1

NCERT DISCRETE

EE23BTECH11020 - Raghava Ganji*

Question 10.5.3.5: The first term of an AP is 5, the last term is 45 and the sum is 400. Find the number of terms and the common difference.

solution:

Given AP is 5, ..., 45.

x (0)	5	1st term
x(n-1)	45	nth term
s(n-1)	400	sum of n terms
n	?	no.of terms
d	?	common difference

TABLE 0
PARAMETERS

PARAMETERS

$$x(n) = x(0) + nd \tag{1}$$

$$40 = (n-1)d$$
 (2)

$$s(n) = \frac{n+1}{2} [2x(0) + nd]$$
 (3)

$$s(n-1) = \frac{n}{2} \left[2x(0) + (n-1)d \right]$$
 (4)

$$\rightarrow n = 16 \tag{5}$$

$$\to d = \frac{8}{3} \tag{6}$$

by substituting the value of n in the equation 2, we get the equation 6.

z transform of x(n), s(n) are X(z), S(z)

$$\to X(z) = \frac{7}{3(1 - z^{-1})} + \frac{8}{3(1 - z^{-1})^2} \tag{7}$$

$$\to S(z) = \frac{7}{3(1-z^{-1})^2} + \frac{8}{3(1-z^{-1})^3}$$
 (8)

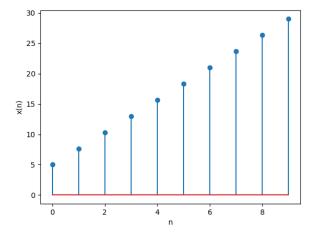


Fig. 0. figure:1