

## Summary of the simulation results

These results are based on, and further analyses can be carried out with the result files in the zip archive *simulation\_results.zip*.

### ***Convergence***

The convergence rate was at least 98% for all studied range combinations and values of  $Sp$  for  $n = 500$ , 99.2% for  $n = 1000$ , 99.8% for  $n = 2000$ , and 100% for  $n \geq 5000$ .

### ***Power to detect that $Y$ depends on $X$***

*Missing upper one-third of the probability range for  $Se$  and  $Y$ , and low  $Sp$  influenced the power negatively. For  $n \leq 1000$ , this resulted in power as low as 40-50%. From  $n = 2000$ , power exceeded 90% for almost all combinations of probability ranges and  $Sp$  values.*

For  $n = 500$ , the power was above 89% when the upper one-third of the probability range for  $Se$  was present. When it was missing, the power varied between 41.6% (low  $Y$ ,  $Sp \leq 0.8$ ) and 100% (whole  $Y$ ,  $Sp \geq 0.999$ ).

For  $n=1000$ , the power reached 80% for most combinations of ranges, except for low probability range for  $Se$  with  $Sp \leq 0.9$ . The smallest values (41.6% and 53.8%) occurred for low  $Y$ , low  $Se$ ,  $Sp=0.7$  and 0.8, respectively.

For  $n=2000$ , the power reached 93% for all combinations of ranges, except for three ones: whole  $Y$ , low  $Se$ ,  $Sp = 0.7$  (70.4%), low  $Y$ , low  $Se$ ,  $Sp = 0.8$  (62.6%), low  $Y$ , low  $Se$ ,  $Sp = 0.7$  (52.8%).

For  $n=5000$ , the power reached 98% for all combinations of ranges, except for three ones: whole  $Y$ , low  $Se$ ,  $Sp = 0.7$  (74.8%), low  $Y$ , low  $Se$ ,  $Sp = 0.8$  (71.8%), low  $Y$ , low  $Se$ ,  $Sp = 0.7$  (70.6%).

For  $n=10000$ , the power was at least 98.6% for all combinations of ranges, except for three ones: whole  $Y$ , low  $Se$ ,  $Sp = 0.7$  (77.8%), low  $Y$ , low  $Se$ ,  $Sp = 0.8$  (75.0%), low  $Y$ , low  $Se$ ,  $Sp = 0.7$  (86.0%).

### ***Power to detect that Se depends on Z***

*The power was negatively influenced by low  $Sp$  and missing upper one-third of the probability range for Y. From  $n = 1000$ , the power reached 80% for almost all combinations of probability ranges and  $Sp$  values.*

For  $n = 500$ , the power to detect that Se depends on Z exceeded 90% when the upper one-third of the probability range of Y was present, and also when it was missing but the whole probability range for Se was present.

For  $n=1000$ , the power reached 80% for most combinations of ranges, except for low Y and low Se with  $Sp \leq 0.8$ , when it was 49.0% and 71.6% for  $Sp=0.7$  and 0.8, respectively.

For  $n=2000$ , the power reached 88% for all combinations of ranges, except for low Y and low Se with  $Sp = 0.7$ , when it was 66.0%.

For  $n=5000$ , the power exceeded 97% for all combinations of ranges.

For  $n=10000$ , the power was 100% for all combinations of ranges.

### ***The betas***

*The estimates of the betas were most accurate when the upper one-third for Se was present and  $Sp$  was high. If the upper one-third for both Y and Se were present and  $Sp$  was at least 0.9, the estimates had acceptable accuracy ( $RMSE < 0.55$ ) from  $n = 1000$ .*

*The estimate of  $\beta_1$  seems to have an upwards bias (about 0.1 and 0.03 for  $n=500$  and 5000) but estimating it from our simulation study is rather uncertain. Bias of  $\beta_0$  seems to be smaller and downwards direction (about 0.05 and 0.01 for  $n=500$  and 5000), but estimating it is even more uncertain.*

For  $n = 500$ , RMSE of  $\beta_1$  was 0.328 when the whole range was present for both Y and Se, and  $Sp$  was 1 (0.331 for  $Sp=0.999$ ).  $\beta_1$  and  $\beta_0$  were estimable with  $RMSE \leq 0.331$  and 0.336, respectively, when the whole range for Y and the upper one-third for Se were present, and  $Sp$  was at least 0.999.

For  $n=1000$ , RMSE of  $\beta_1$  was 0.155 when the whole range was present for both Y and Se, and  $Sp$  was 1 (0.143 for  $Sp=0.999$ ).  $\beta_1$  and  $\beta_0$  were well estimable with  $RMSE \leq 0.343$  and 0.546, respectively, when the upper one-third was present for both Y and Se, and  $Sp$  was at least 0.9.

For  $n=2000$ , RMSE of  $\beta_1$  was 0.1 when the whole range was present for both Y and Se, and Sp was 1 (0.103 for  $Sp=0.999$ ).  $\beta_1$  was well estimable with  $RMSE \leq 0.242$  if the upper one-third was present for both Y and Se. If the upper one-third was missing for Y but it was present for Se, and Sp was at least 0.9, the RMSE of  $\beta_1$  remained under 0.384.  $\beta_0$  was well estimable with  $RMSE \leq 0.493$  if the upper one-third was present for both Y and Se. If the upper one-third was missing for Y but it was present for Se, and Sp was at least 0.9, the RMSE of  $\beta_1$  remained under 0.558.

For  $n=5000$ , RMSE of  $\beta_1$  was 0.059 when the whole range was present for both Y and Se, and Sp was 1 (0.061 for  $Sp=0.999$ ). If the upper one-third of the Se probability range was not missing, RMSE was at most 0.206 (at most 0.127 when Sp was at least 0.9). Similarly,  $\beta_0$  was also well estimable (with  $RMSE \leq 0.316$ ) when the upper one-third of the Se probability range was not missing.

For  $n=10000$ , RMSE of  $\beta_1$  was 0.040 when the whole range was present for both Y and Se, and Sp 0.999 or 1. If the upper one-third of the Se probability range was not missing, RMSE was at most 0.126 (at most 0.086 when Sp was at least 0.9). Similarly,  $\beta_0$  was also well estimable (with  $RMSE \leq 0.211$ ) when the upper one-third of the Se probability range was not missing.

### ***The gammas***

*The estimates of the gammas were most accurate when the upper one-third of Y was present, and Sp was high. If the upper one-third was present for both Y and Se, the estimates had acceptable accuracy from  $n = 1000$ .*

*Bias of  $\gamma_1$  seems to be upwards (about 0.1 and 0.01 for  $n=500$  and 5000), but estimating is rather uncertain from the simulation. Bias of  $\gamma_0$  seems to be smaller and downwards (about 0.01 and 0.005 for  $n=500$  and 5000) but estimating it is even more uncertain.*

For  $n = 500$ , RMSE of  $\gamma_1$  was 0.231 when the whole range was present for both Y and Se, and Sp was 1 (0.877 for  $Sp=0.999$ ). RMSE of the gammas remained below 0.877 if the whole range for Se and the upper one-third for Y were present.

For  $n=1000$ , RMSE of  $\gamma_1$  was 0.132 when the whole range was present for both Y and Se, and Sp was 1 (0.136 for  $Sp=0.999$ ). RMSE of the gammas remained below 0.251 if the upper one-third was present both for Y and Se.

For  $n=2000$ , RMSE of  $\gamma_1$  was 0.093 when the whole range was present for both Y and Se, and Sp was 1 (0.092 for  $Sp=0.999$ ). RMSE of  $\gamma_1$  remained below 0.227 if the upper one-third of Y was present and Sp was higher than 0.7. RMSE of  $\gamma_0$  was below 0.365 if the upper one-third of Y was present. If the upper one-third of Se was also present, it remained below 0.186.

For  $n=5000$ , RMSE of  $\gamma_1$  was 0.055 when the whole range was present for both Y and Se, and Sp was 1 (0.059 for  $Sp=0.999$ ).  $\gamma_1$  was well estimable with  $RMSE \leq 0.121$  if the upper one-third of Y was present and Sp was greater than 0.7. RMSE of  $\gamma_0$  was at most 0.219 if the upper one-third of Y was present.

For  $n=10000$ , RMSE of  $\gamma_1$  was 0.038 when the whole range was present for both Y and Se, and Sp was 1 (0.040 for  $Sp=0.999$ ).  $\gamma_1$  was well estimable with  $RMSE \leq 0.081$  if the upper one-third of Y was present and Sp was greater than 0.7. RMSE of  $\gamma_0$  was at most 0.168 if the upper one-third of Y was present.

## ***Sp***

*The estimate of Sp was most accurate when the lower one-third for Y and the whole range of Se were present, and second most accurate when the lower one-third for Y and the upper one-third for Se were present. Accuracy was acceptable from  $n = 2000$ .*

*Bias of Sp depends on its true value. For true  $Sp < 0.9$ , the estimate is biased upwards, for  $Sp > 0.9$  downwards. Estimation of bias was rather uncertain.*

For  $n=500$ , RMSE of Sp was smallest (0.037 to 0.041 for  $Sp \leq 0.9$  and 0.009 to 0.010 for  $Sp \geq 0.999$ ) when the whole range for both Y and Se was present.

For  $n=1000$ , RMSE of Sp was smallest (0.021 to 0.035 for  $Sp \leq 0.9$  and 0.004 to 0.006 for  $Sp \geq 0.999$ ) when the lower one-third for Y and the whole range for Se was present. With missing lower one-third for Se it was higher (0.034 to 0.062 for  $Sp \leq 0.9$  and 0.010 to 0.011 for  $Sp \geq 0.999$ ).

For  $n=2000$ , RMSE of Sp was smallest (0.013 to 0.019 for  $Sp \leq 0.9$  and 0.003 to 0.004 for  $Sp \geq 0.999$ ) when the lower one-third for Y and the whole range for Se was present. With

missing lower one-third for Se, it was a little higher (0.023 to 0.032 for  $Sp \leq 0.9$  and 0.006 to 0.008 for  $Sp \geq 0.999$ ).

For  $n=5000$ , RMSE of  $Sp$  was smallest (0.008 to 0.019 for  $Sp \leq 0.9$  and 0.001 to 0.004 for  $Sp \geq 0.999$ ) when the lower one-third for  $Y$  and the whole range for  $Se$  was present. With missing lower one-third for  $Se$ , it was a little higher (0.013 to 0.019 for  $Sp \leq 0.9$  and 0.004 for  $Sp \geq 0.999$ ).

For  $n=10000$ , RMSE of  $Sp$  was smallest (0.006 to 0.009 for  $Sp \leq 0.9$  and 0.001 to 0.002 for  $Sp \geq 0.999$ ) when the lower one-third for  $Y$  and the whole range for  $Se$  was present. With missing lower one-third for  $Se$ , it was a little higher (0.009 to 0.013 for  $Sp \leq 0.9$  and 0.003 for  $Sp \geq 0.999$ ).