

# NCERT DISCRETE

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**Question 11.9.4.3:** Find the sum to n terms to the series  $3 \times (1)^2 + 5 \times (2)^2 + 7 \times (3)^2 + \dots$

**solution:**

Given series is  $3 \times (1)^2 + 5 \times (2)^2 + 7 \times (3)^2 + \dots$

The  $n^{th}$  term of the series can be written as  $(2n + 1) \times n^2$ .

Let us assume  $n^{th}$  term as  $X_n$ .

Therefore ,

$$X_n = (2n + 1) \times n^2 \quad (1)$$

Then,

$$\sum X_n = \sum (2n + 1) \times n^2 \quad (2)$$

$$\sum X_n = \sum 2n^3 + \sum n^2 \quad (3)$$

We know that

$$\sum n^3 = \frac{n^2 \times (n + 1)^2}{4}, \sum n^2 = \frac{n \times (n + 1) \times (2n + 1)}{6} \quad (4)$$

Then,

$$\sum X_n = \frac{n^2 \times (n + 1)^2}{2} + \frac{n \times (n + 1) \times (2n + 1)}{6} \quad (5)$$

$$\sum X_n = \frac{n \times (n + 1) \times (3n^2 + 5n + 1)}{6} \quad (6)$$

Therefore the sum to the n series to the series  $3 \times (1)^2 + 5 \times (2)^2 + 7 \times (3)^2 + \dots$  is

$$\sum X_n = \frac{n \times (n+1) \times (3n^2 + 5n + 1)}{6} \quad (6)$$