Artificial Intelligence & Machine Learning

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Lecture 6

Local Search

- Mostly we have to search in the solution space instead of state space, and optimize an objective function.
- Proceed through nearby solutions.

Hill-climbing search

```
function HILL-CLIMBING( problem) returns a state that is a local maximum  \begin{array}{l} \text{current} \leftarrow \text{MAKE-NODE}(\text{problem.INITIAL-STATE}) \\ \text{loop do} \\ \text{neighbor} \leftarrow \text{a highest-valued successor of current} \\ \text{if neighbor.VALUE} \leq \text{current.VALUE then return} \\ \text{current.STATE} \\ \text{current} \leftarrow \text{neighbor} \end{array}
```

Hill-climbing search

- Stochastic hill climbing chooses at random from among the uphill moves.
- ► First-choice hill climbing implements stochastic hill climbing by generating successors randomly until one is generated that is better than the current state.
- Random-restart hill climbing adopts the well-known saying, "If at first you don't succeed, try, try again."

Simulated annealing

```
function SIMULATED -ANNEALING(problem, schedule) returns a
solution state
  inputs: problem,
      schedule, a mapping from time to "temperature"
  current ← MAKE -NODE(problem.INITIAL-STATE)
  for t = 1 to \infty do
    T \leftarrow schedule(t)
    if T = 0 then return current
    next \leftarrow a randomly selected successor of current
    \Delta E \leftarrow \text{next.VAI UE} - \text{current.VAI UE}
    if \Delta E > 0 then current \leftarrow next
    else current \leftarrow next only with probability e^{\Delta E/T}
```

Simulated annealing

The innermost loop of the simulated-annealing algorithm is quite similar to hill climbing. Instead of picking the best move, however, it picks a random move. If the move improves the situation, it is always accepted. Otherwise, the algorithm accepts the move with some probability less than 1. The probability decreases exponentially with the "badness" of the move—the amount ΔE by which the evaluation is worsened. The probability also decreases as the "temperature" T goes down: "bad" moves are more likely to be allowed at the start when T is high, and they become more unlikely as T decreases. If the schedule lowers T slowly enough, the algorithm will find a global optimum with probability approaching 1.

Genetic algorithm

```
function GENETIC -ALGORITHM(population, FITNESS -FN)
returns an individual
 inputs: population, a set of individuals
     FITNESS -FN, a function that measures the fitness of an
individual repeat
   new population \leftarrow empty set
   for i = 1 to SIZE(population) do
     x ← RANDOM -SELECTION (population, FITNESS -FN)
     y ← RANDOM -SELECTION ( population , FITNESS -FN)
     child \leftarrow REPRODUCE (x , y)
     if (small random probability) then child \leftarrow MUTATE(child)
     add child to new population
population ← new population
until some individual is fit enough, or enough time has elapsed
return the best individual in population, according to FITNESS
-FN
```

Genetic algorithm

```
function REPRODUCE (x,y) returns an individual inputs: x, y, parent individuals n \leftarrow \mathsf{LENGTH}(\mathsf{x}); \ \mathsf{c} \leftarrow \mathsf{random} \ \mathsf{number} \ \mathsf{from} \ 1 \ \mathsf{to} \ \mathsf{n} return \mathsf{APPEND}(\mathsf{SUBSTRING}(\mathsf{x},1,\mathsf{c}), \ \mathsf{SUBSTRING}(\mathsf{y}, \ \mathsf{c}+1, \ \mathsf{n}))
```