

AMERICAN INTERNATIONAL UNIVERSITY BANGLADESH  
Faculty of Engineering

Laboratory Report Cover Sheet



Students must complete all details except the faculty use part.

Please submit all reports to your subject supervisor or the office of the concerned faculty.

Laboratory Title: Study of Nyquist bit rate and Shannon capacity using MATLAB  
Experiment Number: 03 Submission Date: 15/02/2023 Semester: Spring 2022 - 2023  
Subject Code: COE 3201 Subject Name: Data Communication Section: K  
Course Instructor: DR. SHUVRA MONDAL Degree Program: BSc CSE

Declaration and Statement of Authorship:

- I/we hold a copy of this report, which can be produced if the original is lost/ damaged.
- This report is my/our original work and no part of it has been copied from any other student's work or from any other source except where due acknowledgement is made.
- No part of this report has been written for me/us by any other person except where such collaboration has been authorized by the lecturer/teacher concerned and is clearly acknowledged in the report.
- I/we have not previously submitted or currently submitting this work for any other course/unit.
- This work may be reproduced, communicated, compared and archived for the purpose of detecting plagiarism.
- I/we give permission for a copy of my/our marked work to be retained by the School for review and comparison, including review by external examiners.

I/we understand that

- Plagiarism is the presentation of the work, idea or creation of another person as though it is your own. It is a form of cheating and is a very serious academic offence that may lead to expulsion from the University. Plagiarized material can be drawn from, and presented in, written, graphic and visual form, including electronic data, and oral presentations. Plagiarism occurs when the origin of the material used is not appropriately cited.
- Enabling plagiarism is the act of assisting or allowing another person to plagiarize or to copy your work

Group Number (if applicable): 01 ☐ Individual Submission ☒ Group Submission

No.	Student Name	Student ID	Contribution
1	SHEAKH, MOHAMMAD BIN AB. JALIL SHEAKH	20-42132-1	Performance Task (b)
2	AURTHY, MOST. LILUN NAHAR	20-43997-2	Performance Task (b)
3	NISHAT, TARIKUL ISLAM	21-44632-1	Abstract, Introduction, Performance Task (c)
4	MULLICK, IFTEKHAR UDDIN	21-44649-1	Discussion, Conclusion, Performance Task (d)
5	ULLAH, MD ISMAIL JOBI	21-44747-1	Performance Task (c)
6	ALANSAR, SADIHA	21-45612-3	Performance Task (d)

For faculty use only:

Total Marks: 6 Marks Obtained: 6

Faculty comments

*Excellent!*



## Title:

Study of Nyquist bit rate and Shannon capacity using MATLAB

## Abstract:

This experiment was designed to help understand the use of MATLAB for solving communication engineering problems. This experiment also helps us develop the understanding of Nyquist bit rate and Shannon capacity using MATLAB.

## Introduction:

- i. **Nyquist Bit Rate:** The Nyquist bit rate formula defines the theoretical maximum bit rate for a noiseless channel.

$$\text{BitRate} = 2 \times \text{bandwidth} \times \log_2 L$$

In this formula, bandwidth is the bandwidth of the channel,  $L$  is the number of signal levels used to represent data, and BitRate is the bit rate in bits per second.

- ii. **Shannon capacity:** Shannon capacity formula was introduced to determine the theoretical highest data rate for a noisy channel:

$$\text{Capacity} = \text{bandwidth} \times \log_2 (1 + \text{SNR})$$

In this formula, bandwidth is the bandwidth of the channel, SNR is the signal-to-noise ratio, and capacity is the capacity of the channel in bits per second.

**Signal-to-noise ratio (SNR):** To find the theoretical bit rate limit, we need to know the ratio of the signal power to the noise power.

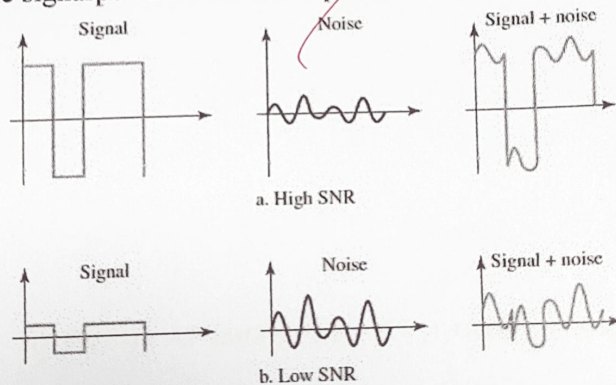


Fig: Two cases of SNR; One is high and the other is Low SNR  
Because SNR is the ratio of two powers, it is often described in decibel units, SNRdB, defined as  $\text{SNRdB} = 10 \log_{10} (\text{SNR})$



## Simulation:

### Performance Task:

The selected ID is the following:

2	0	-	4	3	9	9	7	-	2
A	B		C	D	E	F	G		H

**Performance Task for Lab Report:** (your ID = AB-CDEFG-H)

**\*\*Generate a composite signal using two simple signals as,**

$x = A1 \sin(2\pi((C+D+H)*100)t) + A2 \cos(2\pi((D+E+H)*100)t) + s*\text{randn}(\text{size}(t));$

(a) Select the value of the amplitudes as follows: let  $A1 = (A+B+H)$ ,  $A2 = (B+C+H)$  and  $s = (C+D+H)/30$

(b) Calculate the SNR value of the composite signal.

(c) Find the bandwidth of the signal and calculate the maximum capacity of the channel.

(d) What will be the signal level to achieve the data rate?

### Performance Task A:

$$A1 = 2 + 0 + 2 = 4$$

$$A2 = 0 + 4 + 2 + 6$$

$$s = (4 + 3 + 2) / 30 = 9 / 30$$

### Performance Task B :

#### Code:

```
close all;
```

```
clc;
```

```
%Define number of samples to take  
fs = 8000; % Sampling frequency
```

```
A = 2;
```

```
B = 0;
```

```
C = 4;
```

```
D = 3;
```

```
E = 9;
```

```
F = 9;
```

```
G = 7;
```

```
H = 2;
```

```
t = 0:1/fs:1-1/fs;
```

```
A1 = A + B + H;
```

```
A2 = B + C + H;
```

```
s = (C + D + H)/30;
```

```
X = A1*sin(2*pi*((C + D + H)*100)*t) + A2*cos(2*pi*((E + D + H)*100)*t) + s*randn(size(t));  
%noise
```

```
noise = s*randn(size(X));
```

```
noisySignal = X + noise;
```

```
SNR = snr(noisySignal) %Calculation of SNR using snr function
```



Command Window

```
>> %Define number of samples to take
fs = 8000; % Sampling frequency
A = 2;
B = 0;
C = 4;
D = 3;
E = 9;
F = 9;
G = 7;
H = 2;
t = 0:1/fs:1-1/fs;
A1 = A + B + H;
A2 = B + C + H;
s = (C + D + H)/30;
X = A1*sin(2*pi*((C + D + H)*100)*t) + A2*cos(2*pi*((E + D + H)*100)*t) + s*randn(size(t));
%noise
noise = s*randn(size(X));
noisySignal = X + noise;
SNR = snr(noisySignal) %Calculation of SNR using snr function

SNR =
    3.3805
```

fx >>

Fig 1: SNR value of the composite signal

**Performance Task C :**

**Code:**

```
fs = 8000; % Sampling frequency
%Define signal
t = 0:1/fs:1-1/fs;
A = 2;
B = 0;
C = 4;
D = 3;
E = 9;
F = 9;
G = 7;
H = 2;
%signal
A1 = A + B + H;
A2 = B + C + H;
s = (C + D + H)/30;
X = A1*sin(2*pi*((C + D + H)*100)*t) + A2*cos(2*pi*((E + D + H)*100)*t) + s*randn(size(t));
%noise
ns = s*randn(size(X));
S_N_R = snr(X,ns);
bandwidth = obw(X,fs) % Bandwidth of the signal
%capacity
C = bandwidth*log2(1+S_N_R)
```

# Command Window

```
>> fs = 8000; % Sampling frequency
%Define signal
t = 0:1/fs:1-1/fs;
A = 2;
B = 0;
C = 4;
D = 3;
E = 9;
F = 9;
G = 7;
H = 2;
%signal
A1 = A + B + H;
A2 = B + C + H;
s = (C + D + H)/30;
X = A1*sin(2*pi*((C + D + H)*100)*t) + A2*cos(2*pi*((E + D + H)*100)*t) + s*randn(size(t));
%noise
ns = s*randn(size(X));
S_N_R = snr(X,ns);
bandwidth = obw(X,fs) % Bandwidth of the signal
%capacity
C = bandwidth*log2(1+S_N_R)

bandwidth =

    500.9822

C =

    2.3448e+03

fx >> |
```

Fig 2: Bandwidth of the signal and the maximum capacity of the channel

## Performance Task D:

### Code :

```
fs = 8000; % Sampling frequency
A = 2;
B = 0;
C = 4;
D = 3;
E = 9;
F = 9;
G = 7;
H = 2;
t = 0:1/fs:1-1/fs; % Time duration
A1 = A + B + H;
A2 = B + C + H;
s = (C + D + H)/30;
X = A1*sin(2*pi*((C + D + H)*100)*t) + A2*cos(2*pi*((E + D + H)*100)*t) + s*randn(size(t));
bandwidth = obw(X,fs) % Bandwidth of the signal
L=1.9;
BitRate = 2*bandwidth*log2(L)
L = 2.^(BitRate/(2*bandwidth)) %Signal level to achieve data rate
```



#### Command Window

```
>> fs = 8000; % Sampling frequency
A = 2;
B = 0;
C = 4;
D = 3;
E = 9;
F = 9;
G = 7;
H = 2;
t = 0:1/fs:1-1/fs; % Time duration
A1 = A + B + H;
A2 = B + C + H;
s = (C + D + H)/30;
X = A1*sin(2*pi*((C + D + H)*100)*t) + A2*cos(2*pi*((E + D + H)*100)*t) + s*randn(size(t));
bandwidth = obw(X,fs); % Bandwidth of the signal
L=1.9; % Level of the signal
BitRate = 2*bandwidth*log2(L)

BitRate =

    927.8188

>> L = 2.^(BitRate/(2*bandwidth))

L =

    1.9000

fx >>
```

Fig 3: The signal level to achieve the data rate

#### Discussion and Conclusion:

In the following experiment, the problem statement (b), the Signal-to-noise ratio (SNR) was determined. To determine the following value, two methods were implemented in MATLAB. In the MATLAB, there was a pre-determined function called 'snr' function. This function can determine the value of SNR by implementing the value signal. In the performance task, the noisy composite signal was implemented in the snr function and a value was obtained. Another way to determine the SNR value is using the definition of SNR. But using that formula can cause some errors in the calculation due to using approximation and manual input. Hence, the 'snr' function is used for the most accurate answer.

In the problem statement (c), bandwidth of the signal was determined using the built-in function - obw. The 'obw' function took the composite signal and the estimated sample frequency and provided the value of bandwidth. Using the SNR Value and Bandwidth, maximum capacity of the channel was calculated. This provided us with a value that tells us the highest theoretical data rate in the noisy channel in bits/sec.

In the problem statement (d), the level of the signal was determined at which the data rate could have been achieved. The signal level needed to be as low as possible as increasing level of signal reduces the reliability of the system. As the level of system matched with the preferred level of signal used on previous calculations, the signal level was appropriate for the data rate for the composite signal. Hence, all the objectives of the experiment were achieved.

**References:**

- Prakash C. Gupta, "Data communications", Prentice Hall India Pvt.
- William Stallings, "Data and Computer Communications", Pearson
- Forouzan, B. A. "Data Communication and Networking. Tata McGraw." (2005).
- AIUB Data Communication Engineering Lab Manual, Report 03