Advanced Encryption Standard (AES)



Outline

- Overview of the AES algorithm
- Internal structure of AES
 - Byte Substitution
 - Shift rows
 - MixColumns
 - Key Addition
 - Key schedule
- Decryption

Overview of the AES algorithm



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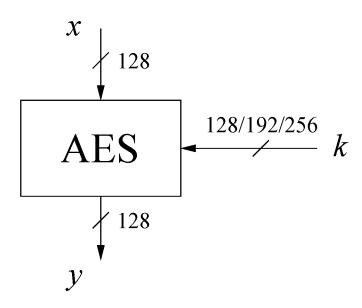
Some Basic Facts

- AES is the most widely used symmetric cipher today
- The algorithm for AES was chosen by the US National Institute of Standards and Technology (NIST) in a multi-year selection process
- The requirements for all AES candidate submissions were:
 - Block cipher with 128-bit block size
 - Three supported key lengths: 128, 192 and 256 bit
 - Security relative to other submitted algorithms
 - Efficiency in software and hardware implementation

Chronology of the AES Selection

- The need for a new block cipher announced by NIST in January, 1997
- 15 candidates algorithms accepted in August, 1998
- 5 finalists announced in August, 1999:
 - Mars IBM Corporation
 - RC6 RSA Laboratories
 - Rijndael J. Daemen & V. Rijmen
 - Serpent Eli Biham et al.
 - Twofish B. Schneier et al.
- In October 2000, Rijndael was chosen as the AES
- AES was formally approved as a US federal standard in November 2001

AES Overview

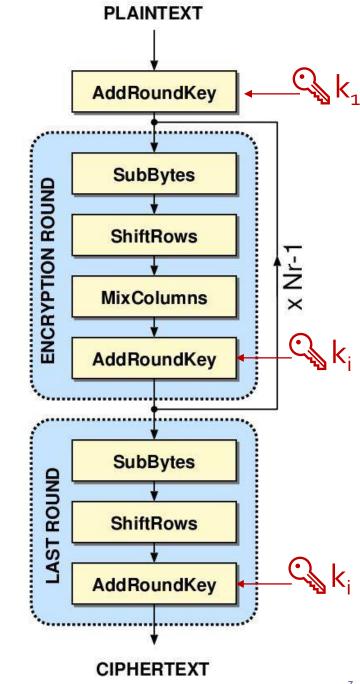


The number of rounds depends on the chosen key length:

Key length (bits)	Number of rounds
128	10
192	12
256	14

AES Overview

- An **iterative** rather than Feistel cipher
- Operates on entire data block in every round
- 10/12/14 rounds depending on the key size.
- Each round consists of Confusion and Diffusion operations
- Note: In the last round, the MixColumns tansformation is omitted

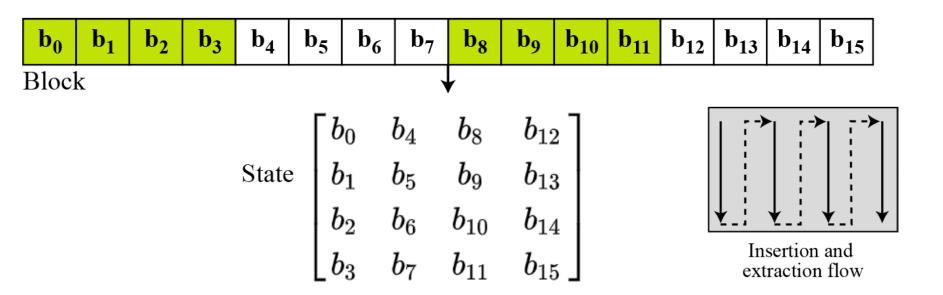


Internal structure of AES



Block to state

- AES is a byte-oriented cipher
- State = Block of bytes that are currently being worked on
- Arranged in 4 x 4 Matrix of bytes



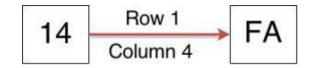
with $b_0,...,b_1$ denoting the **16-byte** input of AES arranged in a 4x4 matrix

Block to state -example

Text	A	Е	S	U	S	Е	S	A	M	A	T	R	I	X	Z	Z
Hexadecimal	00	04	12	14	12	04	12	00	0C	00	13	11	08	23	19	19
'							Гоо	12	0C	08						
							04		00							
								12		19		e				
							14	00	11	19						

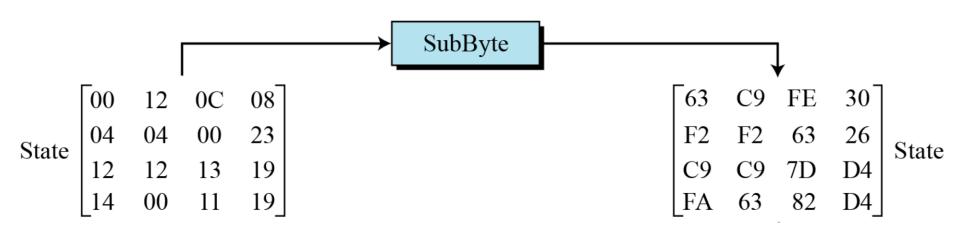
SubByte = Byte Substitution

- Each value of the state is replaced with the corresponding S-Box value
- E.g. HEX 14 would get replaced with HEX FA



	0	1	2	3	4	5	6	7	8	9	Α	В	С	D	E	F
0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	C0
2	В7	FD	93	26	36	3F	F7	СС	34	A5	E5	F1	71	D8	31	15
3	04	C7	23	СЗ	18	96	05	9A	07	12	80	E2	EB	27	B2	75
4	09	83	2C	1A	1B	6E	5A	Α0	52	3B	D6	В3	29	E3	2F	84
5	53	D1	00	ED	20	FC	B1	5B	6A	СВ	BE	39	4A	4C	58	CF
6	D0	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
7	51	А3	40	8F	92	9D	38	F5	вс	В6	DA	21	10	FF	F3	D2
8	CD	0C	13	EC	5F	97	44	17	C4	A7	7E	3D	64	5D	19	73
9	60	81	4F	DC	22	2A	90	88	46	EE	B8	14	DE	5E	0B	DB
Α	E0	32	3A	0A	49	06	24	5C	C2	D3	AC	62	91	95	E4	79
В	E7	C8	37	6D	8D	D5	4E	A9	6C	56	F4	EA	65	7A	AE	08
С	ВА	78	25	2E	1C	A6	B4	C6	E8	DD	74	1F	4B	BD	8B	8A
D	70	3E	B5	66	48	03	F6	0E	61	35	57	В9	86	C1	1D	9E
E	E1	F8	98	11	69	D9	8E	94	9B	1E	87	E9	CE	55	28	DF
F	8C	A1	89	0D	BF	E6	42	68	41	99	2D	0F	В0	54	ВВ	16

SubByte Example



Shift rows

- Performs Left Circular Shift of the state matrix row:
- This is not a bit wise shift. The circular shift just moves each byte one space over.

Input matrix

B_0	B_4	B_8	B ₁₂
B_1	B_5	B_9	B ₁₃
B_2	B_6	B ₁₀	B ₁₄
B_3	<i>B</i> ₇	B ₁₁	B ₁₅

Output matrix

B_0	B_4	<i>B</i> ₈	B ₁₂
B_5	B_9	B ₁₃	B_1
B ₁₀	B ₁₄	B_2	B_6
B ₁₅	B_3	B ₇	<i>B</i> ₁₁

- ← one position left shift
 ← two positions left shift
 ← three positions left shift

MixColumns

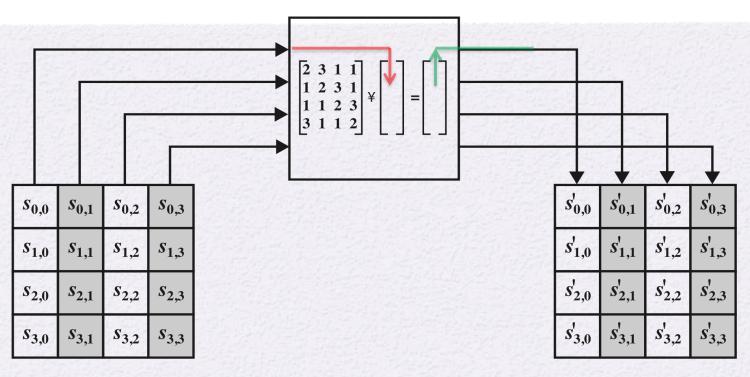
- The MixColumns transformation operates at the column level. It transforms each column of the state to a new column.
- Each 4-byte column is considered as a vector and multiplied by a fixed 4x4 matrix, e.g.,

$$\begin{pmatrix}
C_0 \\
C_1 \\
C_2 \\
C_3
\end{pmatrix} = \begin{pmatrix}
02 & 03 & 01 & 01 \\
01 & 02 & 03 & 01 \\
01 & 01 & 02 & 03 \\
03 & 01 & 01 & 02
\end{pmatrix} \cdot \begin{pmatrix}
B_0 \\
B_5 \\
B_{10} \\
B_{15}
\end{pmatrix}$$

where 01, 02 and 03 are given in hexadecimal notation

MixColumn Transformation

$$s'_{0,0} = 2 \cdot s_{0,0} + 3 \cdot s_{1,0} + 1 \cdot s_{2,0} + 1 \cdot s_{3,0}$$



- The MixColumns transformation operates at the column level. It transforms each column of the state to a new column.
- Each 4-byte column is considered as a vector and multiplied by a fixed 4x4 matrix.

Key Addition

XOR state with 128-bits of the round key

- Inputs:
 - 16-byte state matrix C
 - 16-byte subkey k_i

- Output: $C \oplus k_i$
- The subkeys are generated by the key schedule

Key Schedule

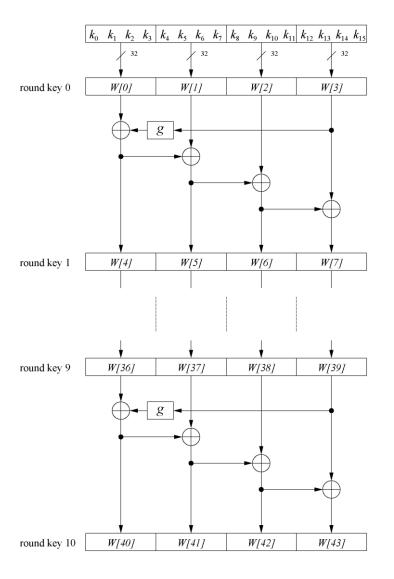
Subkeys are derived recursively from the original 128/192/256-bit input key

 Each round has 1 subkey, plus 1 subkey at the beginning of AES

Key length (bits)	Number of subkeys
128	11
192	13
256	15

Key Schedule

Example: Key schedule for 128-bit key AES



Word-oriented: 1 word = 32 bits

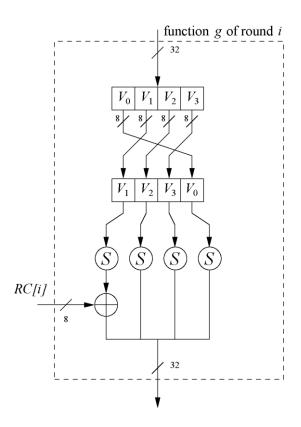
 11 subkeys are stored in W[0]...W[3], W[4]...W[7], ..., W[40]...W[43]

First subkey W[0]...W[3] is the original AES key

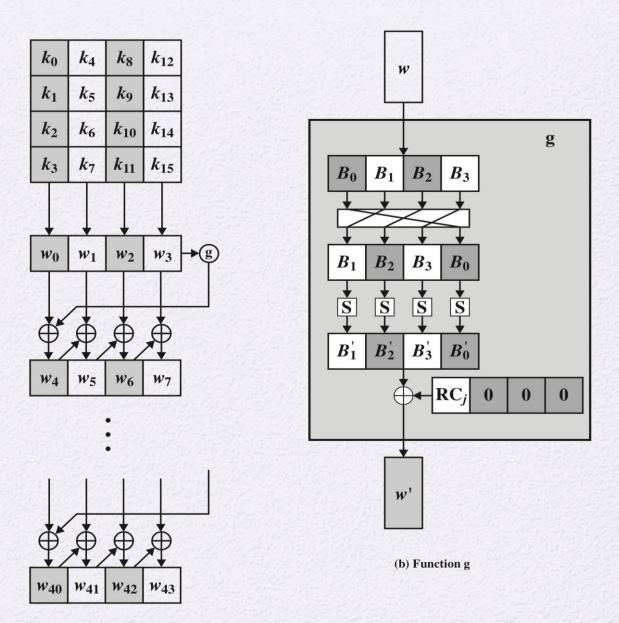
Key Schedule

- Function g rotates its four input bytes and performs a bytewise S-Box substitution
- Leftmost byte is XORed with a Round
 Coefficient (RC) constant:

Rcon Constants (Base 16)												
Round	Constant(Rcon)	Round	Constant(Rcon)									
1	01 00 00 00	6	20 00 00 00									
2	02 00 00 00	7	40 00 00 00									
3	04 00 00 00	8	80 00 00 00									
4	08 00 00 00	9	1B 00 00 00									
5	10 00 00 00	10	36 00 00 00									



AES Key Expansion

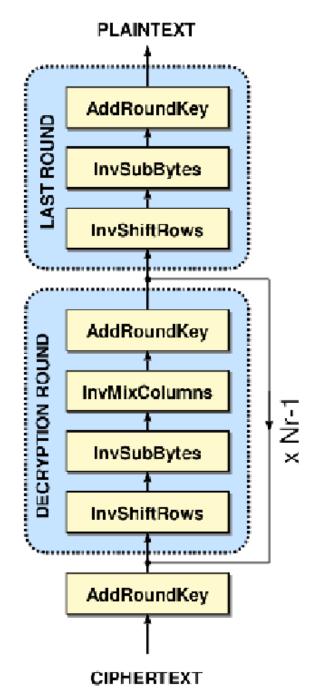


(a) Overall algorithm

Figure 5.9 AES Key Expansion

Decryption





Decryption

- AES is not based on a Feistel network
- ⇒ All layers must be inverted for decryption:
 - MixColumn layer → Inv
 MixColumn layer
 - ShiftRows layer → Inv ShiftRows
 layer
 - Byte Substitution layer → Inv
 Byte Substitution layer
 - Key Addition layer uses XOR
 - Subkeys are needed in reversed order

Inv MixColumn

 To reverse the MixColumn operation, each column of the state matrix C must be multiplied with the inverse of the 4x4 matrix, e.g.,

$$\begin{pmatrix}
B_0 \\
B_1 \\
B_2 \\
B_3
\end{pmatrix} = \begin{pmatrix}
0E & 0B & 0D & 09 \\
09 & 0E & 0B & 0D \\
0D & 09 & 0E & 0B \\
0B & 0D & 09 & 0E
\end{pmatrix} \cdot \begin{pmatrix}
C_0 \\
C_1 \\
C_2 \\
C_3
\end{pmatrix}$$

where 09, 0B, 0D and 0E are given in hexadecimal notation

Inv ShiftRows

All rows of the state matrix B are shifted to the opposite direction:

Input matrix

B_0	B_4	<i>B</i> ₈	B ₁₂
B_1	B_5	B_9	B ₁₃
B_2	B_6	B ₁₀	B ₁₄
B_3	<i>B</i> ₇	B ₁₁	B ₁₅

Output matrix

B_0	B_4	<i>B</i> ₈	B ₁₂
B ₁₃	B_1	B_5	B_9
B ₁₀	B ₁₄	B_2	B_6
B ₇	B ₁₁	B ₁₅	B_3

no shift

- → one position right shift
 → two positions right shift
 → three positions right shift

InvSubByte

- During decryption each value in the state is replaced with the corresponding inverse of the S-Box
- For example HEX D4 would get replaced with HEX 19

		У															
		0	1	2	3	4	5	6	7	8	9	a	b	С	d	е	f
	0	52	09	6a	d5	30	36	a5	38	bf	40	a3	9e	81	f3	d7	fb
- 60	1	7c	e 3	39	82	9b	2f	ff	87	34	8e	43	44	c4	de	e9	cb
Ĩ	2	54	7b	94	32	a6	c2	23	3d	ee	4c	95	0b	42	fa	с3	4e
	3	08	2e	a1	66	28	d9	24	b2	76	5b	a2	49	6d	8b	d1	25
	4	72	f8	f6	64	86	68	98	16	d4	a4	5c	CC	5d	65	b6	92
	5	6c	70	48	50	fd	ed	b9	da	5e	15	46	57	a7	8d	9d	84
100	6	90	d8	ab	00	8c	bc	d3	0a	f7	e4	58	05	b8	b3	45	06
	7	d0	2c	1e	8f	ca	3f	0f	02	c1	af	bd	03	01	13	8a	6b
x	8	3a	91	11	41	4f	67	dc	ea	97	f2	cf	ce	f0	b4	e6	73
3	9	96	ac	74	22	e7	ad	35	85	e2	f9	37	e8	1c	75	df	6e
ij	a	47	f1	1a	71	1d	29	с5	89	6f	b7	62	0e	aa	18	be	1b
Ĭ	b	fc	56	3e	4b	c6	d2	79	20	9a	db	c0	fe	78	cd	5a	f4
- 23	C	1f	dd	a8	33	88	07	c7	31	b1	12	10	59	27	80	ec	5f
	d	60	51	7f	a9	19	b5	4a	0d	2d	e5	7a	9f	93	с9	9c	ef
23	е	a0	e0	3b	4d	ae	2a	f5	b0	c8	eb	bb	3c	83	53	99	61
Ĩ	f	17	2b	04	7e	ba	77	d6	26	e1	69	14	63	55	21	0c	7d

AES Security

- Brute-force attack: Due to the key length of 128,
 192 or 256 bits, a brute-force attack is not possible
- Analytical attacks: There is no known analytical attack.
- Side-channel attacks:
 - Several side-channel attacks have been published
 - Note that side-channel attacks do not attack the underlying algorithm but the implementation of it

Summary

- AES is a modern block cipher which supports three key lengths of 128, 192 and 256 bit. It provides excellent long-term security against brute-force attacks.
- AES has been studied intensively since the late 1990s and no attacks have been found.
- AES is not based on Feistel networks. Its basic operations use Galois field arithmetic and provide strong diffusion and confusion.
- AES is part of numerous open standards such as IPsec or TLS, in addition to being the mandatory encryption algorithm for US government applications. It seems likely that the cipher will be the dominant encryption algorithm for many years to come.
- AES is efficient in software and hardware.