## 11.9.3

## EE23BTECH11053-R.Rahul\*

## **QUESTION:**

1. How many terms of G.P.3, $3^2$ , $3^3$ ,... are needed to give the sum 120 ?

## **SOLUTION:**

Parameter	Description	Value
n	No. of terms in the G.P	4
x(0)	first term in the G.P	3
r	common ratio in the G.P	3

VARIABLES

$$y(n) = \frac{1}{2\pi j} \oint_C \frac{3z^2}{(z-1)(z-3)} z^{n-1} dz$$

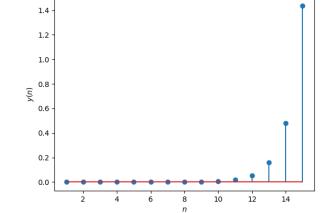
$$= \frac{1}{2\pi j} \oint_C \frac{3}{2} \left( \frac{1}{z-3} - \frac{1}{z-1} z^{n+1} \right) dz$$

$$= \frac{3}{2} \left( \left( \lim_{z \to 3} \frac{z^{n+1}}{z-3} (z-3) \right) - \left( \lim_{z \to 1} \frac{z^{n+1}}{z-1} (z-1) \right) \right)$$
(10)

$$=\frac{3}{2}(3^n-1)\tag{11}$$

$$120 = \frac{3}{2}(3^n - 1) \tag{12}$$

$$n = 4 \tag{13}$$



$$x(n) = x(0)r^n (1)$$

$$x(z) = \frac{x(0)}{1 - rz^{-1}} \qquad |z| > |r| \tag{2}$$

$$=\frac{3}{1-3z^{-1}}\tag{3}$$

$$U(z) = \frac{1}{1 - z^{-1}} \qquad |z| > 1$$

Fig. 1. Stem plot of y(n)

$$y(n) = x(n) * u(n)$$
 (5)

$$Y(z) = X(z)U(z) \tag{6}$$

$$= \left(\frac{3}{1 - 3z^{-1}}\right) \left(\frac{1}{1 - z^{-1}}\right) \quad |z| > 3 \tag{7}$$