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## NCERT DISCRETE

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Question 11.9.4.3: Find the sum to n terms to the series  $3 \times (1)^2 + 5 \times (2)^2 + 7 \times (3)^2 + \dots$ 

## solution:

Given series is  $3 \times (1)^2 + 5 \times (2)^2 + 7 \times (3)^2 + \dots$ 

The  $n^{th}$  term of the series can be written as  $(2n+1) \times n^2$ .

Let us assume  $n^{th}$  term as  $X_n$ .

Therefore,

$$X_n = (2n+1) \times n^2 \tag{1}$$

Then,

$$\sum X_n = \sum (2n+1) \times n^2 \tag{2}$$

$$\sum X_n = \sum 2n^3 + \sum n^2 \tag{3}$$

We know that

$$\sum n^3 = \frac{n^2 \times (n+1)^2}{4}, \sum n^2 = \frac{n \times (n+1) \times (2n+1)}{6}$$
(4)

Then.

$$\sum X_n = \frac{n^2 \times (n+1)^2}{2} + \frac{n \times (n+1) \times (2n+1)}{6}$$
 (5)

$$\sum X_n = \frac{n \times (n+1) \times (3n^2 + 5n + 1)}{6}$$
 (6)

Therefore the sum to the n series to the series  $3 \times (1)^2 + 5 \times (2)^2 + 7 \times (3)^2 + \dots$  is

$$\sum X_n = \frac{n \times (n+1) \times (3n^2 + 5n + 1)}{6}$$
 (6)