

Assignment 4

Raghav Juyal - EP20BTECH11018

Download all python codes from

<https://github.com/RaghavJuyal/AI1103/blob/main/Assignment4/Codes/Assignment4.py>

and latex-tikz codes from

<https://github.com/RaghavJuyal/AI1103/tree/main/Assignment4/Assignment4.tex>

Here the initial state, representing the first roll, S_0 is:

$$S_0 = \begin{bmatrix} \frac{1}{6} \\ \frac{5}{6} \end{bmatrix}$$

For the n^{th} state we have

$$S_n = P^n \times S_0 \quad (0.0.3)$$

To get a win on the third trial we need the $(2, 1)^{th}$ position of S_2 .

$$\begin{aligned} S_2 &= P^2 \times S_0 \\ &= \begin{bmatrix} \frac{1}{216} \\ \frac{5}{216} \end{bmatrix} \end{aligned} \quad (0.0.4)$$

\therefore The required probability is $\frac{5}{216}$

QUESTION 15, GATE CS 2018

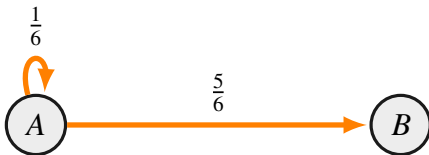
Two people, P and Q decide to independently roll two identical dice, each with 6 faces, numbered 1 to 6. The person with the lower number wins. In case of a tie, they roll the dice repeatedly until there is no tie. Define a trial as a throw of the dice by P and Q. Assume that all 6 numbers on each dice are equi-probable and that all trials are independent. The probability that one of them wins on the third trial is?

SOLUTION

Let p represent probability of a tie and q represent probability that one of them wins.

$$p = 1 \times \frac{1}{6} = \frac{1}{6} \quad (0.0.1)$$

$$q = 1 - p = \frac{5}{6} \quad (0.0.2)$$



Markov Diagram where A represents a tie and B represents that one of P and Q wins

The state transition matrix P is shown below :

$$\begin{matrix} & \begin{matrix} A & B \end{matrix} \\ \begin{matrix} A \\ B \end{matrix} & \begin{bmatrix} \frac{1}{6} & 0 \\ \frac{5}{6} & 0 \end{bmatrix} \end{matrix}$$