NCERT ANALOG

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question 11.15.2: A stone dropped from the top of a tower of height 300 m splashes into the water of a pond near the base of the tower. When is the splash heard at the top given that the speed of the sound in air is 340 m s^{-1} .(g=9.8 m s^{-2})

solution:

Given the height of the tower s=300 m, acceleration a=+g (because the stone is moving down).

Assume speed of the sound in air is V, initial velocity of the stone is $u = 0ms^{-1}$.

S	g	V	u
300m	$9.8ms^{-2}$	$340ms^{-1}$	$0ms^{-1}$

Table 1: Given inputs

For finding the time from droping the stone to hitting the water by using kinematics 2D the formula of displacement

$$s = ut + \frac{1}{2}a(t)^2 \tag{1}$$

by substituting the values of s, a, u in the equation 1

$$300 = (0)t + \frac{1}{2}9.8(t)^2 \tag{2}$$

$$600 = 9.8(t)^2 \tag{3}$$

by solving the above equation we get

$$t = \frac{10\sqrt{30}}{7}s\tag{4}$$

Given that the speed of the sound V=340 m s^{-1}

After the hitting of the stone to the water, the sound of the splash travels with the speed V to the top of the tower of height s.

Time taken by the sound to travel to top of the tower is

$$t = \frac{s}{V} \tag{5}$$

by substituting the values of V, s in the equation 5, we get

$$t = \frac{300}{340}s\tag{6}$$

$$t = \frac{15}{17}s\tag{7}$$

The splash heard at the top of the tower after droping the stone from the top of the tower is

$$t = \left[\frac{10\sqrt{30}}{7} + \frac{15}{17}\right]s\tag{8}$$