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NCERT DISCRETE

EE23BTECH11020 - Raghava Ganji*

Question 11.9.4.3: Find the sum to n terms to the series $3(1)^2 + 5(2)^2 + 7(3)^2 + ...$

Solution:

Given series is $3(1)^2 + 5(2)^2 + 7(3)^2 + \dots$

x(0)	3	1st term
x(n)	?	(n+1)th term
y(n-1)	?	sum of n terms
TABLE 0		
PARAMETERS		

$$x(n) = (2n+3)(n+1)^2$$
 (1)

$$y(n) = x(n) * u(n)$$
 (2)

$$Y(z) = X(z) U(z)$$
 (3)

$$X(z) = \frac{3 + 8z^{-1} + z^{-2}}{(1 - z^{-1})^4} \tag{4}$$

$$U(z) = \frac{1}{1 - z^{-1}} \tag{5}$$

$$\implies Y(z) = \frac{3 + 8z^{-1} + z^{-2}}{(1 - z^{-1})^5} \tag{6}$$



$$y(n) = \frac{1}{2\pi j} \oint_C \frac{\left(3 + 8z^{-1} + z^{-2}\right)z^{n-1}}{\left(1 - z^{-1}\right)^5} dz$$

$$y(n) = \lim_{z \to 1} \frac{1}{4!} \frac{d^4}{dz^4} \frac{3z^{n-1} + 8z^{n-2} + z^{n-3}}{(1 - z^{-1})^5} \left(1 - z^{-1}\right)^{5g} \cdot 0. \text{ simulation vs analysis of } y(n)$$
(7)

$$\implies y(n) = \frac{(n+1)(n+2)(3n^2+11n+9)}{6}$$
 (8)

$$\implies y(n-1) = \frac{n(n+1)(3n^2 + 5n + 1)}{6}$$
 (9)

