

ONLY FOR PYTHON

For a given vector, v , of length $2N$, call `np.fft.fft` and store the coefficients in a vector V , so $V=\text{np.fft.fft}(v)$. MOST importantly the fourier coefficients, \hat{v}_k ,

$$v = \sum_{k=-(N-1)}^{N-1} \hat{v}_k e^{2\pi i k x} = \frac{a_0}{2} + \sum_1^{N-1} a_k \cos(2\pi k x) + b_k \sin(2\pi k x) \quad (1)$$

The fourier coefficients are the ordered as follows

$$V_0 = \hat{v}_0 \quad (2)$$

$$V_k = \hat{v}_k, k \in (1, N-1) \quad (3)$$

$$V_k = \hat{v}_{k-2N}, k \in (N, 2N-1) \quad (4)$$

If one were to do spectral differentiation then the coefficients $\hat{w}_k = ik\hat{v}_k$ can be obtained as follows :

$$\hat{w}_k = ikV_k, k \in (0, N-1) \quad (5)$$

$$\hat{w}_{k-2N} = i(k-2N)V_k, k \in (N, 2N-1) \quad (6)$$

if nothing works copy this:

```
ik=1j*np.hstack((np.arange(0,N),np.arange(-N,0)))*2*pi/(L)
```