MAST90104: A First Course in Statistical Learning

Week 8 Practical and Workshop

1 Practical questions

1. Consider the filter question in Week 7. Recall that we are interested in comparing the lifespan of 5 different types of filters. Six filters of each type are tested, and the time to failure in hours is given in the dataset (on the website) filters (in csv format).

Read the data. Then convert the type component into a factor. Recall that we fit a one-way classification model using the treatment contrast

> model <- lm(y~type, data=filters)</pre>

- (a) Calculate a 95% confidence interval for the difference in lifespan between filter types 3 and 4.
- (b) Show that the hypothesis that the filters all have the same lifespan is testable.
- (c) Test this hypothesis, using matrix theory.
- (d) Test the same hypothesis using the linear Hypothesis function from the car package.
- (e) Repeat part d using the sum-to-zero contrast (contr.sum)
- 2. We study the effect of various breeds and diets on the milk yield of cows. A study is conducted on 9 cows and the following data obtained:

		Diet	
Breed	1	2	3
1	18.8	16.7	19.8
	21.2		23.9
2	22.3	15.9	21.8
		19.2	

- (a) Input this data into R. Plot an interaction plot between breed and diet.
- (b) Fit an additive model. What is the estimated amount of milk produced from breed 2 and diet 3 now?
- (c) Test the hypothesis (under the additive model) that the 2nd and 3rd diets are equivalent in terms of milk produced.
- (d) Find a 95% confidence interval, under the additive model, for the amount of milk produced from breed 2 and diet 3. Use both matrix calculations and the estimable function from the gmodels package.

2 Workshop questions

1. An industrial psychologist is investigating absenteeism among production-line workers, based on different types of work hours: (1) 4-day week with a 10-hour day, (2) 5-day week with a flexible 8-hour day, and (3) 5-day week with a structured 8-hour day. A study is conducted and the following data obtained of the average number of days missed:

	Work plan		
	1	2	3
Mean	9	6.2	10.1
Number	100	85	90

They also find $s^2 = 110.15$.

- (a) Test the hypothesis that the work plan has no effect on the absenteeism.
- (b) Test the hypothesis that work plans 1 and 3 have the same rate of absenteeism.
- 2. Prove Theorem 6.2 using the following steps.
 - (a) Show that under the conditions of Theorem 6.1 (question 4 above), the column space of XC is the same as the column space of X.
 - (b) Show that if two full-rank linear models have the same column space, the eigenvectors of their hat matrices are the same.
 - (c) Hence show that if the column space for two linear models is the same, the fitted values are the same.
 - (d) Complete the proof of Theorem 6.2.
- 3. Consider question 2 in practical class this week, where we study the effect of various breeds and diets on the milk yield of cows. A study is conducted on 9 cows and the following data obtained:

		Diet	
Breed	1	2	3
1	18.8	16.7	19.8
	21.2		23.9
2	22.3	15.9	21.8
		19.2	

- (a) Express this as a two-factor model with no interaction in matrix form.
- (b) Express this as a two-factor model with interaction in matrix form.
- (c) Express the hypothesis that there is no interaction in terms of your parameters. Eliminate any redundancies.