

# from the discrete to the continuous

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0, 1, 2... 10



# binomial probability

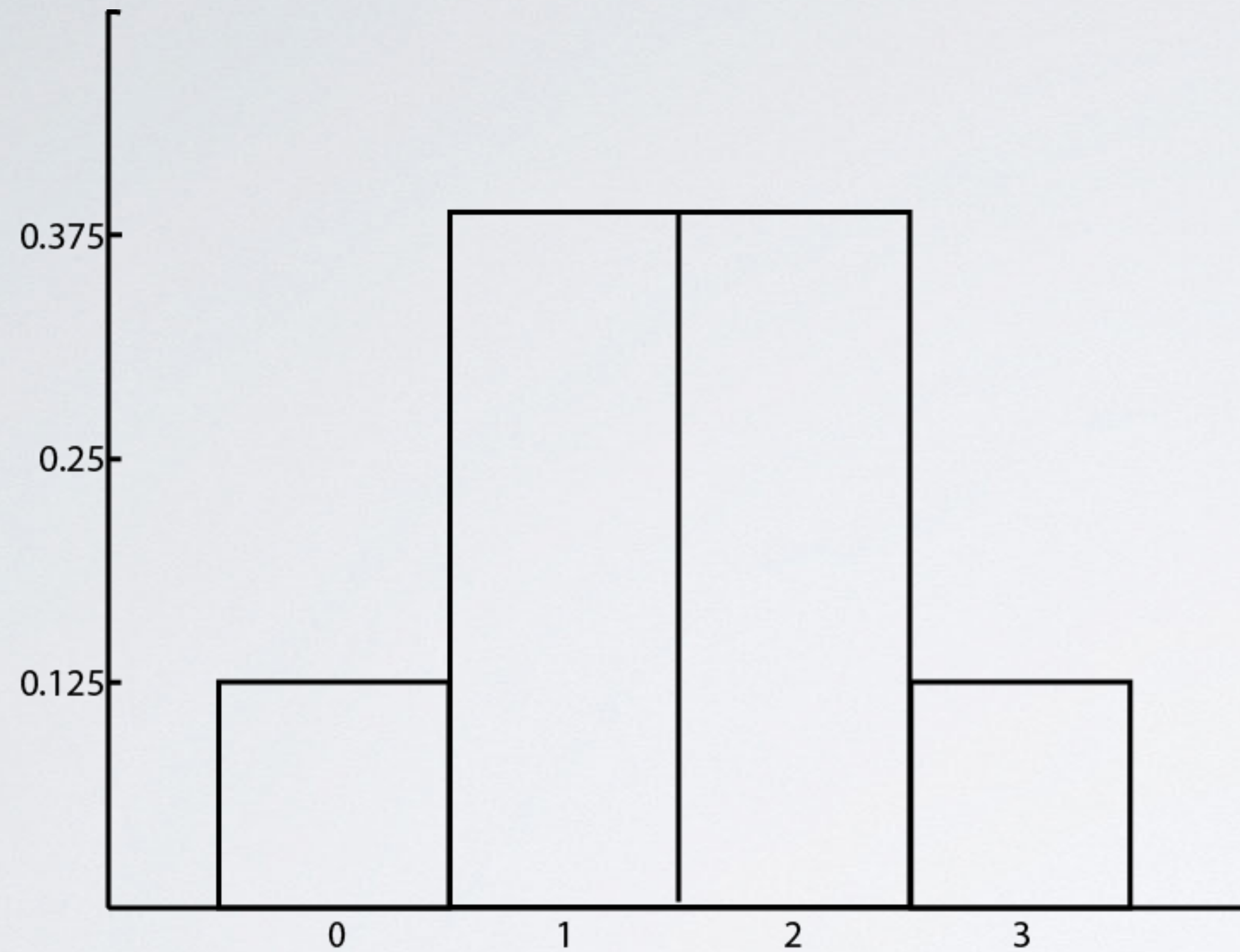
the chance of getting  $k$  heads in  $n$  tosses  
when the probability of heads is  $p$

$$P[X = k] = \binom{n}{k} p^k (1 - p)^{n-k}$$

↓

**probability mass function**

# probability mass function



$$P[X = k] = \binom{n}{k} p^k (1 - p)^{n-k}$$



# normal distribution

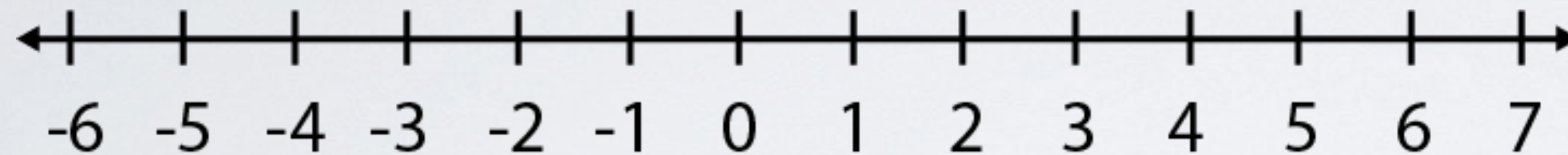
= Gaussian distribution

= bell-shaped curve

$-\infty$  —————  $\infty$   
|—————|  
continuous random variable

# random variables

**discrete random variables** can only take values at separated points

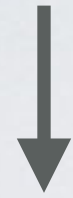


**continuous random variables** can take any value within an interval





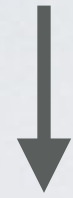
# continuous random variable



# probability mass function

[illegible]

# discrete random variable

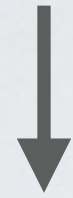


# probability mass function

[illegible]



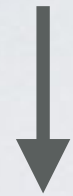
continuous random variable



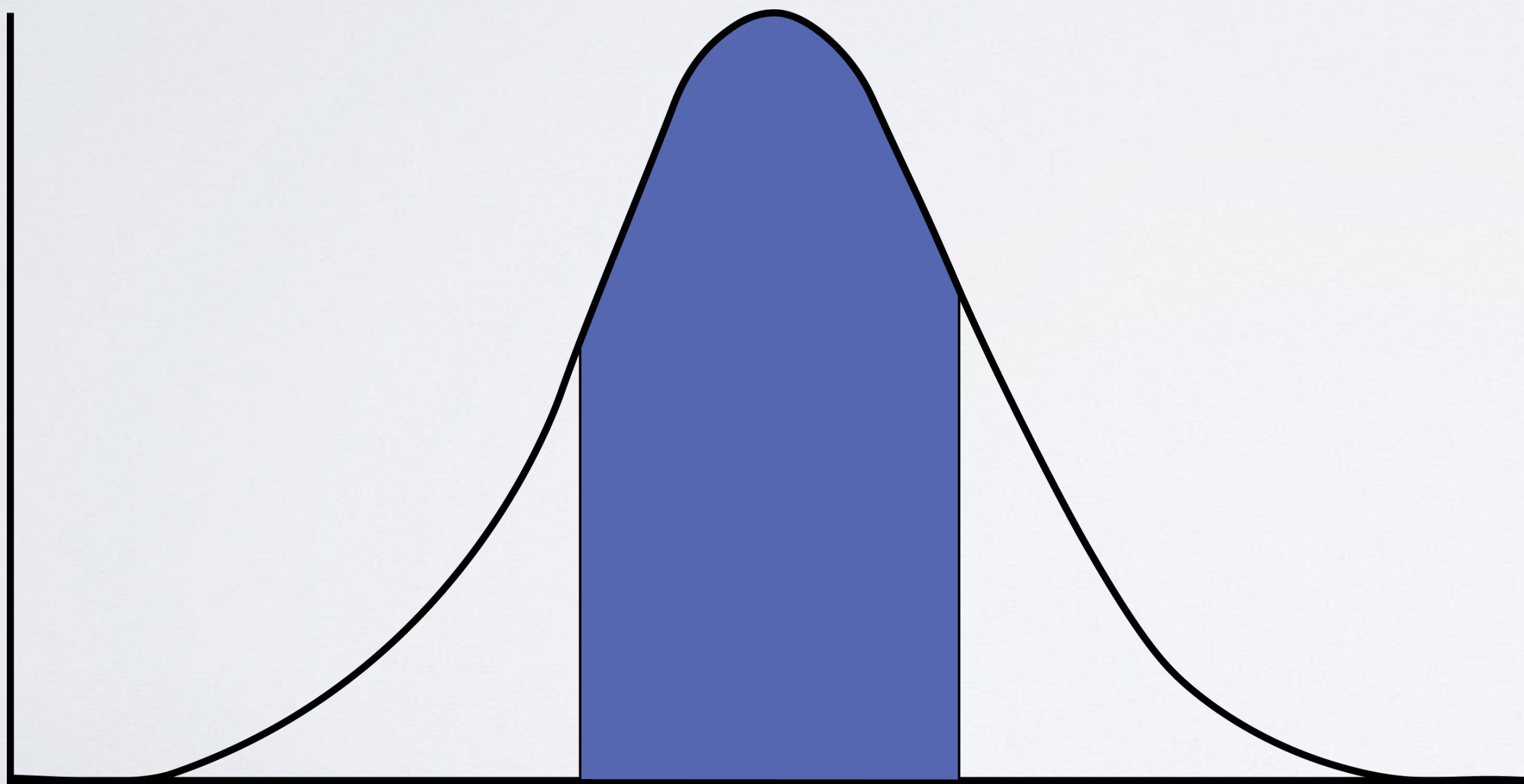
probability mass function

**P** [height = (5'11": 6'1")]

continuous random variable



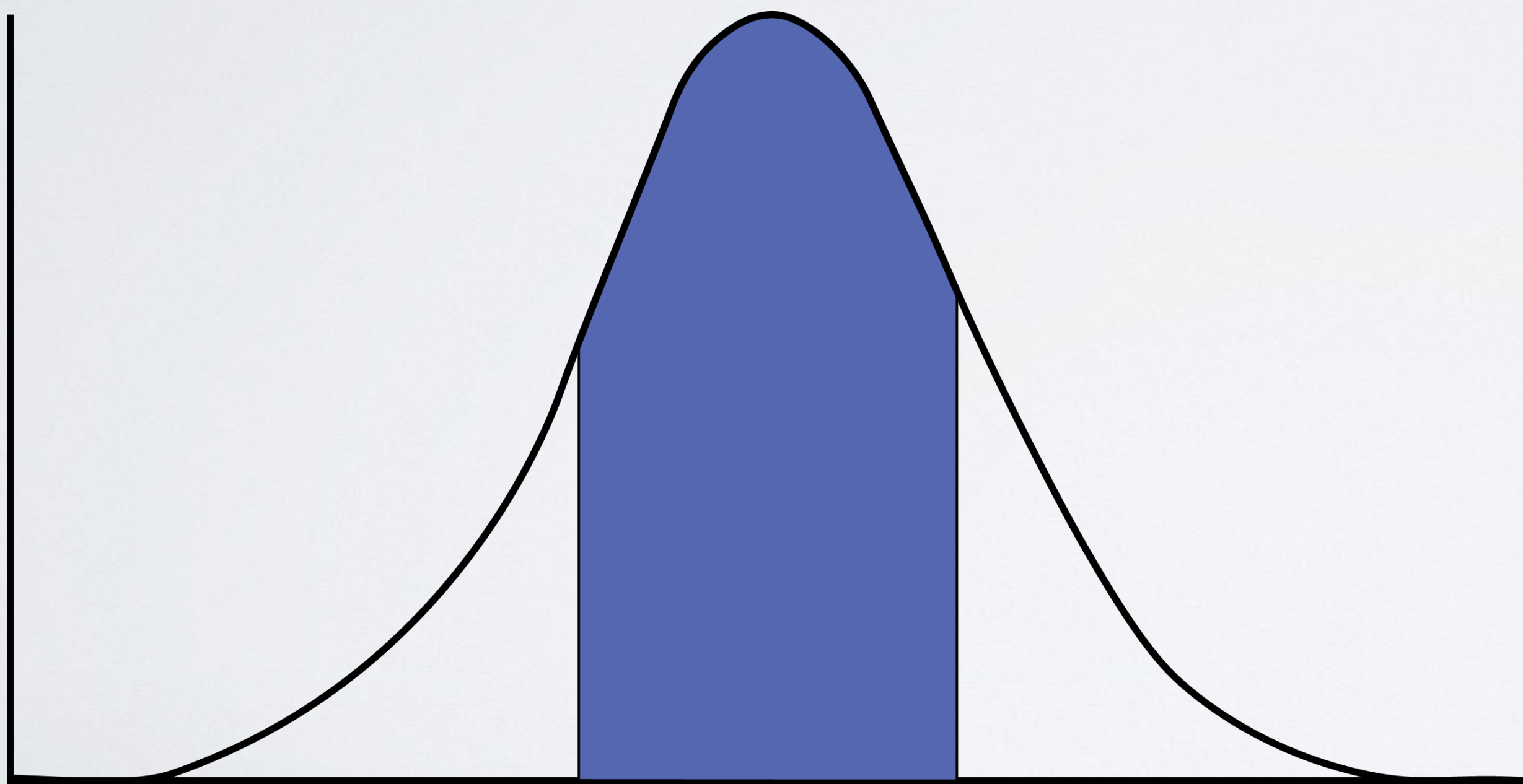
probability density function





continuous random variable

↓  
pdf



the pdf for a random variable  $\mathbf{X}$  from a normal distribution with mean  $\boldsymbol{\mu}$  and standard deviation  $\boldsymbol{\sigma}$

$$f(x) = \frac{1}{\sqrt{2\pi}} \frac{1}{\sigma} e^{\left[-\frac{1}{2\sigma^2} (x - \mu)^2\right]}$$



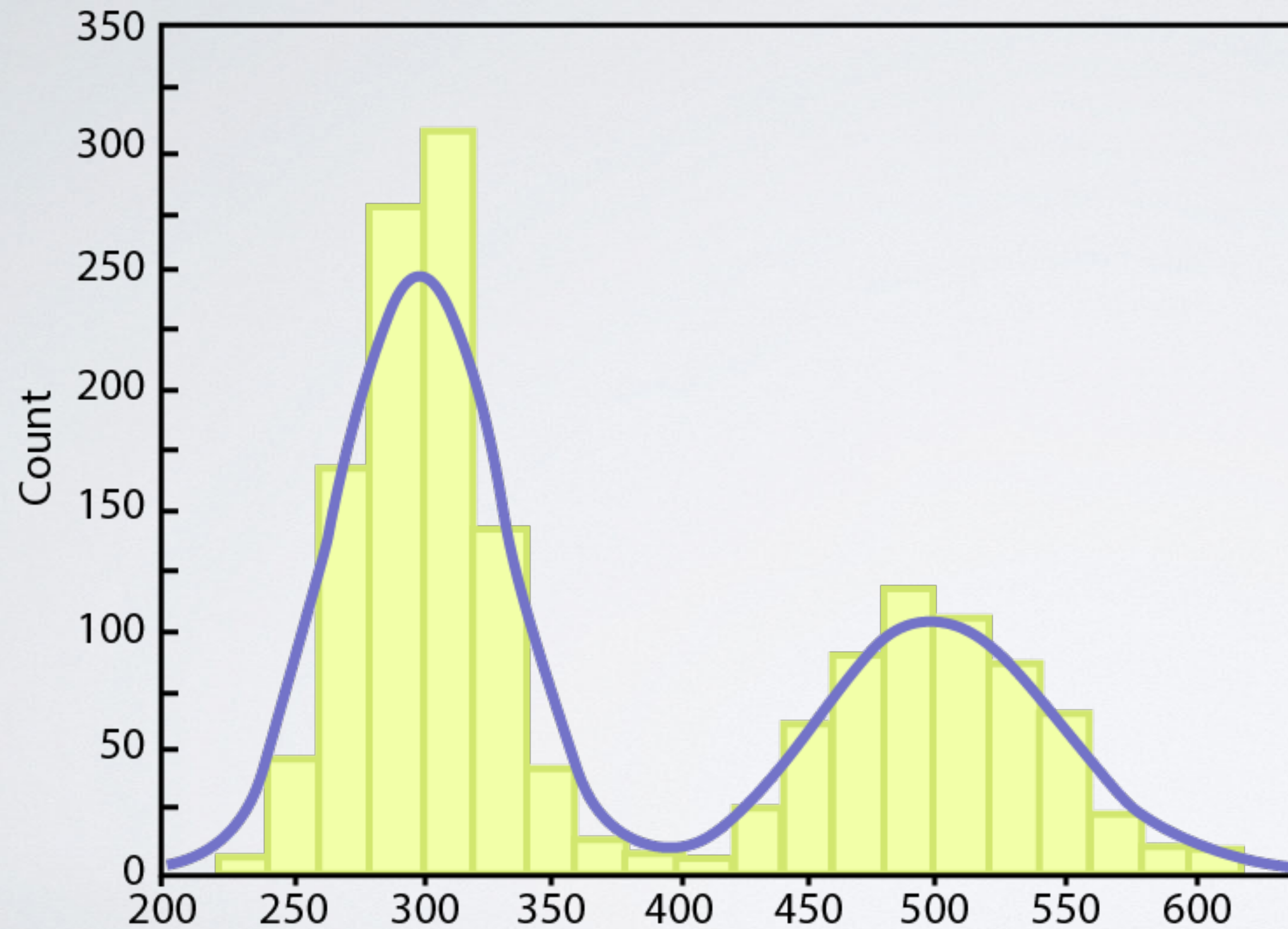
## probability **m**ass **f**unction

assigns the probability that a random variable takes a specific value for the discrete set of possible values. the sum of those probabilities over all possible values must equal one

## probability **d**ensity **f**unction

any function of  $x$  that is non-negative and which has area one underneath its curve

# probability density function





# important distributions

- ▶ continuous
  - ▶ normal
  - ▶ uniform
  - ▶ beta
  - ▶ gamma
- ▶ discrete
  - ▶ binomial
  - ▶ Poisson

## summary

1. continuous random variables can take **any value in a range**
2. the probability that a continuous random variable takes a specific value is **zero**
3. its probabilities are determined by a **pdf**, which is non-negative and the area under the curve is equal to one
4. the probability that it lies between  $c$  and  $d$  is the **area under the pdf** between  $c$  and  $d$