

Lecture Summary: Feb. 10, 2023

- Remedial measures

1. Transformation of x : For nonlinear association.
2. Transformation of Y : For non-normality/unequal variance.

Box-Cox transformation

This is a collection of transformations depending on a “tuning parameter”, λ . The definition is the following:

$$Y'_i = \begin{cases} K_1(Y_i^\lambda - 1), & \lambda \neq 0, \\ K_2 \log(Y_i), & \lambda = 0, \end{cases}$$

where K_1, K_2 are two numbers computed from the data, with K_1 depending on λ :

$$K_2 = (Y_1 Y_2 \dots Y_n)^{1/n} = e^{\overline{\log Y}}, \quad K_1 = \frac{1}{\lambda K_2^{\lambda-1}},$$

where $\overline{\log Y} = n^{-1} \sum_{i=1}^n \log(Y_i)$ (\log means natural logarithm).

How does it work?

- (i) For each λ , find the SSE of regression of Y' on x (i.e., Y' is the response variable, x is the predictor variable).
- (ii) The SSE depends on λ . Find the λ whose SSE is the smallest, which corresponds to the optimal transformation.