int wt = it[2];
       if (dist[u] != 1e8 && dist[u] + wt < dist[v]) {
          dist[v] = dist[u] + wt;
       }
     }
  }
  for (auto it : edges) {
     int u = it[0];
     int v = it[1];
    int wt = it[2];
     if (dist[u] != 1e8 && dist[u] + wt < dist[v]) {
       return {-1};
    }
  }
  return dist;
}
int main() {
  int V, E; cin>>V>>E;
  vector<vector<int>> edges(E, vector<int>(3));
  for (int i = 0; i < E; i++)
     cin >> edges[i][0] >> edges[i][1] >> edges[i][2];
  int S; cin >> S;
  vi dist = bellman_ford(V, edges, S);
  for (auto d : dist) cout << d << " ";
  cout << endl;
  return 0;
}
```

BRIDGES and Articulation POINT : Time complexity: O(n + m)

```
// Given an undirected graph, find all bridges and
articulation points
// Time complexity: O(n + m)
const int MAX_N = 1e5 + 1;
int n, m, dfsCounter;
int dfs_num[MAX_N], dfs_low[MAX_N],
visited[MAX_N];
vector<int> adj[MAX_N];
void dfs(int u, int p = -1) {
    dfs_num[u] = dfs_low[u] = dfsCounter++;
```

```
visited[u] = 1;
  int num child = 0;
  for (int v : adj[u]) {
    if (v == p) continue;
    // back edge
    if (visited[v]) dfs low[u] = min(dfs low[u],
dfs_num[v]);
    // tree edge
    else {
       dfs(v, u);
       dfs_low[u] = min(dfs_low[u], dfs_low[v]);
       num child++;
       if (dfs low[v] > dfs num[u])
         cout << "Edge " << u << "-" << v << " is a
bridge\n";
       if (dfs low[v] >= dfs num[u] && p != -1)
         cout << "Node " << u << " is an articulation
point\n";
    }
  }
  // special case: the root node is an articulation point
if it has more than 1 child
  if (p == -1 \&\& num child > 1)
    cout << "Node " << u << " is an articulation
point\n";
}
void solve() {
  cin >> n >> m;
  for (int i = 0; i < m; i++) {
    int u, v; cin >> u >> v;
    adj[u].push_back(v);
    adj[v].push back(u);
  }
  memset(dfs low, -1, sizeof dfs low);
  memset(dfs_num, -1, sizeof dfs_num);
  for (int i = 1; i <= n; i++)
    if (!visited[i])
       dfs(i);
}
  Example input:
    12 16
    13
```

```
3 5
5 7
......

Expected output:
Edge 4-10 is a bridge
Node 4 is an articulation point
Edge 2-4 is a bridge
....
```

DIAMETER OF TREE

```
const int N = 2e5 + 9;
vector<int> g[N];
int farthest(int s, int n, vector<int> &d) {
 static const int inf = N;
 d.assign(n + 1, inf); d[s] = 0;
 vector < bool > vis(n + 1);
 queue<int> q; q.push(s);
 vis[s] = 1; int last = s;
 while (!q.empty()) {
  int u = q.front(); q.pop();
  for (int v: g[u]) {
   if (vis[v]) continue;
   d[v] = d[u] + 1;
   q.push(v); vis[v] = 1;
  }
  last = u;
 return last;
}
int32_t main() {
 int n; cin >> n;
 for (int i = 1; i < n; i++) {
  int u, v; cin >> u >> v;
  g[u].push_back(v);
  g[v].push back(u);
 }
 vector<int> dx, dy;
 int x = farthest(1, n, dx);
 int y = farthest(x, n, dx);
 farthest(y, n, dy);
 for (int i = 1; i <= n; i++) {
  cout << max(dx[i], dy[i]) << ' ';
```

```
}
cout << '\n'; return 0; }</pre>
```

DIJKSTRA

```
const int N = 3e5 + 9, mod = 998244353;
int n, m;
vector<pair<int, int>> g[N], r[N];
vector<long long> dijkstra(int s, int t, vector<int>
&cnt) {
 const long long inf = 1e18;
 priority_queue<pair<long long, int>,
vector<pair<long long, int>>, greater<pair<long long,
int>>> q;
vector<long long> d(n + 1, inf);
vector < bool > vis(n + 1, 0);
 q.push({0, s});
 d[s] = 0;
 cnt.resize(n + 1, 0); // number of shortest paths
 cnt[s] = 1;
 while(!q.empty()) {
  auto x = q.top();
  q.pop();
  int u = x.second;
  if(vis[u]) continue;
  vis[u] = 1;
  for(auto y: g[u]) {
   int v = y.first;
   long long w = y.second;
   if(d[u] + w < d[v]) {
    d[v] = d[u] + w;
    q.push({d[v], v});
    cnt[v] = cnt[u];
   ellipse = d[v] + w = d[v] + cnt[v] + cnt[u] + cnt[u] 
mod;
  }
 }
 return d;
```

```
int u[N], v[N], w[N];
int32_t main() {
 int s, t;
 cin >> n >> m >> s >> t;
 for(int i = 1; i \le m; i++) {
  cin >> u[i] >> v[i] >> w[i];
  g[u[i]].push back({v[i], w[i]});
  r[v[i]].push_back({u[i], w[i]});
 }
 vector<int> cnt1, cnt2;
 auto d1 = dijkstra(s, t, cnt1);
 auto d2 = dijkstra(t, s, cnt2);
 long long shortest_distance = d1[t];
 int number of ways = cnt1[t];
 cout << shortest_distance << '\n';</pre>
 cout << number of ways << '\n';
 return 0;
}
```

DSU

```
struct DSU {
 vector<int> par, rnk, sz;
 int c;
 DSU(int n): par(n + 1), rnk(n + 1, 0), sz(n + 1, 1), c(n) {
  for (int i = 1; i <= n; ++i) par[i] = i;
 }
 int find(int i) {
  return (par[i] == i ? i : (par[i] = find(par[i])));
 bool same(int i, int j) {
  return find(i) == find(j);
 int get_size(int i) {
  return sz[find(i)];
 }
 int count() {
  return c; //connected components
 }
 int merge(int i, int j) {
  if ((i = find(i)) == (j = find(j))) return -1;
  else --c;
```

```
if (rnk[i] > rnk[j]) swap(i, j);
  par[i] = j;
  sz[j] += sz[i];
  if (rnk[i] == rnk[j]) rnk[j]++;
  return j;
}
};
```

FLOYD WARSHALL

```
#include<bits/stdc++.h>
using namespace std;
const int N = 105;
int d[N][N];
int main() {
 int n = 10;
 for (int i = 1; i <= n; i++) {
  for (int j = 1; j <= n; j++) {
   if (i != j) {
    d[i][j] = 1e9;
   }
  }
 for (int k = 1; k \le n; ++k) {
  for (int i = 1; i \le n; ++i) {
   for (int j = 1; j \le n; ++j) {
    d[i][j] = min(d[i][j], d[i][k] + d[k][j]);
   }
  }
 }
 return 0;
}
```

TOPOLOGICAL SORT

```
const int N = 1e5 + 9;
vector<int> g[N];
bool vis[N];
vector<int> ord;
void dfs(int u) {
```

```
vis[u] = true;
for (auto v: g[u]) {
   if (!vis[v]) {
      dfs(v);
   }
} ord.push_back(u);
}
reverse(ord.begin(), ord.end());
```

DATA STRUCTURE

KADANE

```
int ans = LONG_LONG_MIN, sum = 0;
for (int i = 0; i < n; i++)
{
    sum = max(v[i], sum + v[i]);
    ans = max(ans, sum);
}
ans = max(ans, sum);</pre>
```

KMP: Time complexity: O(n + m)

```
// Given a string s (with length n) and a pattern p (with
length m), find all occurrence of p in s
// f[i] = length of the longest proper prefix of the
substring s[0...i] which is also a suffix of this substring
vector<int> prefix func(string s) {
  int n = s.size();
  vector<int> f(n);
  for (int i = 1; i < n; i++) {
     int j = f[i - 1];
     while (j && s[i] != s[j]) j = f[j - 1];
     f[i] = j + (s[i] == s[j]);
  }
  return f;
int cnt_occ(string s, string t) {
  string ts = t + "#" + s;
  int n = t.size(), m = s.size(), nm = ts.size();
  auto f = prefix func(ts);
```

```
int res = 0;
for (int i = n + 1; i < nm; i++) res += (f[i] == n);
return res;
}
void solve() {
   string s, t; cin >> s >> t;
   cout << cnt_occ(s, t) << "\n";
}</pre>
```

SEGMENT TREE POINT UPDATE RANGE QUERY

```
#include <bits/stdc++.h>
using namespace std;
const int N = 3e5 + 9;
int a[N];
struct ST {
  int t[4 * N];
  static const int inf = 1e9;
  ST() {
     memset(t, 0, sizeof t);
  }
  void build(int n, int b, int e) {
     if (b == e) {
       t[n] = a[b];
       return;
    }
     int mid = (b + e) >> 1, l = n << 1, r = l | 1;
     build(I, b, mid);
     build(r, mid + 1, e);
    t[n] = max(t[l], t[r]);
  }
  void upd(int n, int b, int e, int i, int x) {
     if (b > i \mid | e < i) return;
     if (b == e \&\& b == i) {
       t[n] = x;
       // to increase t[n]+=x
       return;
     }
     int mid = (b + e) >> 1, l = n << 1, r = l | 1;
     upd(l, b, mid, i, x);
     upd(r, mid + 1, e, i, x);
```

```
t[n] = max(t[l], t[r]);
}
int query(int n, int b, int e, int i, int j) {
    if (b > j | | e < i) return -inf;
    if (b >= i && e <= j) return t[n];
    int mid = (b + e) >> 1, l = n << 1, r = l | 1;
    int L = query(l, b, mid, i, j);
    int R = query(r, mid + 1, e, i, j);
    return max(L, R);
}
}t;</pre>
```

SEGMENT TREE RANGE UPDATE RANGE QUERY

```
const int N = 5e5 + 9;
int a[N];
struct ST {
 #define lc (n << 1)
 #define rc ((n << 1) | 1)
 long long t[4 * N], lazy[4 * N];
 ST() {
  memset(t, 0, sizeof t);
  memset(lazy, 0, sizeof lazy);
 }
 inline void push(int n, int b, int e) {
  if (lazy[n] == 0) return;
  t[n] = t[n] + lazy[n] * (e - b + 1);
  if (b != e) {
   lazy[lc] = lazy[lc] + lazy[n];
   lazy[rc] = lazy[rc] + lazy[n];
  lazy[n] = 0;
 inline long long combine(long long a,long long b) {
  return a + b;
 inline void pull(int n) {
  t[n] = t[lc] + t[rc];
 void build(int n, int b, int e) {
  lazy[n] = 0;
  if (b == e) {
```

```
t[n] = a[b];
   return;
  }
  int mid = (b + e) >> 1;
  build(lc, b, mid);
  build(rc, mid + 1, e);
  pull(n);
 }
 void upd(int n, int b, int e, int i, int j, long long v) {
  push(n, b, e);
  if (j < b \mid j \in < i) return;
  if (i \leq b && e \leq j) {
   lazy[n] = v; //set lazy
   push(n, b, e);
   return;
  }
  int mid = (b + e) >> 1;
  upd(lc, b, mid, i, j, v);
  upd(rc, mid + 1, e, i, j, v);
  pull(n);
 long long query(int n, int b, int e, int i, int j) {
  push(n, b, e);
  if (i > e \mid | b > j) return 0; //return null
  if (i <= b && e <= j) return t[n];
  int mid = (b + e) >> 1;
  return combine(query(lc, b, mid, i, j), query(rc, mid
+ 1, e, i, j));
 }
};
```

SPARSE TABLE:

```
const int N = 1e5 + 9;
int t[N][18], a[N];
void build(int n) {
  for(int i = 1; i <= n; ++i) t[i][0] = a[i];
  for(int k = 1; k < 18; ++k) {
    for(int i = 1; i + (1 << k) - 1 <= n; ++i) {
        t[i][k] = min(t[i][k - 1], t[i + (1 << (k - 1))][k - 1]);
    }
  }
}</pre>
```

```
int query(int I, int r) {
  int k = 31 - __builtin_clz(r - I + 1);
  return min(t[I][k], t[r - (1 << k) + 1][k]);
}
build(n);</pre>
```

TERNARY SEARCH:

```
int lo=0,hi=1e12,ans=LONG_LONG_MAX;
while (hi-lo>4)
{
   int m1 = (hi+lo)>>1LL;
   int m2 = (hi+lo)/2 + 1;

   int a1 = koro(v, m1);
   int a2 = koro(v, m2);
   if(a1>a2) lo = m1;
   else hi = m2;
   // for max
   if(a1>a2) hi = m1;
   else lo = m2;
}
```

TERNARY SEARCH ON DOUBLE

```
double find_max_volume(double S) {
  double left = 0.0, right = sqrt(S);
  double epsilon = 1e-7;
  while (right - left > epsilon) {
    double mid1 = left + (right - left) / 3.0;
    double mid2 = right - (right - left) / 3.0;
    double volume1 = calculate_volume(mid1, S);
    double volume2 = calculate_volume(mid2, S);
    if (volume1 > volume2) {
        right = mid2;
    } else {
        left = mid1;
    }
}
return calculate_volume((left + right) / 2.0, S);
```

```
}
cout << fixed << setprecision(4) <<
max_volume << endl;</pre>
```

Segment tree point update min val and freq

```
const int N = 1e5+5;
int arr[N];
struct node {
  int ele, freq;
};
node tr[4*N];
node merge(node left, node right) {
  node notun;
  int m = min(left.ele, right.ele);
  int f = 0;
  if(m==left.ele) f+=left.freq;
  if(m==right.ele) f+=right.freq;
  notun.ele=m;
  notun.freq=f;
  return notun;
}
void build(int idx, int b, int e) {
  if(b==e) {
    tr[idx].ele=arr[b],
    tr[idx].freq=1;
    return;
  }
  int left = idx*2+1, right = idx*2+2;
  int mid = (b+e) >> 1LL;
  build(left, b, mid);
  build(right, mid+1, e);
  tr[idx]=merge(tr[left], tr[right]);
node query(int idx, int b, int e, int l, int r) {
  //!overlap
  if(e<l | | r<b) {
    node notun;
```

```
notun.ele=inf;
    notun.freq=0;
    return notun;
  }
  // full overlap
  if(b>=1 && e<=r) return tr[idx];
  int mid = (b+e) >> 1LL;
  return merge(
    query(2*idx+1, b, mid, l, r),
    query(2*idx+2, mid+1, e, l, r)
  );
}
void update(int idx, int b, int e, int pos, int val){
  if(b==e) {
    tr[idx].ele=val;
    tr[idx].freq=1;
    return;
  }
  int mid = (b+e) >> 1LL;
  if(pos<=mid) update(2*idx+1, b, mid, pos, val);</pre>
  else update(2*idx+2, mid+1, e, pos, val);
  tr[idx]=merge(tr[2*idx+1], tr[2*idx+2]);
}
update(0,0,n-1,pos,val);
node koto = query(0,0,n-1,l,r);
cout<<koto.ele<<" "<<koto.freq<<endl;
   NUMBER OF RIGHT BRACKET SEQUENCE
string s;
const int N = 1e6+2;
struct node {
  int open, close, full;
};
node tree[4*N];
node merge(node I, node r) {
  node notun;
  notun.full = I.full+r.full+min(l.open, r.close);
  notun.open = l.open+r.open-min(l.open, r.close);
  notun.close = l.close+r.close-min(l.open, r.close);
  return notun;
node query(int ind, int b, int e, int i, int j) {
```

if(j<b || e<i) {

```
node ans;
    ans.open=0,ans.close=0,ans.full=0;
    return ans;
  }
  if(b>=i && e<=j) return tree[ind];
  int mid = (b+e)>>1;
  return merge(
    query(2*ind+1, b, mid, i, j),
    query(2*ind+2, mid+1, e, i, j)
  );
}
void build(int ind, int b, int e) {
  if(b==e) {
    if(s[b]=='(')
tree[ind].open=1,tree[ind].close=0,tree[ind].full=0;
    else
tree[ind].open=0,tree[ind].close=1,tree[ind].full=0;
    return;
  }
  int left = ind*2+1;
  int right = ind*2+2;
  int mid = (b+e)>>1;
  build(left, b,mid);
  build(right, mid+1,e);
  tree[ind]=merge(tree[left],tree[right]);
}
```

Largest subarray having sum less than equal to k

```
int subarray_start = 0;
  int subarray_end = 0;
  int subarray_sum = 0;
  int max_len = -1;
  for (int i : s) {
     subarray_sum += i;
     subarray_end++;
     while (subarray_sum > k) {
        subarray_sum -= s[subarray_start];
        subarray_start++;
     }
     max_len = max(max_len, subarray_end -
subarray_start);
```

```
} return max_len;
```

Longest sub-array having sum k

```
unordered map<int, int> sum index map;
  int maxLen = 0;
  int prefix sum = 0;
  for (int i = 0; i < N; ++i) {
    prefix sum += A[i];
    if (prefix_sum == K) {
      maxLen = i + 1;
    else if (sum index map.find(prefix sum - K) !=
sum index map.end()) {
      maxLen = max(maxLen, i -
sum index map[prefix sum - K]);
    }
    if (sum_index_map.find(prefix_sum) ==
sum index map.end()) {
      sum_index_map[prefix_sum] = i;
    }
  return maxLen;
```

Longest subarray lenght such that sum is divisible by k

```
int n,k; cin>>n>>k;
  vector<int> v(n);
  for (int i = 0; i < n; i++) cin>>v[i];
  int ans = -1,csum=0
  map<int,int> mp;
  for (int i = 0; i < n; i++)
  {
     csum += v[i];
     int rem = csum%k;
     if(rem==0)
        ans = max(ans, i+1);
     else if(mp.find(rem)!=mp.end())
        ans = max(ans, i-mp[rem]);</pre>
```

```
else mp[rem]=i;
}
if(ans==-1) cout<<ans<<endl;
else cout<<n-ans<<endl;</pre>
```

The number of trailing zeros in the factorial

<u>n!</u>

```
Il n; cin>>n;
int five=0; int ache = 5;
  while (ache<=n) {
     five+=n/ache; ache*=5;
  }
  cout<<five<<endl;</pre>
```

Number of subbarray having sum x

```
int n,k; cin>>n>>k;
  vl v(n); inv(v);
  map<int,int> mp;
  int csum = 0;
  int ans = 0;
  for (int i = 0; i < n; i++)
  {
     csum+=v[i];
     if(mp.find(csum-k)!=mp.end()) {
        ans+=mp[csum-k];
     }
     mp[csum]++;
  }
  ans += mp[k];
  cout<<ans<<endl;</pre>
```

Number of subarray sum divisible by x

```
int n; cin>>n; vl v(n);
  inv(v);
  map<int,int> mp;
  int sum = 0;
  int ans = 0;
  for (int i = 0; i < n; i++)
  {</pre>
```

```
sum+=v[i];
int rm = (sum%n+n)%n;

if(rm==0) ans++;
  mp[rm]++;
}
for(auto &it: mp) ans+=(it.S*(it.S-1))/2;
cout<<ans<<endl;</pre>
```

NUMBER OF INVERSION

```
// Inversion: i < j and A[i] > A[j]
// find the number of inversions of A.
int n;cin >> n;
int a[n + 1];
for (int i = 1; i <= n; i++)
    cin >> a[i];
o_set<int> se;
long long ans = 0;
for (int i = n; i >= 1; i--)
    ans += se.order_of_key(a[i]);
    se.insert(a[i]);
cout << ans << '\n';</pre>
```

ORDERED SET

```
#include<ext/pb_ds/assoc_container.hpp>
#include<ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
using namespace std;
template <typename T> using o_set = tree<T,
null_type, less<T>, rb_tree_tag,
tree_order_statistics_node_update>;
template <typename T, typename R> using o_map =
tree<T, R, less<T>, rb_tree_tag,
tree_order_statistics_node_update>;
int main() {
  int i, j, k, n, m;
  o_set<int>se;
  se.insert(1);
  se.insert(2);
```

```
cout << *se.find_by_order(0) << endl; ///k th
element
cout << se.order_of_key(2) << endl; ///number of
elements less than k
o_map<int, int>mp;
mp.insert({1, 10});
mp.insert({2, 20});
cout << mp.find_by_order(0)->second << endl; ///k
th element
cout << mp.order_of_key(2) << endl; ///number of
first elements less than k
return 0;
}</pre>
```

THEOREM

```
a^b^c
b = power(b,c, mod-1);
cout<<power(a,b, mod)<<endl;

(1/a)%m = pow(a,m-2,m)

# Chicken McNugget Theorem / Postage Stamp
Problem / Frobenius Coin Problem
For any two relatively prime positive integers m,n.
The greatest integer that cannot be written in the form am + bn is (mn-m-n).
There are exactly (m - 1)(n - 1)/2 positive integers which cannot be expressed in the form am + bn
ios_base::sync_with_stdio(false); cin.tie(NULL);
```

PYTHON

```
import math
t = int(input()) # Number of test cases
for i in range(1, t + 1):
    a, b = map(int, input().split())
    print(a + b) # Sum
```

cout.tie(NULL)

```
print(a - b) # Difference
product = a * b # Store the product of a and b
print(product) # Product
print(a // b) # Quotient (integer division)
print(a % b) # Remainder
g = math.gcd(a, b) # GCD
print(g) # Print GCD
print(product // g) # LCM
print(math.sqrt(a)) # Square root of a
print(math.sqrt(b)) # Square root of b
a, b, c, d = map(int, input().split())
if a * d == b * c:
    print("Equal")
else:
    print("Not Equal")
```

1.1 Primality Test

```
bool prime (int N) {
  if (N < 2)
     return false:
  if (N \le 3)
     return true;
  if (N \% 2 == 0)
     return false:
  for (int i = 3; i * i <= N; i += 2) {
    if (N \% i == 0)
       return false;
  return true:
```

1.2 Miller-Rabin Primality Test

Description: Deterministic Miller-Rabin primality test. Guaranteed to work for numbers up to 7·10e18; for larger numbers, use Python and extend A randomly.

Time: 7 times the complexity of a^b mod c.

```
typedef unsigned long long ull;
#define ll long long int
ull modmul(ull a, ull b, ull M) {
  ll ret = a * b - M * ull(1.L / M * a * b);
  return ret + M * (ret < 0) - M * (ret >= (11)M);
ull modpow(ull b, ull e, ull mod) {
  ull ans = 1:
  for (; e; b = modmul(b, b, mod), e = 2)
    if (e & 1) ans = modmul(ans, b, mod);
  return ans:
bool isPrime(ull n) {
  if (n < 2 || n \% 6 \% 4 != 1) return (n | 1) == 3;
  ull A[] = \{2, 325, 9375, 28178, 450775, 9780504, 1795265022\}
        s = builtin ctzll(n-1), d = n >> s;
  for (ull a : A) {
     ull p = \text{modpow}(a\%n, d, n), i = s;
     while (p != 1 \&\& p != n - 1 \&\& a \% n \&\& i--)
       p = modmul(p, p, n);
     if (p != n-1 \&\& i != s) return 0;
  return 1;
```

1.3 Sieve of Eratosthenes

```
Description: Normal sieve for generating all primes numbers up to 1e8.
const int N = 100000000:
bool is prime[N+1]:
vector<int>prime;
void sieve() {
  memset (is prime, true, sizeof(is prime));
  for (int i = 3: i * i <= N: i += 2) {
    if (is prime[i]) {
       for (int j = 2*i; j \le N; j += i)
          is prime[j] = false;
  prime.push back(2);
  for (int i = \overline{3}; i \le N; i += 2) {
    if (is prime[i])
       prime.push back(i);
```

1.4 Prime Factorization

mp[N]++;

Description: For first one, Generating Sieve of Eratosthenes.

```
map<int, int>mp:
                                     // Complexity: O(log(log(N))
void prime factor (int N) {
  int i = 0, pf = prime [0];
  while (pf * pf \le N) {
    while (N \% pf == 0)  {
      N = pf:
       mp[pf]++;
    pf = prime[i++];
  if (N > 1)
    mp[N]++;
map<int,int>mp;
                                     // Complexity: O(Sqrt(N))
void prime factor (int N) {
  for (int i = 2; i * i \le N; i++) {
    if (N \% i == 0)  {
       while (N % i == 0) {
         N = i;
         mp[i]++;
  if (N > 1)
```

1.5 Divisors

```
Description: Complexity: O(Sqrt(N))
set<int>st:
```

```
void Divisors (int N) {
  for (int i = 1; i*i \le N; i++) {
     if (N \% i == 0)  {
        st.insert(i); st.insert(N / i);
```

1.6 Number of Divisors

Description: Complexity: O(Sqrt(N))

```
int number of divisors (int N) {
  int total = 1;
  for (int i = 2; i*i \le N; i++) {
     if (N \% i == 0)  {
       int e = 0:
       while (N \% i == 0)  {
          e++; N = i;
        total *= e + 1:
  if (N > 1) total *= 2;
  return total;
```

Description: For multiple test cases. (CSES-Counting Divisors) At first, Generating Sieve of Eratosthenes up to 10⁶.

```
#define all(v) v.begin(),v.end()
int number of divisors (int n) {
  int ans = 1:
  for (int i = 0; i < prime.size(); i++) {
     int p = prime[i];
     if (p * p * p > n)
        break:
     int count = 1;
     while (n \% p == 0)  {
        n \neq p; count++;
     ans *= (count);
  if (binary search(all(prime), n)) ans *= 2;
   else if (binary search(all(prime), sqrt(n))) ans *= 3;
   else if (n > 1) ans *= 4;
   return ans;
```

1.7 Sum of Divisors

Description: Complexity: O(Sqrt(N))

```
Il SumOfDivisors (Il num) {
  II total = 1:
  for (ll i = 2; i * i \le num; i++) {
    if (num \% i == 0) {
       II e = 0:
       do {
         e++:
         num = i:
       } while (num % i == 0);
       II sum = 0, pow = 1;
       do {
         sum += pow;
         pow *= i;
       } while (e-->0);
       total *= sum;
  if (num > 1)
    total *= (1 + num);
  return total;
```

Description: Calculate the sum of divisors of 1 to N

```
const 11 \text{ MOD} = 1000000007;
ll sigma (ll x) {
  return ((x \% MOD) * ((x + 1) \% MOD) / 2) \% MOD;
ll SumOfDivisors (ll N) {
  11 sum = 0;
  for (111 = 1; 1 \le N; 1++)
    11 r = N / (N / 1);
    sum += (N/1) \% MOD * (sigma(r) - sigma(l-1) + MOD) \% MOD;
    sum = (sum + MOD) \% MOD;
    1 = r:
  return sum;
```

Modular Arithmetic

```
(a + b) \% M = ((a \% M) + (b \% M)) \% M
(a - b) \% M = ((a \% M) - (b \% M) + M) \% M
(a * b) \% M = ((a \% M) * (b \% M)) \% M
(a/b) % M = ((a \% M) * (b^{-1} \% M)) % M
```

Binary Exponentiation

Description: Calculate the values a^b modulo $10^{9}+7$.

Complexity: O(log(b)) **const** 11 MOD = 10000000007;

II BinExpo (ll a, ll b) { 11 ans = 1;while (b) { **if** (b & 1) ans = (ans * a) % MOD; a = (a * a) % MOD: b >>= 1:

Large Exponentiation

Description: Calculate the values a^{b^c} modulo 10^{9+7} .

Complexity: O(log(b))

return ans:

```
const 11 \text{ MOD} = 1000000007;
II BinExpo (ll a, ll b, ll MOD) {
  11 \text{ ans} = 1:
  while (b) {
    if (b & 1) ans = (ans * a) \% MOD;
    a = (a * a) \% MOD;
    b >>= 1:
  return ans;
```

• BinExpo(a, BinExpo (b, c, MOD-1), MOD)

Binary Multiplication

Description: Calculate the values a*b modulo 10^9+7 .

Complexity: O(log(b))

```
const 11 \text{ MOD} = 10000000007:
II BinMultiply(ll a, ll b) {
  11 \text{ ans} = 1:
  while (b) {
    if (b & 1) ans = (ans + a) % MOD;
    a = (a + a) \% MOD;
    b >>= 1:
  return ans;
```

Modular Multiplicative Inverse

Description: Calculate the values a^{-1} modulo $10^{9}+7$.

```
const 11 MOD = 1000000007;
II ModInverse(ll a) {
  11 b = MOD - 2;
  11 \text{ ans} = 1:
  while (b) {
    if (b & 1) ans = (ans * a) \% MOD;
    a = (a * a) \% MOD;
    b >>= 1:
  return ans;
```

Binomial Coefficients

Description: Calculate the values $\binom{n}{n}$ modulo 10^{9+7} for N test cases.

Where $1 \le N \le n \le r \le 10^6$

```
const 11 \text{ N} = 1000001:
const 11 \text{ MOD} = 1000000007;
II fact[N];
void Factorial () {
   fact [0] = 1;
   for (ll i = 1; i \le N; i++)
      fact[i] = (fact[i-1] * i) % MOD;
II ModInverse(ll a) {
   11 b = MOD - 2;
   11 \text{ ans} = 1;
   while (b) {
      if (b & 1) ans = (ans * a) % MOD;
      a = (a * a) \% MOD;
      b >>= 1:
   return ans:
\mathbf{II} \, \mathbf{nCr} \, (\mathbf{ll} \, \mathbf{n}, \, \mathbf{ll} \, \mathbf{r}) \, \{
   ll ans = fact[n];
   ll den = (fact[n-r] * fact[r]) % MOD;
   ans = (ans * ModInverse(den)) % MOD;
   return ans:
```

Fibonacci Numbers

Description: Find the Fibonacci numbers till 10^{18} .

Kadane's Algorithm

Description: Find the maximum subarray sum.

Complexity: O(N)

```
int KadanesAlgo(int a[], int N) {
  int MaxSum = INT_MIN;
  int CurrentSum = 0;

for (int i=0; i<N; i++) {
    CurrentSum += a[i];
    MaxSum = max (MaxSum, CurrentSum);
    if (CurrentSum < 0)
        CurrentSum = 0;
  }
  return MaxSum;
}</pre>
```

Counting Subarrays

Description: Count the number of subarrays having sum x.

```
Il N, x, sum, cnt, a;
map<II, II> freq;
Il SubArray () {
    cin >> N >> x;
    freq[0] = 1;
    for (II i = 1; i <= N; i++) {
        cin >> a;
        sum += a;
        cnt += freq[sum-x];
        freq[sum]++;
    }
    return cnt;
}
```

Description: Count the number of subarrays where the sum of values is divisible by x.

```
II N, x, pre, cnt, a;
map<|ll, l|> freq;
II SubArray () {
    cin >> N >> x;
    freq[0] = 1;
    for (Il i = 1; i <= N; i++) {
        cin >> a;
        pre = ((pre+a) % x + x) % x;
        cnt += freq[pre];
        freq[pre]++;
    }
    return cnt;
}
```

```
AND (&): any 0 => 0

OR (|): any 1 => 1

X-OR (^): same => 0, different=> 0

Left Shift: n<<i, n*2^(i)

Right Shift: n>>i, n/2^(i)

2^n = 1<<n
```

Binary Search

```
while(l<=r) {
    mid = (l+r) / 2;
    if (a[mid] == value)
        return mid;
    if(a[mid] < value)
        l = mid + 1;
    else
        r = mid - 1;
```

If a number n has an odd divisor, then it has an odd prime divisor. If a number has no odd divisors, then it must be a power of two.

• Check Power of two: n&(n-1) == 0 Only perfect square number has odd number of divisors.

Vector

```
sort(v.begin(), v.end()); //Increasing
sort(v.begin(), v.end(), greater<int>()); //Decreasing
sort(v.rbegin(), v.rend()); //Reverse
rotate(v.begin(), v.begin()+1, v.end()) // Rotate
    • swap(v[i], v[i+1])
int UniqueValue = unique(v.begin(), v.end()) - v.begin();
int MaxValue = max element(v.begin(), v.end()) - v.begin();
int MinValue = min element(v.begin(), v.end()) - v.begin();
         cout << MaxValue << endl; //Index
         cout << *MaxValue << endl: //Value
v.pop back();
v.back(); //LastValue
v.erase(v.begin()); //O(n)
Check sorted or not:
if (is sorted(v.begin(), v.end()))
  cout << "execute" << endl:
```

```
String
getline (cin, s);
s.push back();
s.pop back();
s.back(); //LastValue
s.erase(v.begin() + i); //i = index
Subtring
string str = s.substring (i, j);
                            //i=>Strating index, j=>Ending index
Check Subtring:
if (a.substring(0, n) == s)
  cout << "Yes" << endl:
if(s.find(str)!=string::npos) //Return 0 or 1
  cout << "Yes" << endl:
2D String
string s [n];
for (int i = 0; i < n; i++) cin >> s[i];
Accessing Index:
for (int i = 0; i < n; i + +) {
  for (int i = 0; i < n; i++) {
     if(s[i][i] == "-") cout << "-" << endl;
int x = stoi(s); // String to Number
                            for (auto i: s) x + = x*10 + (i - 48);
string s = to string(x) / Number to String
```

Adjacency List

```
Description: n=>node, m=>edges
const int mx = 10e5+123:
vector<int>adj[mx];
cin >> n >> m:
for (i=0; i<m; i++) {
  int u,v;
  cin >> u >> v;
  adj[u].push back(v);
  adj[v].push back(u);
const int mx = 1e5 + 123:
vector<pair<int,int>> adi[mx];
cin >> n >> m:
for(i=1; i \le m; i++)
```

Adjacency Matrix

cin >> u >> v >> w:

 $adi[u].push back(\{v,w\});$ adj[v].push back({u,w});

int u, v, w;

Description: n=>node, m=>edges

```
char adjMat[mx][mx];
cin >> n >> m;
  for (int j=1; j \le m; j++)
     cin >> adjMat[i][j];
```

Description: n=>node, m=>edges

```
const int mx = 1002:
bool vis[max];
vector<int>adj[mx];
void dfs (int u) {
   \mathbf{vis}[\mathbf{u}] = 1;
   for (auto v: adj[u]) {
     if (vis[v] == 0)
        dfs(v);
```

Find Connected Components

Description: dfs is required.

if (vis[v] == 0)dfs(v);

for (int i = 1; $i \le n$; i++) {

cc.push back(current cc);

if(vis[i]) continue;

current cc.clear();

int CC(int n) {

dfs(i);

return cnt:

Cycle Detection

```
int CC (int n) {
  int cnt = 0;
  for (int i = 1; i \le n; i++) {
    if(vis[i]) continue;
    dfs(i);
    cnt++;
  return cnt;
Description: To store connected components.
vector<vector<int>>cc;
vector<int>current cc;
void dfs (int u) {
  vis[u] = 1;
  current cc.push back(u);
  for (auto v: adj[u]) {
```

```
const int mx = 1002;
```

for (int i=1; $i \le n$; i++) {

Depth First Search (DFS)

```
bool is cycle(int node, int par){
     vis[node] = true;
    for (auto& new node : adj[node]) {
       if (!vis[new node]){
         if (is cycle(new node, node))
            return true:
       else if (new node != par) return true;
     return false;
```

Breath First Search (BFS)

Description: Distance vector provides the level of all nodes.

```
const int mx = 1e5+123:
int vis[mx],dis[mx];
vector\langle int \rangle v[mx];
void bfs(int node) {
  queue<int>q;
  q.push(node);
   vis[node]=1; dis[node]=0;
   while (!q.empty()) {
     int a=q.front();
     q.pop();
     for (int child: v[a]) {
        if (vis[child]==0) {
          dis[child]=dis[a]+1;
          vis[child]=1;
          q.push(child);
```

Dijkstra

Description:

```
const int mx = 1e5+123:
vector<pair<int,int>> adj[mx];
ll dis[mx];
void dijkstra (int s, int n) {
  for (int i = 0; i \le n; i++) dis[i] = infLL;
  dis[s] = 0;
priority queue<pair<|l,|l>,vector<pair<|l,|l>>,greater<pair<|l,|l>>>pq;
  pq.push ( \{ 0, s \} );
  while (!pq.empty() ) {
    int u = pq.top().second;
    ll curD = pq.top().first;
    pq.pop();
    if (dis[u] < curD ) continue;</pre>
    for (auto p : adj[u]) {
       int v = p.first;
       11 w = p.second;
       if (curD + w < dis[v]) {
         dis[v] = curD + w;
         pq.push ( { dis[v], v } );
```