

(%i1) load('clifford);

package name: clifford.mac

author:

Dimiter Prodanov

version:

v20

Recommended location: share/contrib

last update: 20 June 2016

(%o1)

"C:/Dropbox/maxima/clifford.mac"

(%i2) clifford(e,3);

[1, 1, 1]

(%o2)

(%i3) EE:cons(1, %elements);

[1, e₁, e₂, e₃, e₁.e₂, e₁.e₃, e₂.e₃, e₁.e₂.e₃]

(EE)

Cl(3,0,0)

(%i4) mtablelo(%elements);

$$\begin{pmatrix} 1 & e_1 & e_2 & e_3 & e_1.e_2 & e_1.e_3 & e_2.e_3 & e_1.e_2.e_3 \\ e_1 & 0 & e_1.e_2 & e_1.e_3 & 0 & 0 & e_1.e_2.e_3 & 0 \\ e_2 & -e_1.e_2 & 0 & e_2.e_3 & 0 & -e_1.e_2.e_3 & 0 & 0 \\ e_3 & -e_1.e_3 & -e_2.e_3 & 0 & e_1.e_2.e_3 & 0 & 0 & 0 \\ e_1.e_2 & 0 & 0 & e_1.e_2.e_3 & 0 & 0 & 0 & 0 \\ e_1.e_3 & 0 & -e_1.e_2.e_3 & 0 & 0 & 0 & 0 & 0 \\ e_2.e_3 & e_1.e_2.e_3 & 0 & 0 & 0 & 0 & 0 & 0 \\ e_1.e_2.e_3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

(%o4)

(%i5) mtable1i(%elements);

$$\begin{pmatrix} 1 & e_1 & e_2 & e_3 & e_1.e_2 & e_1.e_3 & e_2.e_3 & e_1.e_2.e_3 \\ e_1 & 1 & 0 & 0 & e_2 & e_3 & 0 & e_2.e_3 \\ e_2 & 0 & 1 & 0 & -e_1 & 0 & e_3 & -e_1.e_3 \\ e_3 & 0 & 0 & 1 & 0 & -e_1 & -e_2 & e_1.e_2 \\ e_1.e_2 & -e_2 & e_1 & 0 & -1 & 0 & 0 & -e_3 \\ e_1.e_3 & -e_3 & 0 & e_1 & 0 & -1 & 0 & e_2 \\ e_2.e_3 & 0 & -e_3 & e_2 & 0 & 0 & -1 & -e_1 \\ e_1.e_2.e_3 & e_2.e_3 & -e_1.e_3 & e_1.e_2 & -e_3 & e_2 & -e_1 & -1 \end{pmatrix} \quad (%o5)$$

(%i6) mtable2();

$$\begin{pmatrix} 1 & e_1 & e_2 & e_3 & e_1.e_2 & e_1.e_3 & e_2.e_3 & e_1.e_2.e_3 \\ e_1 & 1 & e_1.e_2 & e_1.e_3 & e_2 & e_3 & e_1.e_2.e_3 & e_2.e_3 \\ e_2 & -e_1.e_2 & 1 & e_2.e_3 & -e_1 & -e_1.e_2.e_3 & e_3 & -e_1.e_3 \\ e_3 & -e_1.e_3 & -e_2.e_3 & 1 & e_1.e_2.e_3 & -e_1 & -e_2 & e_1.e_2 \\ e_1.e_2 & -e_2 & e_1 & e_1.e_2.e_3 & -1 & -e_2.e_3 & e_1.e_3 & -e_3 \\ e_1.e_3 & -e_3 & -e_1.e_2.e_3 & e_1 & e_2.e_3 & -1 & -e_1.e_2 & e_2 \\ e_2.e_3 & e_1.e_2.e_3 & -e_3 & e_2 & -e_1.e_3 & e_1.e_2 & -1 & -e_1 \\ e_1.e_2.e_3 & e_2.e_3 & -e_1.e_3 & e_1.e_2 & -e_3 & e_2 & -e_1 & -1 \end{pmatrix} \quad (%o6)$$

Cl(1,1,1)

(%i7) clifford(e,1,1,1);

$$[1, -1, 0] \quad (%o7)$$

(%i8) mtable1o(%elements);

$$\begin{pmatrix} 1 & e_1 & e_2 & e_3 & e_1.e_2 & e_1.e_3 & e_2.e_3 & e_1.e_2.e_3 \\ e_1 & 0 & e_1.e_2 & e_1.e_3 & 0 & 0 & e_1.e_2.e_3 & 0 \\ e_2 & -e_1.e_2 & 0 & e_2.e_3 & 0 & -e_1.e_2.e_3 & 0 & 0 \\ e_3 & -e_1.e_3 & -e_2.e_3 & 0 & e_1.e_2.e_3 & 0 & 0 & 0 \\ e_1.e_2 & 0 & 0 & e_1.e_2.e_3 & 0 & 0 & 0 & 0 \\ e_1.e_3 & 0 & -e_1.e_2.e_3 & 0 & 0 & 0 & 0 & 0 \\ e_2.e_3 & e_1.e_2.e_3 & 0 & 0 & 0 & 0 & 0 & 0 \\ e_1.e_2.e_3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix} \quad (%o8)$$

(%i9) mtable1i(%elements);

$$\begin{pmatrix} 1 & e_1 & e_2 & e_3 & e_1.e_2 & e_1.e_3 & e_2.e_3 & e_1.e_2.e_3 \\ e_1 & 1 & 0 & 0 & e_2 & e_3 & 0 & e_2.e_3 \\ e_2 & 0 & -1 & 0 & e_1 & 0 & -e_3 & e_1.e_3 \\ e_3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ e_1.e_2 & -e_2 & -e_1 & 0 & 1 & 0 & 0 & e_3 \\ e_1.e_3 & -e_3 & 0 & 0 & 0 & 0 & 0 & 0 \\ e_2.e_3 & 0 & e_3 & 0 & 0 & 0 & 0 & 0 \\ e_1.e_2.e_3 & e_2.e_3 & e_1.e_3 & 0 & e_3 & 0 & 0 & 0 \end{pmatrix} \quad (%o9)$$

(%i10) mtable2();

$$\begin{pmatrix} 1 & e_1 & e_2 & e_3 & e_1.e_2 & e_1.e_3 & e_2.e_3 & e_1.e_2.e_3 \\ e_1 & 1 & e_1.e_2 & e_1.e_3 & e_2 & e_3 & e_1.e_2.e_3 & e_2.e_3 \\ e_2 & -e_1.e_2 & -1 & e_2.e_3 & e_1 & -e_1.e_2.e_3 & -e_3 & e_1.e_3 \\ e_3 & -e_1.e_3 & -e_2.e_3 & 0 & e_1.e_2.e_3 & 0 & 0 & 0 \\ e_1.e_2 & -e_2 & -e_1 & e_1.e_2.e_3 & 1 & -e_2.e_3 & -e_1.e_3 & e_3 \\ e_1.e_3 & -e_3 & -e_1.e_2.e_3 & 0 & e_2.e_3 & 0 & 0 & 0 \\ e_2.e_3 & e_1.e_2.e_3 & e_3 & 0 & e_1.e_3 & 0 & 0 & 0 \\ e_1.e_2.e_3 & e_2.e_3 & e_1.e_3 & 0 & e_3 & 0 & 0 & 0 \end{pmatrix} \quad (%o10)$$

Cl(0,2,1)

(%i11) clifford(e,0,2,1);

$$[-1, -1, 0] \quad (%o11)$$

(%i12) mtable1o(%elements);

$$\begin{pmatrix} 1 & e_1 & e_2 & e_3 & e_1.e_2 & e_1.e_3 & e_2.e_3 & e_1.e_2.e_3 \\ e_1 & 0 & e_1.e_2 & e_1.e_3 & 0 & 0 & e_1.e_2.e_3 & 0 \\ e_2 & -e_1.e_2 & 0 & e_2.e_3 & 0 & -e_1.e_2.e_3 & 0 & 0 \\ e_3 & -e_1.e_3 & -e_2.e_3 & 0 & e_1.e_2.e_3 & 0 & 0 & 0 \\ e_1.e_2 & 0 & 0 & e_1.e_2.e_3 & 0 & 0 & 0 & 0 \\ e_1.e_3 & 0 & -e_1.e_2.e_3 & 0 & 0 & 0 & 0 & 0 \\ e_2.e_3 & e_1.e_2.e_3 & 0 & 0 & 0 & 0 & 0 & 0 \\ e_1.e_2.e_3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix} \quad (%o12)$$

(%i13) mtable1i(%elements);

$$\begin{pmatrix} 1 & e_1 & e_2 & e_3 & e_1.e_2 & e_1.e_3 & e_2.e_3 & e_1.e_2.e_3 \\ e_1 & -1 & 0 & 0 & -e_2 & -e_3 & 0 & -e_2.e_3 \\ e_2 & 0 & -1 & 0 & e_1 & 0 & -e_3 & e_1.e_3 \\ e_3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ e_1.e_2 & e_2 & -e_1 & 0 & -1 & 0 & 0 & -e_3 \\ e_1.e_3 & e_3 & 0 & 0 & 0 & 0 & 0 & 0 \\ e_2.e_3 & 0 & e_3 & 0 & 0 & 0 & 0 & 0 \\ e_1.e_2.e_3 & -e_2.e_3 & e_1.e_3 & 0 & -e_3 & 0 & 0 & 0 \end{pmatrix} \quad (\%o13)$$

(%i14) mtable2();

$$\begin{pmatrix} 1 & e_1 & e_2 & e_3 & e_1.e_2 & e_1.e_3 & e_2.e_3 & e_1.e_2.e_3 \\ e_1 & -1 & e_1.e_2 & e_1.e_3 & -e_2 & -e_3 & e_1.e_2.e_3 & -e_2.e_3 \\ e_2 & -e_1.e_2 & -1 & e_2.e_3 & e_1 & -e_1.e_2.e_3 & -e_3 & e_1.e_3 \\ e_3 & -e_1.e_3 & -e_2.e_3 & 0 & e_1.e_2.e_3 & 0 & 0 & 0 \\ e_1.e_2 & e_2 & -e_1 & e_1.e_2.e_3 & -1 & e_2.e_3 & -e_1.e_3 & -e_3 \\ e_1.e_3 & e_3 & -e_1.e_2.e_3 & 0 & -e_2.e_3 & 0 & 0 & 0 \\ e_2.e_3 & e_1.e_2.e_3 & e_3 & 0 & e_1.e_3 & 0 & 0 & 0 \\ e_1.e_2.e_3 & -e_2.e_3 & e_1.e_3 & 0 & -e_3 & 0 & 0 & 0 \end{pmatrix} \quad (\%o14)$$