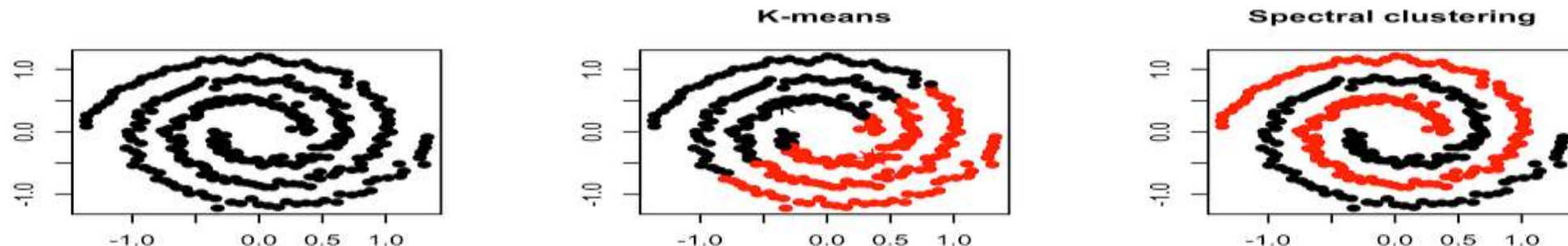


# SPECTRAL CLUSTERING

- **Spectral clustering** is a powerful technique used for clustering data points based on their similarity. Unlike traditional clustering algorithms, **spectral clustering doesn't make strong assumptions about the shape or size of the clusters**. Instead, it leverages the eigenvalues and eigenvectors of a similarity matrix derived from the data to perform clustering.
- **Similarity Matrix Construction:**
  - Spectral clustering begins by constructing a **similarity matrix based on pairwise similarities between data points**. Common measures include the radial basis function (RBF) kernel or nearest neighbors.
- **Dimensionality Reduction:**
  - The eigenvectors corresponding to **the smallest eigenvalues** are used to embed the data into a **lower-dimensional space**. Typically, the first  $k$  eigenvectors are selected, where  $k$  represents the number of desired clusters.
- **Clustering in Reduced Space:**
  - Traditional clustering algorithms (**k-means**) are applied to the reduced-dimensional space to partition the data into clusters.



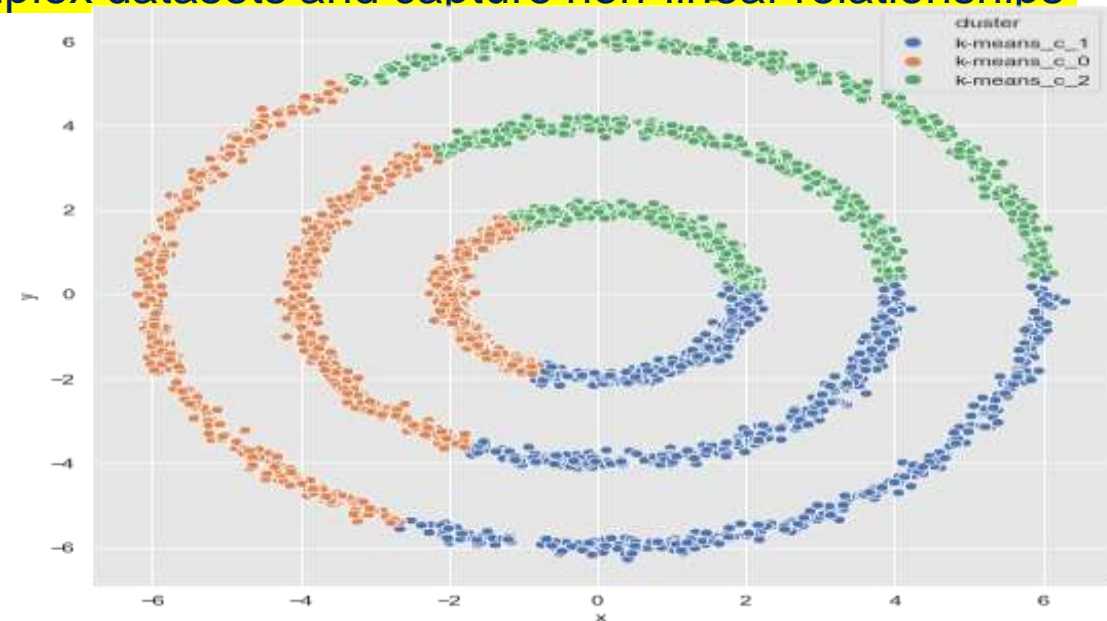
# SPECTRAL CLUSTERING

- **Advantages of Spectral Clustering:**

- **Flexibility:** Spectral clustering can detect clusters of arbitrary shapes and sizes.
- **Robustness:** It is robust to noise and outliers in the data.
- **Performance:** Spectral clustering often outperforms traditional methods, especially for complex datasets.

- **Conclusion:**

- Spectral clustering is a versatile technique that addresses many of the limitations of traditional clustering algorithms. Its ability to handle complex datasets and capture non-linear relationships makes it a valuable tool in various domains.



# SPECTRAL CLUSTERING

*Here's a breakdown of the Python code, focusing on the application of Spectral Clustering*

- `import pandas as pd`
- `import numpy as np`
- `import matplotlib.pyplot as plt`
- These lines import the necessary libraries: pandas for data manipulation, numpy for numerical operations.
- `dataset=pd.read_csv("Mall_Customers.csv")`  
This line reads the dataset from the CSV file named "Mall\_Customers.csv" into a pandas DataFrame named dataset.
- `X=dataset.iloc[:,3:5].values`  
This line extracts the features (columns 3 and 4) from the dataset and assigns them to the variable X

# SPECTRAL CLUSTERING

- `from sklearn.cluster import SpectralClustering`
- `from sklearn.preprocessing import StandardScaler, normalize`
- `from sklearn.decomposition import PCA`
- `from sklearn.metrics import silhouette_score`
- These lines import the Spectral Clustering class from scikit-learn, as well as other necessary modules for preprocessing and evaluation.
- `spectral_model_rbf = SpectralClustering(n_clusters = 2, affinity='rbf')`
- `labels_rbf = spectral_model_rbf.fit_predict(X_principal)`
- This initializes the SpectralClustering model with 2 clusters using the radial basis function (RBF) kernel as the similarity measure and assigns cluster labels to the data.

# SPECTRAL CLUSTERING

- `plt.scatter(X_principal['P1'], X_principal['P2'],`
- `c = SpectralClustering(n_clusters = 2, affinity='rbf').fit_predict(X_principal), cmap=plt.cm.winter)`
- `plt.show()`
- This creates a scatter plot of the data points in the reduced 2-dimensional space, with colors representing different clusters obtained from spectral clustering with the RBF affinity.
- `spectral_model_nn = SpectralClustering(n_clusters = 3, affinity='nearest_neighbors')`
- `labels_nn = spectral_model_nn.fit_predict(X_principal)`
- This initializes another Spectral Clustering model with 3 clusters using the nearest neighbors affinity and assigns cluster labels to the data.

# SPECTRAL CLUSTERING

- `plt.scatter(X_principal['P1'], X_principal['P2'],`
- `c = SpectralClustering(n_clusters = 3, affinity='nearest_neighbors').fit_predict(X_principal), cmap=plt.cm.winter)`
- `plt.show()`
- This creates a scatter plot of the data points, similar to the previous plot, but using spectral clustering with nearest neighbors affinity and 3 clusters.
- Overall, your code performs spectral clustering on the Mall Customers dataset, reduces the dimensionality of the data using PCA, and visualizes the clusters in a 2-dimensional space. It demonstrates how spectral clustering can be applied to group data points based on their similarities in reduced dimensions.

# SPECTRAL CLUSTERING

