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## Main Function

```
function ECE340_Lab2()
    warning('off','all');
    Q1_Convolution();
    Q2_Convolution_Filter();
    Q3_Aliasing_Effect();
    Q4_2D_Aliasing();
    OptionalQ_LowPassFilter_Aliasing();
end
```

## Q1 Convolution

```
function Q1_Convolution()
    %Defining the discrete function x[k]
    function X=x(k)
        X=k.*(k>=0 & k<=4);
    end
    %Defining the discrete function h[k]
    function H=h(k)
        H=(2-k).*(k>=0 & k<=3);
    end

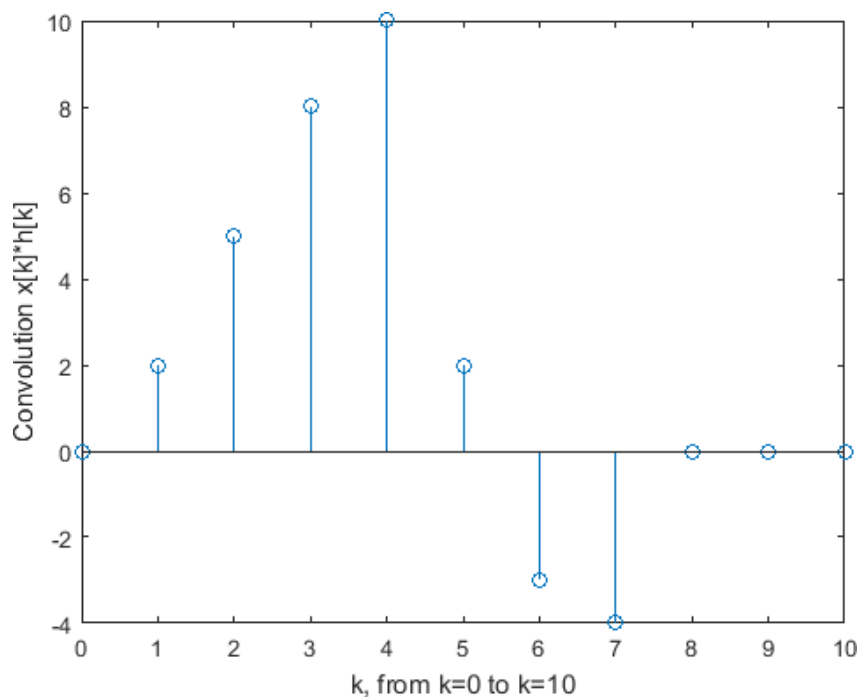
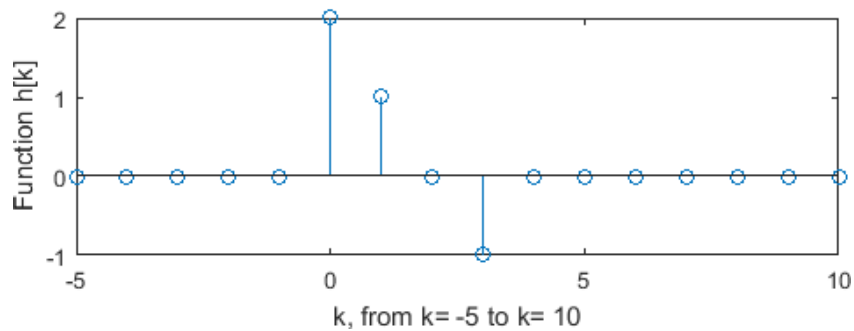
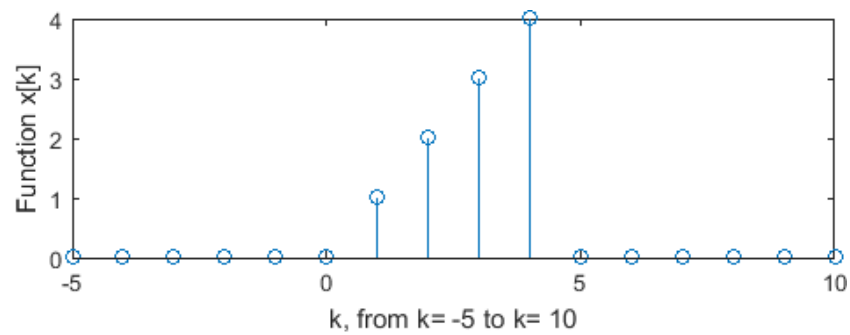
    %(1a)
    %Plotting the two functions
    figure %Creating a figure
    subplot(2,1,1) %Creating 1st subplot
    stem(-5:1:10,x(-5:1:10)); %plotting x[k]
    xlabel('k, from k= -5 to k= 10'); %Labelling axis
    ylabel('Function x[k]')
    hold on
    subplot(2,1,2) %Creatting the 2nd subplot
    stem(-5:1:10,h(-5:1:10)); %plotting x[k]
    xlabel('k, from k= -5 to k= 10'); %Labelling axis
    ylabel('Function h[k]')

    %(1b)
    %Calculating and plotting the convolution
    conv_x_and_h=conv(x(0:5),h(0:5))
    %conv_x_and_h is [0 2 5 8 10 2 -3 -4 0 0 0]

    figure %Creating a new figure
    stem(0:10,conv_x_and_h) %Plotting the convolution
    xlabel('k, from k=0 to k=10'); %Labelling axis
    ylabel('Convolution x[k]*h[k]')
    %(1c) See attachment
end
```

conv\_x\_and\_h =

0      2      5      8      10      2      -3      -4      0      0      0



## Q2 Convolution Audio Filter

```
function Q2_Convolution_Filter()
%2a) Defining the discrete function h[k]
function H=h(k)
    H=(0.3.*sinc(0.3.*(k-25)).* ...
    (0.54-0.46.*cos(2.*pi.*k./50))).*(k>=0 & k<=50);
end

%2b) Plotting the function h[k]
figure %Creating a new figure
stem(-10:60,h(-10:60)); %plotting h[k]
xlabel('k, from k= -10 to k= 60'); %Labelling axis
ylabel('Function h[k]')

%2c) reading the audio file, "baila.wav"
[baila, baila_FS]=audioread('baila.wav');
%2c+d) Calculating and saving the filtered file, "baila_filtered.wav"
```

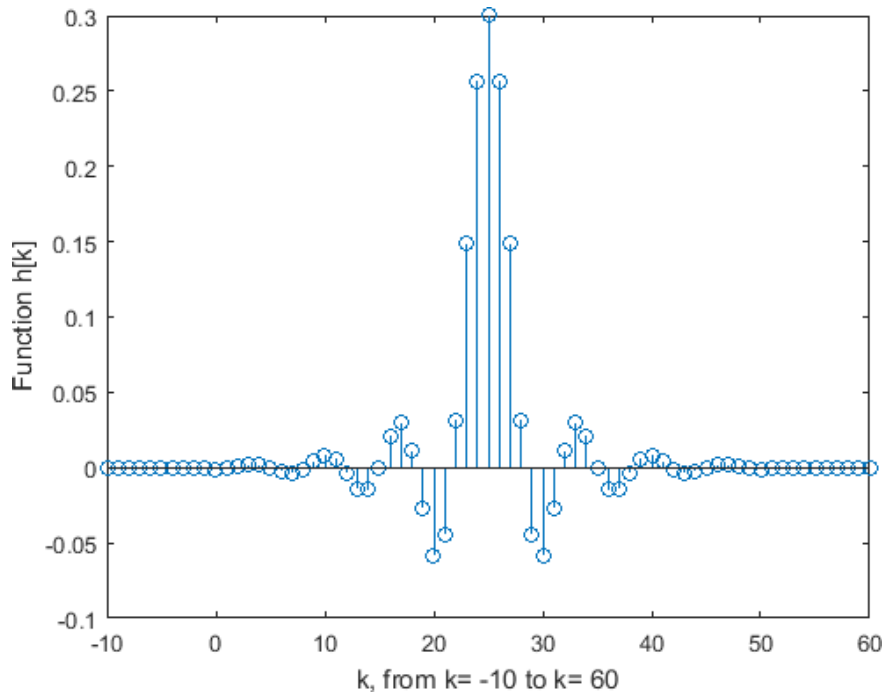
```

baila_filtered=conv(baila,h(0:50));
audiowrite('baila_filtered.wav',baila_filtered,baila_FS);
%Comments on Quality
Quality_comment=sprintf(['The filtered audio file is 'sharper' with less '...
    'noise. baila.wav sounds as if it was recorded in a bathroom \n'...
    'while baila_filtered.wav is crispy sharp.'])
end

```

Quality\_comment =

The filtered audio file is 'sharper' with less noise. baila.wav sounds as if it was recorded in a bathroom while baila\_filtered.wav is crispy sharp.



### Q3 Aliasing Effect

```

function Q3_Aliasing_Effect()
    function X1=x1(t)
        X1=cos(35.*pi.*t);
    end
    function X2=x2(t)
        X2=cos(165.*pi.*t);
    end
    function X3=x3(t)
        X3=cos(235.*pi.*t);
    end
    %(3a): y1 & y2
    %Defining Sampling Frequenct and thus sampling period
    f=100;
    t=1/f;

    %Calculating the digital signals y1[n] and y2[n] and stem-plotting them
    y1=x1((0:30)*t);
    y2=x2((0:30)*t);
    figure %Creatting new figure
    subplot(2,1,1); %Creating first subplot for y1[n]
    stem((0:30)*t,y1);
    xlabel('t, (with sampling period 0.01 seconds; n=0 to 30)'); %Labels
    ylabel('y_1[n]');
    subplot(2,1,2); %Creating second subplot for y2[n]
    stem((0:30)*t,y2);

```

```

xlabel('t, (with sampling period 0.01 seconds; n=0 to 30)'); %Labels
ylabel('y_2[n]');
    Comment=sprintf(['The two sequences y_1[n] and y_2[n] have the same values but'...
    ' the two functions x1 and x2 are not the same, \nthey only appear'...
    ' to be the same due to alising and choice of sampling frequency.'])

%(3b): z1 & z2
%Defining Sampling Frequencyt and thus sampling period
f2=1000;
t2=1/f2;
%Calculating the digital signals y1[n] and y2[n] and stem-plotting them
z1=x1((0:300)*t2);
z2=x2((0:300)*t2);
figure %Creatting new figure
subplot(2,1,1);
plot((0:300)*t2,z1,'r-', (0:30)*t,y1,'b+');
xlabel('Time t, (s)'); ylabel('y_1[n] and z_1[n]');
legend('z_1[n]', 'y_1[n]');
subplot(2,1,2);
plot((0:300)*t2,z2,'r-', (0:30)*t,y2,'b+');
xlabel('Time t, (s)'); ylabel('y_2[n] and z_2[n]');
legend('z_2[n]', 'y_2[n]');
    Comment=sprintf(['At high enough frequency the differences in x1 and x2 '...
    'becomes clear. Eventhough y1 and y2 have the same values but z1 and\n'...
    ' z2 do not have the same values. So at high enough sampling rate'...
    ' the aliasing effect disappears.'])

%(3c): z3
y3=x3((0:50)*t);
y1=x1((0:50)*t);
figure %Creatting new figure
subplot(2,1,1); %Creating first subplot for y1[n] and y3[n]
stem([(0:50)*t;(0:50)*t],[y1' y3']);
xlabel('t, (with sampling period 0.01 seconds; n=0 to 50)'); %Labels
ylabel('y_1[n] & y_3[n]');
legend('y_1[n]', 'y_3[n]');
subplot(2,1,2); %Creating second subplot for difference y1[n]-y3[n]
stem((0:50)*t,[y1-y3]);
xlabel('t, (with sampling period 0.01 seconds; n=0 to 50)'); %Labels
ylabel('(y_1[n] - y_3[n])');
title('Negligible Difference in the two Sequences');
end

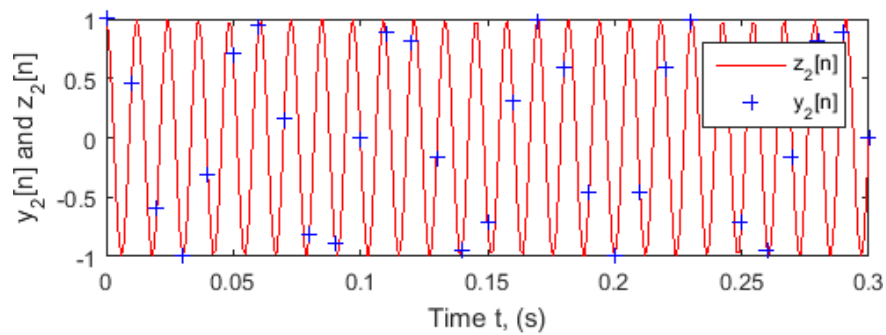
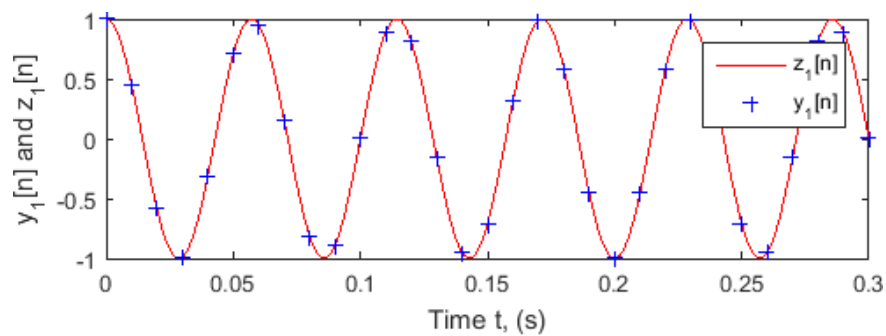
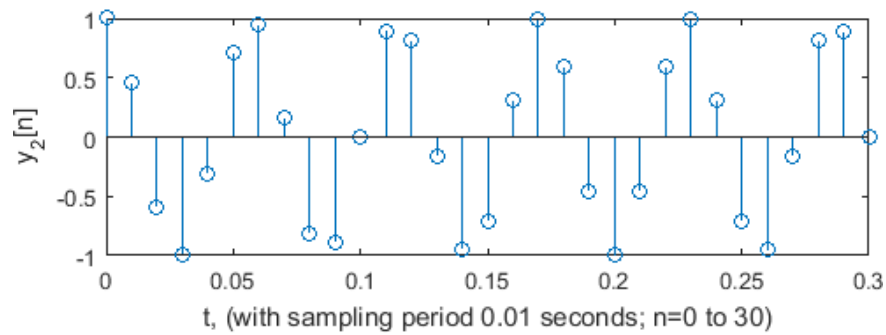
```

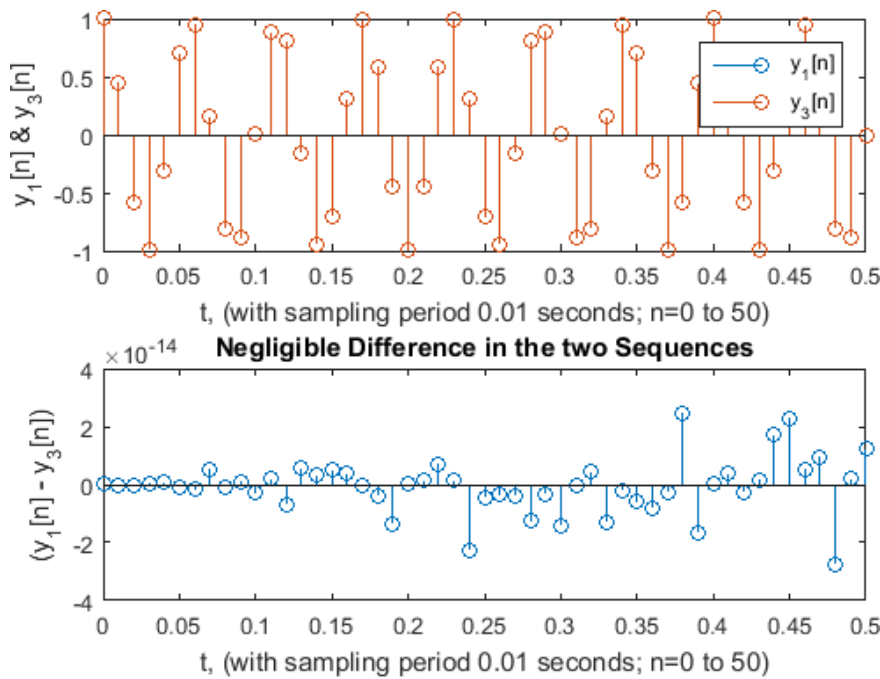
Comment =

The two sequences y\_1[n] and y\_2[n] have the same values but the two functions x1 and x2 are not the same, they only appear to be the same due to alising and choice of sampling frequency.

Comment =

At high enough frequency the differences in x1 and x2 becomes clear. Eventhough y1 and y2 have the same values but z1 and z2 do not have the same values. So at high enough sampling rate the aliasing effect disappears.





#### Q4 2D Aliasing in an image

```
function Q4_2D_Aliasing()
%a) Reading the image file
Img=imread('barbaraLarge.jpg');
%b) Displaying the original image
figure; imshow(Img), colorbar;
title('Original Image Of barbaraLarge.jpg');
%c) Resizing the image files with and without antialiasing enabled
Img0_9_AntiAlisOn=imresize(Img, 0.9, 'nearest','antialiasing',1);
Img0_7_AntiAlisOn=imresize(Img, 0.7, 'nearest','antialiasing',1);
Img0_5_AntiAlisOn=imresize(Img, 0.5, 'nearest','antialiasing',1);
Img0_9_AntiAlisOff=imresize(Img, 0.9, 'nearest','antialiasing',0);
Img0_7_AntiAlisOff=imresize(Img, 0.7, 'nearest','antialiasing',0);
Img0_5_AntiAlisOff=imresize(Img, 0.5, 'nearest','antialiasing',0);
comments=sprintf(['When antialiasing is enabled the image quality is not '...
    'affected as much and there is less aliasing observable in high\n'...
    'frequency regions'])

%d) Showing the images
figure;imshow(Img0_9_AntiAlisOn), colorbar;
title('Resized to 90% with Antialiasing On');
figure;imshow(Img0_9_AntiAlisOff), colorbar;
title('Resized to 90% with Antialiasing Off');
figure;imshow(Img0_7_AntiAlisOn), colorbar;
title('Resized to 70% with Antialiasing On');
figure;imshow(Img0_7_AntiAlisOff), colorbar;
title('Resized to 70% with Antialiasing Off');
figure;imshow(Img0_5_AntiAlisOn), colorbar;
title('Resized to 50% with Antialiasing On');
figure;imshow(Img0_5_AntiAlisOff), colorbar;
title('Resized to 50% with Antialiasing Off');
comments=sprintf(['High frequency regions begin to show aliasing when the '...
    'sampling frequency is reduced. Having antialiasing enabled \n'...
    'reduces aliasing and the image quality is better.'])
end
```

comments =

When antialiasing is enabled the image quality is not affected as much and there is less aliasing observable in high frequency regions

comments =

High frequency regions begin to show aliasing when the sampling frequency is reduced. Having antialiasing enabled reduces aliasing and the image quality is better.

**Original Image Of barbaraLarge.jpg**



**Resized to 90% with Antialiasing On**



**Resized to 90% with Antialiasing Off****Resized to 70% with Antialiasing On****Resized to 70% with Antialiasing Off****Resized to 50% with Antialiasing On****Resized to 50% with Antialiasing Off****Optional Demo, Low pass filtering prior to resizing**

```
function OptionalQ_LowPassFilter_Aliasing()
    I=imread('barbaraLarge.jpg');
    % Low pass filtering before downsampling
```



```
% creates a 3x3 low pass filter kernel
filt=fspecial('average',[3 3]);
% applies the lpf by convolving the image with the filter kernel
filt_img=imfilter(I,filt,'conv');

%Resizing the image to 70% with and without low pass filter applied
B_LPF=imresize(filt_img, 0.7 , 'nearest', 0);
B=imresize(I, 0.7, 'nearest', 0);

%Printing the figures
figure, imshow(I);
title('Original Barbara Image');
figure, imshow(B);
title('Barbara Image Resized to 70% of Original Size');
figure, imshow(B_LPF);
title('Low-pass Filter Applied Before Resizing to 70%');
comment=sprintf(['The filter is a 3by3 squar that averages the nearby values '...
    'and thus removes the high frequency components that have periods\n'...
    ' of smaller than 3 pixels. This lp filtering reduces the aliasing'...
    ' effect and improves the image quality during resizing.'])
end
```

comment =

The filter is a 3by3 squar that averages the nearby values and thus removes the high frequency components that have periods of smaller than 3 pixels. This lp filtering reduces the aliasing effect and improves the image quality during resizing.

**Original Barbara Image****Barbara Image Resized to 70% of Original Size****Low-pass Filter Applied Before Resizing to 70%**