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# EE3900: Assignment-4

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Download all python codes from

https://github.com/Rahul27n/EE3900/blob/main/ Assignment\_4/Assignment\_4.py

and latex-tikz codes from

https://github.com/Rahul27n/EE3900/blob/main/ Assignment\_4/Assignment\_4.tex

## 1 QUESTION: LINEAR FORMS Q2.18

Find the equation of a line that cuts off equal intercepts on the coordinate axes and passes through the point  $\binom{2}{3}$ .

### 2 SOLUTION

The general equation of a line can be written as:

$$\mathbf{n}^T \mathbf{x} = c \tag{2.0.1}$$

where  $\mathbf{n}$  is the normal to the line.

The standard basis vectors in 2D plane are given by:

$$\mathbf{e_1} = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \tag{2.0.2}$$

$$\mathbf{e_2} = \begin{pmatrix} 0 \\ 1 \end{pmatrix} \tag{2.0.3}$$

Let the line (2.0.1) cut the x and y co-ordinate axes at **A** and **B** respectively. They can be written as:

$$\mathbf{A} = \frac{c\mathbf{e}_1}{\mathbf{n}^T \mathbf{e}_1} \tag{2.0.4}$$

$$\mathbf{B} = \frac{c\mathbf{e}_2}{\mathbf{n}^T \mathbf{e}_2} \tag{2.0.5}$$

It is given that the line cuts off equal intercepts on the co-ordinate axes. Hence from (2.0.4) and (2.0.5) we have:

$$\mathbf{n}^T \mathbf{e_1} = \mathbf{n}^T \mathbf{e_2} \tag{2.0.6}$$

which is equivalent to:

$$\mathbf{n}^T(\mathbf{e_1} - \mathbf{e_2}) = 0 \tag{2.0.7}$$

$$\mathbf{n}^T \begin{pmatrix} 1 \\ -1 \end{pmatrix} = 0 \tag{2.0.8}$$

$$\implies \mathbf{n} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \tag{2.0.9}$$

Hence from (2.0.1) and (2.0.9), the equation of the line is given by:

$$\begin{pmatrix} 1 & 1 \end{pmatrix} \mathbf{x} = c \tag{2.0.10}$$

It is given that  $\binom{2}{3}$  lies on the line. Hence from (2.0.10) we have:

$$c = \begin{pmatrix} 1 & 1 \end{pmatrix} \begin{pmatrix} 2 \\ 3 \end{pmatrix} = 5$$
 (2.0.11)

Therefore the equation of the line is:

$$\begin{pmatrix} 1 & 1 \end{pmatrix} \mathbf{x} = 5 \tag{2.0.12}$$

The illustration of the line is shown below:

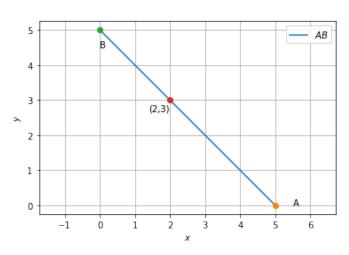


Fig. 0: Line **AB** making equal intercepts on coordinate axes