

## Exam Questions

### Problem 1:

- a. Kirchhoff's 1<sup>st</sup> and 2<sup>nd</sup> laws explain the ways in which current and voltage behave in circuits throughout loops and junctions. The 1<sup>st</sup> Law states that, due to Conservation of Charge, all current that enters a junction must also exit that junction. There is no net gain or loss of total current, so the current split among all paths must sum to constant amount. The 2<sup>nd</sup> Law states that, due to Conservation of Energy, potential in a closed circuit is conserved. This means that all voltage drops or gains within a closed loop in a circuit must sum to the total amount of electric potential originally in the system, which is 0.
- b. Nyquist Frequency is the largest frequency that can be used to accurately record a sample's signal. It is equal to half of a given sample rate and, to avoid aliasing distortion, can only be increased if the sample rate is increased by twice the same amount.
- c. The Sifting Property is an attribute of the unit impulse function that allows for particular values of a continuous function to be taken out and evaluated at given times while ignoring evaluation of the impulse function anywhere else as it is equal to 0 at these non-sifted times.

### Problem 2:

- c. MATLAB mean: 7.99  
MATLAB var: 3.96

d.  $E(s_k) = 4 + 0.5E(s_k) + 2e_k$   
 $E(s_k) = 4 + 0.5E(s_k) + 0$

$E(s_k) = 4/0.5 = 8$  No Change

$Var(s_k) = (0.5)(0.5)Var(s_k) + 2e_k$

$Var(s_k) = 0.25Var(s_k) + 2(1)$

$Var(s_k) = 2/0.75 = 2.67$  Doubled Variance

System has increased variance (doubled) and a slightly higher Signal to Noise Ratio  
 from HW #6

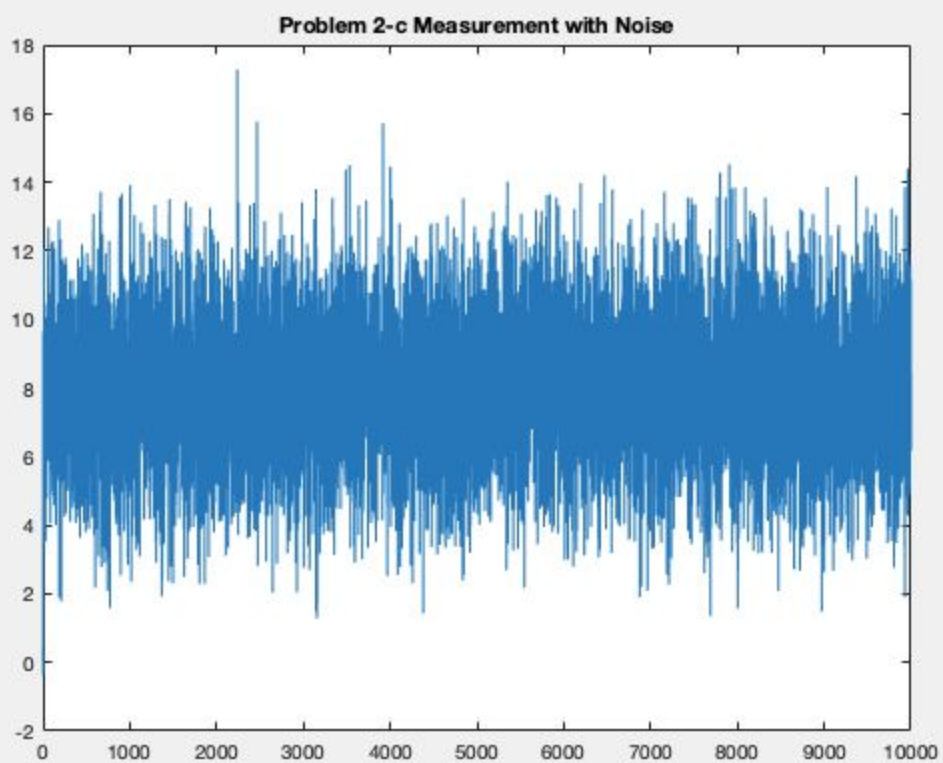
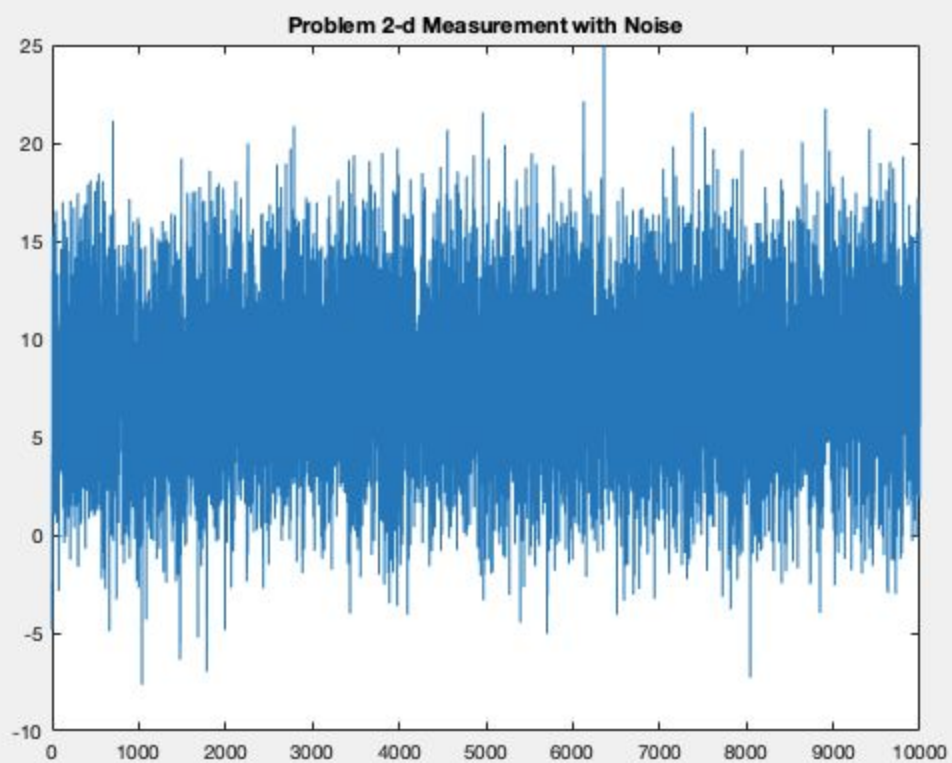
$SNR = \log(Var(s_k) + E(s_k)^2)$

$= \log(2.67 + 8^2)$

$= 1.824$  dB greater than 1.815 found in #6

MATLAB mean = 7.98  
MATLAB var = 16.2

- e. The assumption made would not work if the coefficient for  $s_{k-1}$  were greater than 1. This is because the equation would quickly begin to increase exponentially so there would be a significant difference between a point and the one preceding it over many time steps. The slope difference between points gets smaller and eventually converges to 0 when the coefficient is < 1. It goes to infinity when the coefficient is > 1.



```
Week1_ExamQ_Problem2c.m  Week1_ExamQ_Problem2d.m  +
1  % Problem 2
2  % c
3  % Measurement Noise
4  clear;
5  % Measurement Function and Initial x value
6  A=4;
7  p=0.5;
8  x(1)=0;
9  for n=2:10000
10     x(n)=A+p*x(n-1);
11 end
12 % Additive Noise
13 noise=randn(1,10000)*2;
14
15 M=x+noise;
16
17 figure;plot(M)
18 title('Problem 2-c Measurement with Noise')
19
20 mean(M)
21 var(M)
```

Command Window

```
ans =
    7.9872

ans =
    3.9648

fx >>
```

```
Week1_ExamQ_Problem2c.m Week1_ExamQ_Problem2d.m +
1 % Problem 2
2 % d
3 % Measurement Noise
4 clear;
5 % Measurement Function and Initial x value
6 A=4;
7 p=0.5;
8 x(1)=0;
9 for n=2:10000
10     x(n)=A+p*x(n-1);
11 end
12 % Additive Noise
13 noise=randn(1,10000)*2;
14
15 M=x+(2*noise)
16
17 figure;plot(M)
18 title('Problem 2-d Measurement with Noise')
19
20 mean(M)
21 var(M)
```

Command Window

```
ans =
    7.9784

ans =
    16.1789

fx >>
```