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EE3900 : Assignment-5

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Download all python codes from

https://github.com/Rahul27n/EE3900/blob/main/ Assignment_5/Assignment_5.py

and latex-tikz codes from

https://github.com/Rahul27n/EE3900/blob/main/ Assignment_5/Assignment_5.tex

1 QUESTION: QUADRATIC FORMS Q2.17

Find a quadratic polynomial, the sum and product of whose zeroes are -3 and 2, respectively.

2 SOLUTION

A general polynomial equation p(x, y) of degree 2 is given by :

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$
 (2.0.1)

The vector equation of p(x, y) is given by :

$$\mathbf{x}^{\mathsf{T}} \begin{pmatrix} A & \frac{B}{2} \\ \frac{B}{2} & C \end{pmatrix} \mathbf{x} + \begin{pmatrix} D & E \end{pmatrix} \mathbf{x} + F = 0 \tag{2.0.2}$$

As the polynomial we have to find is a quadratic polynomial we have :

$$B = 0 \tag{2.0.3}$$

$$C = 0 \tag{2.0.4}$$

$$E = 0 \tag{2.0.5}$$

If we take A = 1, we have :

Sum of zeroes =
$$-D = -3 \implies D = 3$$
 (2.0.6)

Product of zeroes =
$$F = 2$$
 (2.0.7)

Substituting the values in (2.0.2) we have :

$$\mathbf{x}^{\mathbf{T}} \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \mathbf{x} + \begin{pmatrix} 3 & 0 \end{pmatrix} \mathbf{x} + 2 = 0 \tag{2.0.8}$$

which is equivalent to:

$$x^2 + 3x + 2 = 0 ag{2.0.9}$$

Therefore the required quadratic polynomial is given by $y = x^2 + 3x + 2$.

The zeroes of the polynomial are given by -1 and -2 as shown in the below figure.

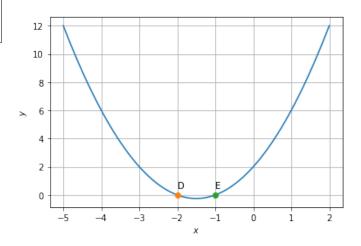


Fig. 0: Quadratic polynomial with zeroes -1 and -2