

2.3 Proof of Drag Translation

Step 1. Define pixel displacement

When the mouse moves from (**dragStartX**, **dragStartY**) to (**e.getX()**, **e.getY()**)

The displacement in screen coordinates is:

$$d_x = \text{dragStartX} - e.getX()$$

$$d_y = \text{dragStartY} - e.getY()$$

These are measured in pixels.

Step 2. Convert displacement into fractional ratios

Relative to screen size:

$$f_x = d_x / \text{SCREEN_WIDTH}$$

$$f_y = d_y / \text{SCREEN_HEIGHT}$$

Step 3. Convert fractions into complex-plane shift

Since the width and height of the complex window are:

$$W = x_{\max} - x_{\min}$$

$$H = y_{\max} - y_{\min}$$

the corresponding shifts in the complex plane are:

$$\Delta x = f_x \cdot W = d_x / \text{SCREEN_WIDTH} \cdot (x_{\max} - x_{\min})$$

$$\Delta y = f_y \cdot H = d_y / \text{SCREEN_HEIGHT} \cdot (y_{\max} - y_{\min})$$

Step 4. Apply translation to boundaries

For the x-axis, increasing screen dx means we move right, so:

$$x_{\min} = x_{\min} + \Delta x,$$

$$x_{\max} = x_{\max} + \Delta x$$

For the y-axis, note: **screen y grows downward**, but in the complex plane, y grows upward. Therefore, we subtract:

$$y_{\min} = y_{\min} - \Delta y$$

$$y_{\max} = y_{\max} - \Delta y$$

