

Process	Allocation			MAX		
	R ₁	R ₂	R ₃	R ₁	R ₂	R ₃
P ₀	0	1	0	7	5	3
P ₁	2	0	0	3	2	2
P ₂	3	0	2	9	0	2
P ₃	2	1	1	2	2	2
P ₄	0	0	2	4	3	3

Available
R₁ R₂ R₃
3 3 2

Suppose at time T₁, process P₂ request 1 additional instance of resource type R₁, 2 instance of resource type R₃. Can the request be granted immediately

⇒ Request of P₂ (1, 0, 2)

need_{P₂} = 902 - 302 = 600
MAX - allocation

Request ≤ need

1 0 2 ≤ 600

1 ≤ 6

0 ≤ 0

2 ≤ 0 x

∴ The process P₂ request can not be granted immediately

Consider a set system with set of 5 process & 4 Resources

Process	Allocation				MAX			
	A	B	C	D	A	B	C	D
P ₀	0	0	1	2	0	0	1	2
P ₁	1	0	0	0	1	7	5	0
P ₂	1	3	5	6	2	3	5	6
P ₃	0	6	3	2	0	6	5	2
P ₄	0	0	1	4	0	6	5	6

Available
A B C D
1 5 2 0

(i) If the request from process P₁ arrives for 4 instance of resource type 'B' & 2 instances for resource type 'C'. Can the request be granted immediately

Request of P_1 (0, 4, 20)

$$\text{need} = 1750 - 1000 = 0750$$

Request \leq need

$$0420 \leq 0750$$

$$0 \leq 0 \checkmark$$

$$4 \leq 7 \checkmark$$

$$2 \leq 5 \checkmark$$

$$0 \leq 0 \checkmark$$

Request \leq Available

$$0420 \leq 1520$$

$$0 \leq 1 \checkmark$$

$$4 \leq 5 \checkmark$$

$$2 \leq 2 \checkmark$$

$$0 \leq 0 \checkmark$$

$$\begin{aligned}\text{Available} &= \text{Available} - \text{Request} \\ &= 1520 - 0420\end{aligned}$$

$$= 1100$$

$$\begin{aligned}\text{Allocation} &= \text{Allocation} + \text{Request} \\ &= 1000 + 0420 \\ &= 1420\end{aligned}$$

$$\text{Need} = \text{Need} - \text{Request}$$

$$= 0750 - 0420$$

$$= \cancel{0330}$$

$$= 0330$$

\therefore Process P_1 request can be granted immediately

ii) Suppose on granting the above P_1 request, can the system be in safe state or not

$$\Rightarrow \text{Available} = 1100$$

$$\text{Allocation of } P_1 = 1420$$

$$\text{Need of } P_1 = \cancel{0750} 0330$$

$work = available = 1100$
 $need \leq work$
 $0330 \leq 1100$
 $0 \leq 1$
 $3 \leq 1 \times$
 $3 \leq 0 \times$
 $0 \leq 0$

Process	Allocation			MAX			Need		
	A	B	C	A	B	C	A	B	C
P ₀	0	0	12				0	0	0
P ₁	1	4	20	1	7	50	0	3	30
P ₂	1	3	54	2	3	56	1	0	2
P ₃	0	6	32	0	6	52	0	0	20
P ₄	0	0	14	0	6	56	0	6	42

$i = 0, P_0 \quad work = available = 1100$
 $need \leq work$
~~0000~~
 $0000 \leq 1100$
 $0 \leq 1$
 $0 \leq 1$
 $0 \leq 0$
 $0 \leq 0$

$work = work + allocation = 1100 + 0012 = 1112$

$i = 1, P_1 \quad work = 1112$
 $need \leq work$
 $0330 \leq 1112$
 $0 \leq 1$
 $3 \leq 1 \times$
 $3 \leq 1 \times$
 $0 \leq 2$

$i = 2, P_2 \quad work = 1112$
 $need \leq work$
 $1002 \leq 1112$
 $1 \leq 1$
 $0 \leq 1$
 $0 \leq 1$
 $2 \leq 1$

$i = 3, P_2 \quad work = 2466$
 $need \leq work$
 $0020 \leq 2466$
 $0 \leq 2$
 $0 \leq 4$
 $2 \leq 6$
 $0 \leq 6$

$work = work + allocation$
 $= 1112 + 1354$
 $= 2466$

$work = work + allocation$
 $= 2466 + 0632$
 $= 3098$

$$P_4, \text{work} = 2 \ 10 \ 9 \ 8$$

$$\text{need} \leq \text{work}$$

$$0642 \leq 21098$$

$$0 \leq 2$$

$$6 \leq 10$$

$$4 \leq 9$$

$$2 \leq 8$$

$$\begin{aligned} \text{work} &= \text{work} + \text{allocation} \\ &= 21098 + 0014 \\ &= 2101012 \end{aligned}$$

Roll back

$$P_1, \text{work} = 2101012$$

$$\text{need} \leq \text{work}$$

$$0330 \leq 2101012$$

$$0 \leq 2$$

$$3 \leq 10$$

$$3 \leq 10$$

$$0 \leq 12$$

$$\begin{aligned} \text{work} &= \text{work} + \text{allocation} \\ &= 2101012 + 1420 \\ &= 3141210 \end{aligned}$$

\therefore System is in safe state & safe sequence is P_0, P_2, P_3, P_4, P_1

4) Consider a system with a set of 5 process P_0, P_1, P_2, P_3, P_4 . There are 3 types of resources R_1, R_2, R_3 . There are 10 instance of R_1 , 5 instance R_2 & 7 instance R_3 . The AT time to situation is as follows

Process	Allocation			MAX
	R_1	R_2	R_3	
P_0	0	1	0	7 5 3
P_1	2	0	0	3 2 2
P_2	3	0	2	9 0 2
P_3	2	1	1	2 2 2
P_4	0	0	2	4 3 3

Apply Banker's algorithm for the following question.

(i) Is the system in safe state at to

(ii) Suppose at time t_1 , process P_2 request 1 addition instance of resource type R_1 & 2 instances of resource type R_3 will the process request be granted immediately

(iii) After granting process P_2 request, will the system be in safe state

(i) \rightarrow

	Need	R_1	R_2	R_3
P_0	7	4	3	3
P_1	1	2	2	2
P_2	6	0	0	0
P_3	6	1	1	1
P_4	4	3	1	1

Available		
R_1	R_2	R_3
10-7	5-2	7-5
3	3	2

$i=0, P_0, \text{work} = \text{available} = 332$

need \leq work

$$743 \leq 332$$

$$7 \leq 3 \times$$

$$4 \leq 3 \times$$

$$3 \leq 2 \times$$

$P_1, \text{need} \leq \text{work}$

$$122 \leq 332$$

$$1 \leq 3 \checkmark$$

$$2 \leq 3 \checkmark$$

$$2 \leq 2$$

$P_2, \text{work} = 532$

need \leq work

$$600 \leq 532$$

$$6 \leq 5 \times$$

$$0 \leq 3$$

$$0 \leq 2$$

work = work + allocation

$$= 332 + 200$$

$$= 532$$

$$P_3 \text{ work} = 532$$

$$\text{need} \leq \text{work}$$

$$011 \leq 532$$

$$0 \leq 5$$

$$1 \leq 3$$

$$1 \leq 2$$

$$\begin{aligned} \text{work} &= \text{work} + \text{allocation} \\ &= 532 + 211 \\ &= 743 \end{aligned}$$

$$P_4 \text{ work} = 743$$

$$\text{need} \leq \text{work}$$

$$431 \leq 743$$

$$4 \leq 7$$

$$3 \leq 4$$

$$1 \leq 3$$

$$\begin{aligned} \text{work} &= \text{work} + \text{allocation} \\ &= 743 + 002 \\ &= 745 \end{aligned}$$

Roll back

$$P_0 \text{ work} = 745$$

$$\text{need} \leq \text{work}$$

$$743 \leq 745$$

$$7 \leq 7$$

$$4 \leq 4$$

$$3 \leq 5$$

$$\begin{aligned} \text{work} &= \text{work} + \text{allocation} \\ &= 745 + 010 \\ &= 755 \end{aligned}$$

$$P_2 \text{ work} = 755$$

$$\text{need} \leq \text{work}$$

$$600 \leq 755$$

$$6 \leq 7$$

$$0 \leq 5$$

$$0 \leq 5$$

$$\begin{aligned} \text{work} &= \text{work} + \text{allocation} \\ &= 755 + 302 \\ &= 1057 \end{aligned}$$

∴ System is in safe state & safe sequence

$$P_1, P_3, P_4, P_0, P_2$$

(i) $\Rightarrow P_2$ request = (1, 0, 2)

need = 600

request \leq need

102 \leq 600

1 \leq 6

0 \leq 0

2 \leq 0 X

\therefore The process P_2 request can not be granted immediately

(iii) Since the process request can not be granted and henceforth no need to apply safety algorithm as values remain same

5) Consider a system with set of 3 process

Process	Allocation			MAX			Available		
	A	B	C	A	B	C			
P_0	2	2	3	3	6	8	A	B	C
P_1	2	0	3	4	3	3	2	3	0
P_2	1	2	4	3	4	4			

(i) Calculate need

(ii) Apply Banker's algorithm for following sub questions

(a) Check whether system is in safe state or not

(b) If the P_3 does not want any additional instance of type A, B, C, is there any necessity to apply resource request algorithm

(c) Suppose if P_2 request for 4 additional instance of type A, 6 additional instance of type B, 8 additional instance of type C. Check if a process request can be granted immediately or not

(d) Suppose on granting process request, check if the system is in safe state or not

Deadlock detection problems

Consider a set of system with set of 5 process

Process	Allocation			Request-		
	A	B	C	A	B	C
P ₀	0	1	0	0	0	0
P ₁	2	0	0	0	0	2
P ₂	3	0	0	0	0	0
P ₃	2	1	1	1	0	0
P ₄	0	0	2	0	0	2

Available
A B C
0 0 0

$\Rightarrow \text{work} = \text{available} = 000$

P₀, ~~req~~ request \leq work

$000 \leq 000 \checkmark$

work = work + allocation

$000 + 010 = 010$

P₁, work = 010

request \leq work

$202 \leq 010 \times$

P₂ work = 010

request \leq work

$000 \leq 010 \checkmark$

work = work + allocation

$= 010 + 303$

$= 313$

P₃ work = 313

request \leq work

$100 \leq 313 \checkmark$

work = work + allocation

$= 313 + 211 = 523$

P₄ work = 523

request \leq work

$002 \leq 523 \checkmark$

work = work + allocation
 $= 523 + 002$
 $= 525$

Roll back

$$P_1: \text{work} = 525$$

$$\text{request} \leq \text{work}$$

$$002 \leq 525 \quad \checkmark$$

$$P_4: \text{work} = 521$$

$$\text{request} \leq \text{work}$$

$$002 \leq 521$$

\therefore System is not in deadlock

24 Process

Allocation

Request

	A	B	C
P_0	0	1	0
P_1	2	0	0
P_2	3	0	3
P_3	2	1	1
P_4	0	0	2

A	B	C
0	0	0
2	0	2
0	0	1
1	0	0
0	0	2

Available

A B C
0 0 0

$$P_0: \text{work} = 000$$

$$\text{request} \leq \text{work}$$

$$000 \leq 000$$

$$\text{work} = \text{work} + \text{allocation} = 000 + 010 = 010$$

$$P_1: \text{work} = 010$$

$$\text{request} \leq \text{work}$$

$$202 \leq 010 \quad \times$$

$$P_2: \text{request} \leq \text{work}$$

$$000 \leq 010 \quad \times$$

$$P_3: \text{request} \leq \text{work}$$

$$100 \leq 010 \quad \times$$

P_1 request ≤ 10014
 $002 \leq 010x$

roll back
 P_2 , request ≤ 10014
 $001 \leq 010x$

\therefore ~~System is in~~
 \therefore deadlock is detected in the system