1

NCERT DISCRETE

EE23BTECH11020 - Raghava Ganji*

Question 10.5.3.5: The first term of an AP is 5, the last term is 45 and the sum is 400. Find the number of terms and the common difference.

solution:

Given AP is 5, ..., 45.

x(0)	5	1st term
x(n)	45	(n+1)th term
y(n)	400	sum of $(n + 1)$ terms
n+1	?	no.of terms
d	?	common difference

TABLE 0

PARAMETERS

$$x(n) = x(0) + nd$$

$$40 = nd$$
(1)

$$40 = nd$$

$$y(n) = \frac{n+1}{2} [2x(0) + nd]$$

$$\implies n = 15$$
 (2)

$$\implies d = \frac{8}{3} \tag{3}$$

by substituting equation (2) in the equation (1), we get the equation (3).

z transform of x(n), y(n) are X(z), Y(z)

$$X(z) = \frac{7}{3(1 - z^{-1})} + \frac{8}{3(1 - z^{-1})^2}$$
$$Y(z) = \frac{7}{3(1 - z^{-1})^2} + \frac{8}{3(1 - z^{-1})^3}$$

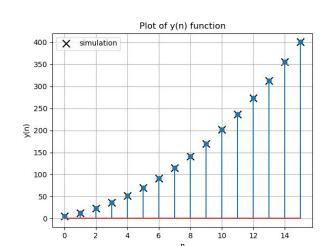


Fig. 0. simulation vs analysis of y(n)

Fig. 0. analysis of x(n)