

Assignment

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Q1. $(-17)_{10}$

i) In sign magnitude: 101001

$$\begin{array}{r} 2 \overline{) 17} - 1 \\ 2 \overline{) 8} - 0 \\ 2 \overline{) 4} - 0 \\ 2 \overline{) 2} - 1 \\ \underline{1} \end{array}$$

ii) one's complement $\rightarrow 010111$

iii) two's complement $\rightarrow 010111 + 1$

$$= 011000$$

Q2.

$$-48 \rightarrow 1001111 + 1 = 1010000$$

$$-23 \rightarrow 101000 + 1 = 101001$$

$$\begin{array}{r} \cancel{1001111} \\ \cancel{101000} \\ -48 - 23 = \begin{array}{r} 1010000 \\ 101001 \\ + \\ \hline 1111001 \end{array} \\ \text{discarded} \end{array}$$

Ans: ~~1001~~ 1111001 (Ans)

Q3 a) $0110 \rightarrow 2^2 + 2^1 = 6$
 ~~$0111 \rightarrow 2^2 + 2^1 + 2^0 = 7$~~

So distance between BCD digit is

$$0110 \oplus 0111 = 0001$$

it contains one only therefore the distance betⁿ the codes are 1.

b) In 0110.

$$M = 4.$$

length of hamming code = $M + p$.

$$2^p \geq p + M + 1.$$

$$\Rightarrow 2^p \geq p + 5$$

$$\Rightarrow \boxed{p = 3}$$

So length = $3 + 4 = 7$.

bit position: 7 6 5 4 3 2 1.

$M_4 M_3 M_2 P_3 M_1 P_2 P_1$

0 0 1 1 2^2 0 2^1 2^0 .

$\frac{111}{7} \quad \frac{110}{6} \quad \frac{101}{5} \quad \frac{100}{4} \quad \frac{011}{3} \quad \frac{010}{2} \quad \frac{001}{1}$

For P_1 , we have to take bit position where LSB is 0 i.e. take bit ~~3~~ 3, 5, 7.

so we get $00101 = 1 + 000101$

$M_4 M_2 M_1 = 010 = \text{odd no. of ones}$

$$\text{so } P_1 = 1.$$

similarly for P_2 , take bit ~~3~~ 3, 6, 7.

$M_4 M_3 M_1 = 010$

$$\text{so } P_2 = 01$$

for P_3 , take bit 5, 6, 7.

$M_4 M_3 M_2 = 011 = \text{even no. of ones.}$

$$\text{so } P_3 = 0.$$

so Hamming code: 0110011

In 0111 0110 0001 0000 0000 0000 0000 0000

$$M = 4, P = 3.$$

bit position:

7	6	5	4	3	2	1
M_4	M_3	M_2	P_3	M_1	P_2	P_1
0	1	1	2^2	2^1	2^1	2^0

For P_1 , take, check 3, 5, 7 in posⁿ.

$$M_4 M_2 M_1 = 011 = \text{even no. of ones.}$$

$$\text{So } P_1 = 0$$

For P_2 , check 3, 6, 7 in posⁿ.

$$M_4 M_3 M_1 = 011 = \text{even no. of ones.}$$

$$\text{So } P_2 = 0$$

For P_3 , check 5, 6, 7 in posⁿ.

$$M_4 M_3 M_2 = 011 = \text{even no. of ones.}$$

$$\text{So } P_3 = 0.$$

Hamming code is: 0 1 1 0 1 0 0

So new distance betⁿ both hamming codes are: $0110011 \oplus 0110100$

$$= 0000111$$

$$\text{So difference is } 2^2 + 2^1 + 2^0 = 7 \text{ (Ans)}$$

Q4) Given no: 4096

i) Binary code: $(10000000000000)_2$

2 4096 - 0	2 64 - 0
2 2048 - 0	2 32 - 0
2 1024 - 0	2 16 - 0
2 512 - 0	2 8 - 0
2 256 - 0	2 4 - 0
2 128 - 0	2 2 - 0
2 64 - 0	

(ii) BCD code: 0100 0000 1001 0110

(iii) Excess-3 code:

$$\begin{array}{cccc} 4 & 0 & 9 & 6 \\ +3 & +3 & +3 & +3 \\ \hline 7 & 3 & 12 & 18 \\ (0111) & (0011) & (1100) & (10010) \end{array}$$

So Ans: (0111 0011 1100 10010)

(iv) Octal code: 1000

$$\begin{array}{r} 8 \overline{) 4096} - 0 \\ 8 \overline{) 512} - 0 \\ 8 \overline{) 64} - 0 \\ 8 \overline{) 8} - 1 \\ \underline{1} \end{array}$$

(v) Hex code: (1000)₁₆

Q5.

AB \ CD	00	01	11	10
00	1			1
01	1			1
11	1	1	1	1
10				

So

$$\begin{aligned} Y &= CD + A\bar{B}\bar{C} + \bar{A}\bar{B}\bar{C} \\ &= CD + \bar{B}\bar{C}(A + \bar{A}) \\ &= CD + \bar{B}\bar{C} \end{aligned}$$

Q6. a) $f(A, B, C, D) = \sum m(0, 1, 2, 3, 5, 7, 8, 9, 11, 14)$

AB \ CD	00	01	11	10
00	1			1
01	1	1		1
11	1	1	1	1
10	1		1	

So

$$Y = \bar{C}A\bar{B} + \bar{A}\bar{B} + \bar{A}BD + \bar{A}CD + C\bar{D}$$

$+ 2(0, 2, 5)$

AB

CD

	00	01	11	10
00	0 X	4	12	8
01	1	1 X	13	9
11	3	1	15	11
10	2 X	6	14	10

$$Y = \bar{A}\bar{C}D + CD$$

Q7. Design of BCD to Excess-3 code converter circuit.

BCD Code (Input)

Excer-3 Code (output)

A	B	C	D	Σ	X	Y	Z
0	0	0	0	0	0	1	1
0	0	0	1	0	1	0	0
0	0	1	0	0	1	0	1
0	0	1	1	0	1	1	0
0	1	0	0	0	1	1	1
0	1	0	1	1	0	0	0
0	1	1	0	1	0	0	1
0	1	1	1	1	0	1	0
1	0	0	0	1	0	1	1
1	0	0	1	1	1	0	0
1	0	1	0	X	X	X	X
1	0	1	1	X	X	X	X
1	1	0	0	X	X	X	X
1	1	0	1	X	X	X	X
1	1	1	0	X	X	X	X
1	1	1	1	X	X	X	X

AB \ CD	00	01	11	10
00	0	1	3	2
01	4	5	7	6
11	12	13	14	15
10	8	9	11	10

K-map for W:

AB \ CD	00	01	11	10
00	0	1	0	1
01	4	5	7	6
11	12	13	14	15
10	8	9	11	10

AB \ CD	00	01	11	10
00	0	1	3	2
01	4	5	7	6
11	12	13	14	15
10	8	9	11	10

K-map for Y:

so now

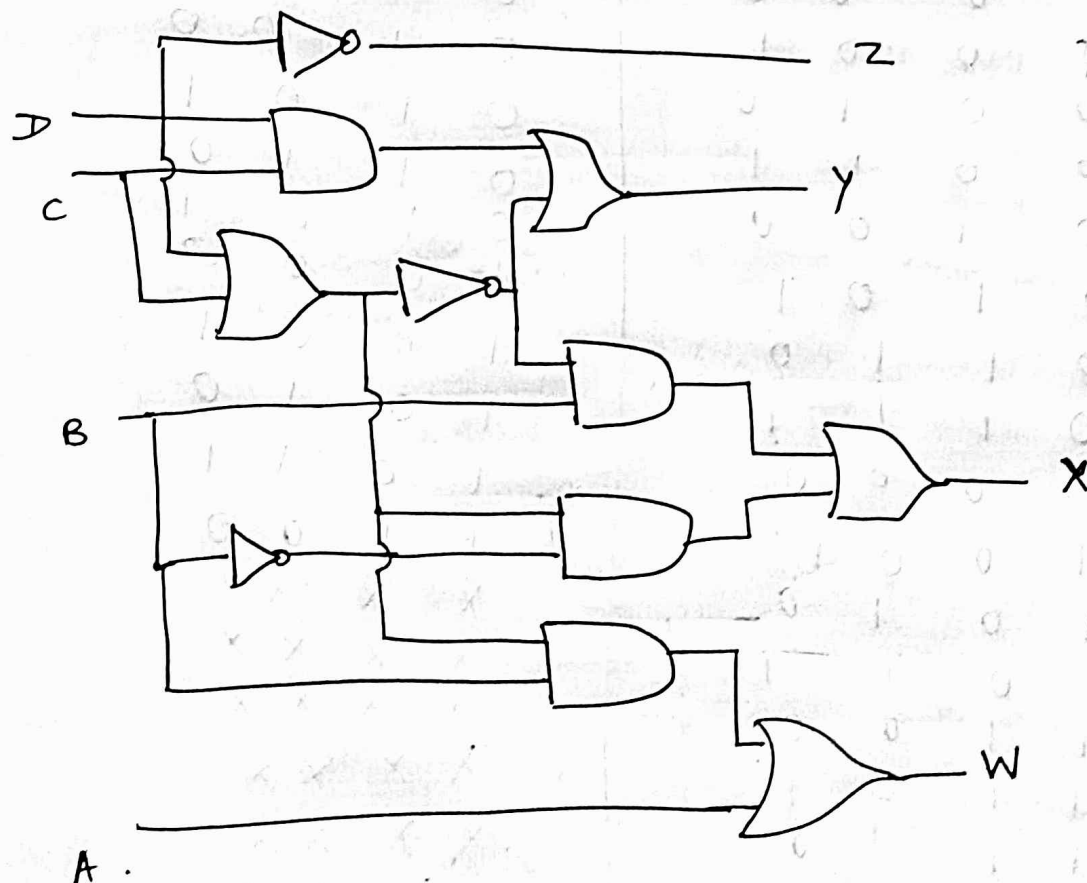
$$W = A + BC + BD$$

$$X = \bar{B}C + \bar{B}D + B\bar{C}\bar{D}$$

$$Y = CD + \bar{C}\bar{D}$$

$$Z = \bar{D}$$

so circuit diagram is:

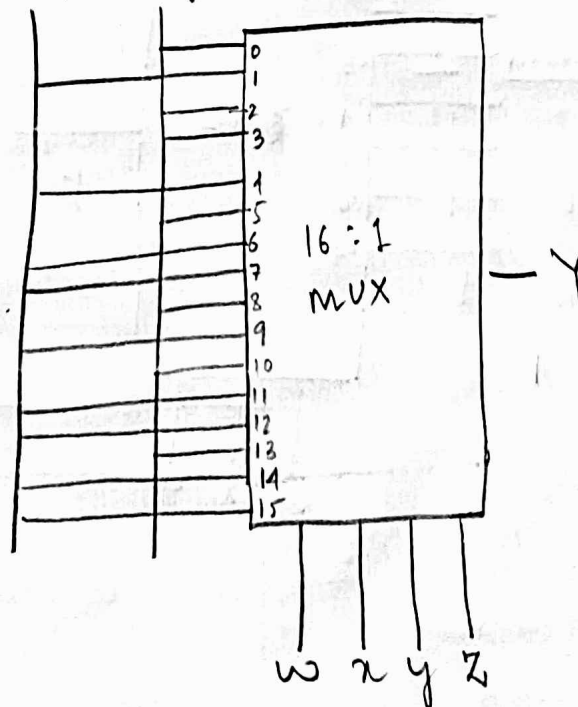


Q8. given : $f(w, x, y, z) = \sum m(1, 4, 6, 7, 9, 11, 12, 14, 15)$

	w	x	y	z	F
(0)	0	0	0	0	0
(1)	0	0	0	1	1
(2)	0	0	1	0	0
(3)	0	0	1	1	0
(4)	0	1	0	0	1
(5)	0	1	0	1	0
(6)	0	1	1	0	1
(7)	0	1	1	1	1
(8)	1	0	0	0	0
(9)	1	0	0	1	1
(10)	1	0	1	0	0
(11)	1	0	1	1	1
(12)	1	1	0	0	1
(13)	1	1	0	1	0
(14)	1	1	1	0	1
(15)	1	1	1	1	1

a)

logic1 logic0

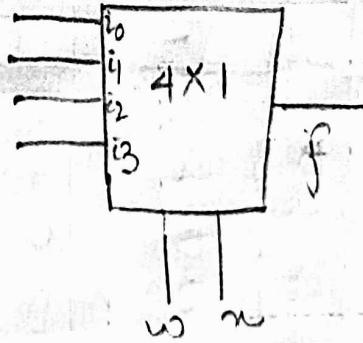


WZ

00	01	11	10
0	1	3	2
4	5	7	6
12	13	15	14
8	9	11	10

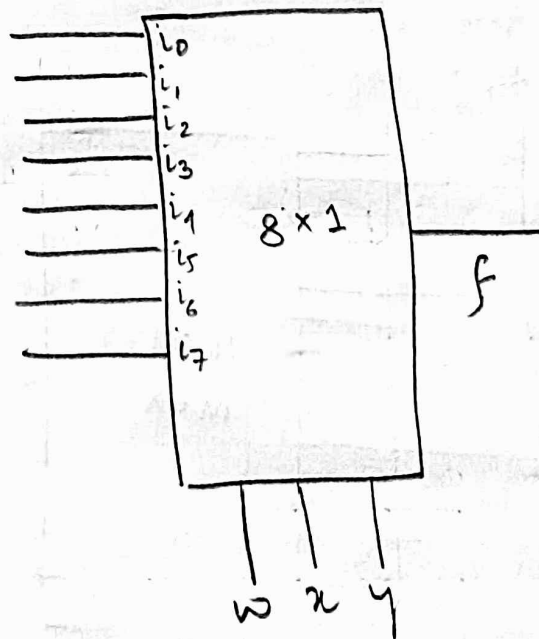
c)

w	x	Y
0	0	$z\bar{y} = i_0$
0	1	$\bar{y}\bar{z} + y = i_1$
1	0	$y\bar{z} + y = i_2$
1	1	$z = i_3$



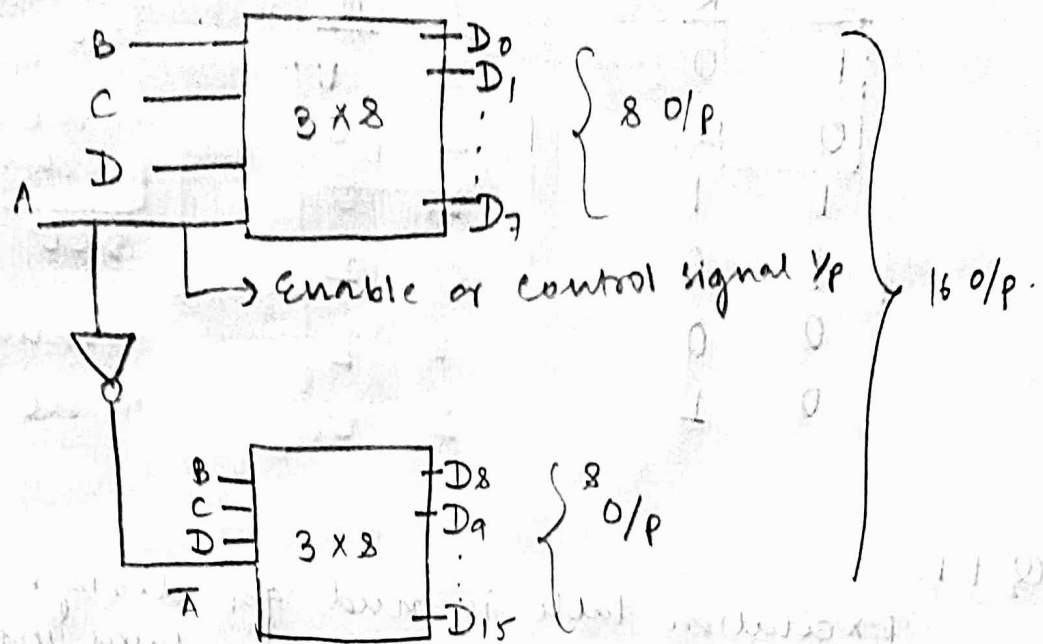
b)

w	x	y	Y
0	0	0	$i_0 = z$
0	0	1	$i_1 = 0$
0	1	0	$i_2 = \bar{z}$
0	1	1	$i_3 = z + \bar{z} = 1$
1	0	0	$i_4 = \bar{z}$
1	0	1	$i_5 = z$
1	1	0	$i_6 = \bar{z}$
1	1	1	$i_7 = z + \bar{z} = 1$



Q9.

a) 4x16 Decoder by using 3x8 decoder:

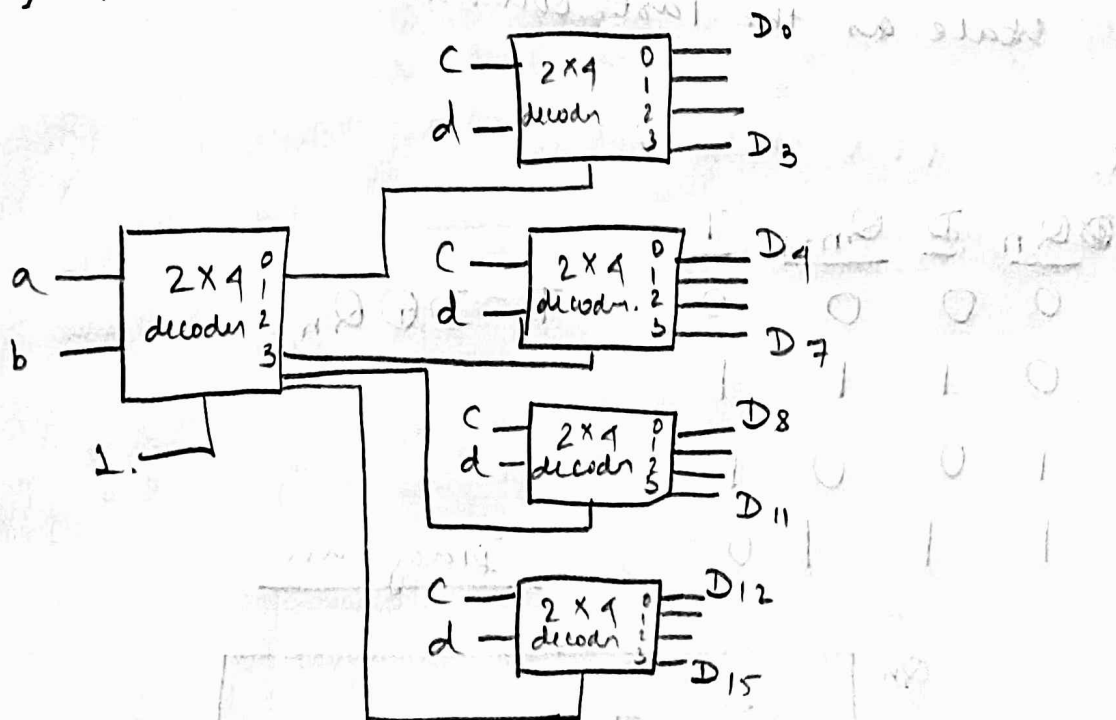


when,

A=0, 1st 3x8 decoder will operate (D₀-D₇) → o/p

A=1, 2nd 3x8 decoder will operate (D₈-D₁₅) → o/p

b) 4x16 line decoder using 2x4 line decoder:



Q 10.

<u>S</u>	<u>R</u>	<u>Outputs</u>		<u>Comments</u>
		<u>Q</u>	<u>\bar{Q}</u>	
1	0	0	1	Set
0	1	1	0	Reset.
1	1	1	0	no change
1	0	0	1	Set
0	0	1	1	invalid condition.
0	1	1	0	Reset.

Q 11.

Excitation table is used for design of flip-flop & counters. Truth table contains inputs & excitation table takes outputs as inputs.

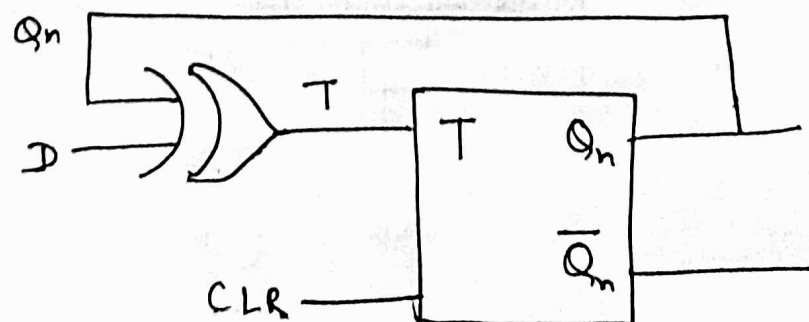
A characteristic table has the control input (D or T) as the first column, the current state as the middle column, & the next state as the last column.

Q 12.

<u>$\oplus Q_n$</u>	<u>D</u>	<u>Q_{n+1}</u>	<u>T</u>
0	0	0	0
0	1	1	1
1	0	0	1
1	1	1	0

$$T = D \oplus Q_n$$

Diagram.



Q13. "Preset" ~~means to~~ refer to forcing an output stage to a logical "1"

"Clear" refer to forcing an output stage to a logical "0".

Q14. No. of states, $N = 7$, Range: $0 - (7-1) = 0-6$
 No. of FF = $N < 2^n$ so $n = 3$

Present			Next			I/p of FF		
Q_A	Q_B	Q_C	Q_{A+1}	Q_{B+1}	Q_{C+1}	T_A	T_B	T_C
0	0	0	0	0	1	0	1	1 (6)
0	0	1	0	1	0	0	0	1 (5)
0	1	0	0	1	1	1	1	1 (4)
0	1	1	1	0	0	0	0	1 (3)
1	0	0	1	0	1	0	1	1 (2)
1	1	0	1	1	0	0	0	1 (1)
1	1	1	0	0	0	1	1	0 (0)
1	1	1	X	X	X	X	X	X (7)

A B C
 ↑ ↑
 MSB LSB.

$$T_A = \sum m(4, 0) + d(7)$$

$$T_B = \sum m(6, 4, 2, 0) + d(7)$$

$$T_C = \sum m(6, 5, 4, 3, 2, 1) + d(7)$$

Q_A	Q_B	Q_C	01	11	10
0	1				
1	1			X	

Q_A	Q_B	Q_C	00	01	11	10
0	1					1
1	1				X	1

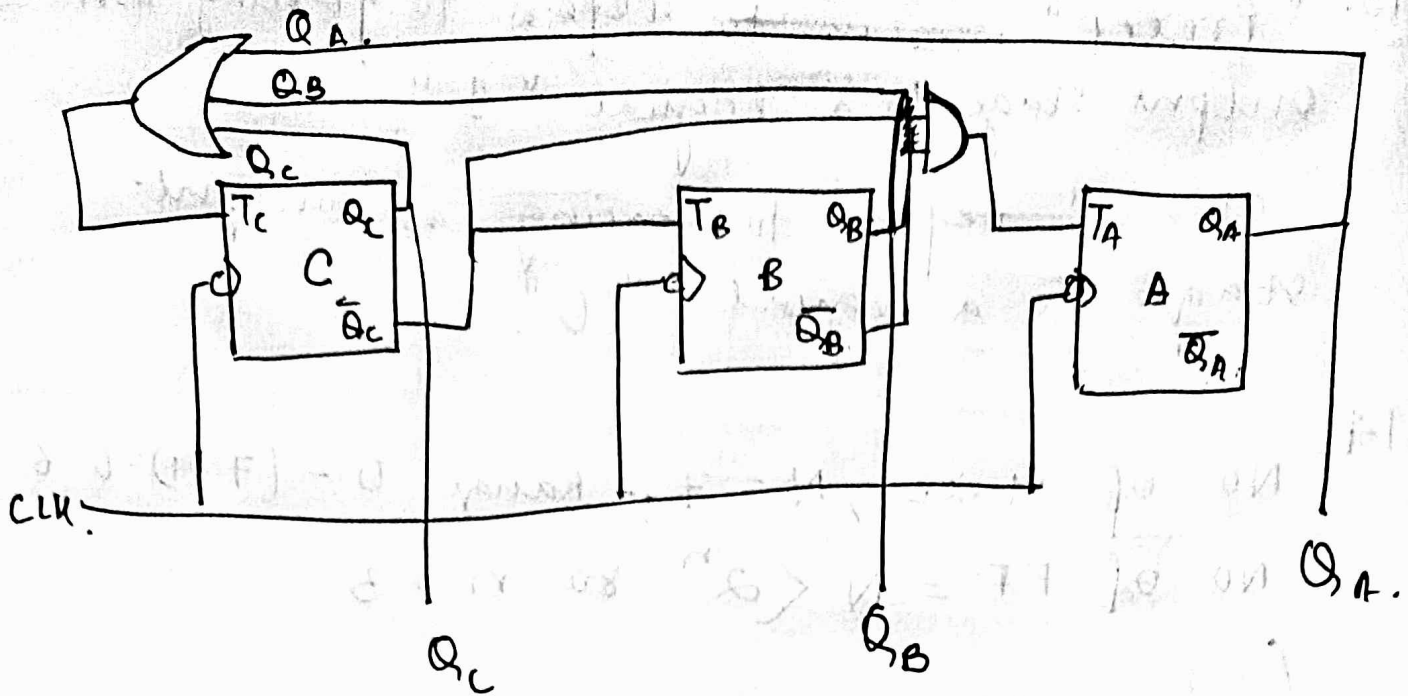
Q_A	Q_B	Q_C	00	01	11	10
0		1		1	1	
1		1		1	X	1

$$T_A = \overline{Q_B} \overline{Q_C}$$

$$T_B = \overline{Q_C}$$

$$T_C = Q_A + Q_B + Q_C$$

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Q15: $n = 5 = \text{no. of bits.}$ ($T_c = 2 \mu s$)

a) In SISO, total delay: $(2(5) - 1) T_c$
 $= 9 \times 2 = 18 \mu s$

b) In SIPO, total delay = $5 \times 2 = 10 \mu s$

c) In PISO, total delay = $(5 - 1) \times 2 = 8 \mu s.$