

19-11-24

Lab-08

⇒ First order logic ⇒ Unification

⇒ Implement unification in first order logic

→ Finding a common substitution for variables in different terms to make them match.

⇒ Statements:

1) Every cat loves to chase mice

2) Tom is a cat

3) Jerry is a mouse

4) If someone loves to chase Jerry, they will try to catch Jerry

5) Jerry can run fast

6) If someone tries to catch a mouse that runs fast, they will fail to catch it

1) $\forall x (\text{cat}(x) \rightarrow \exists y (\text{Mouse}(y) \wedge \text{LovesToChase}(x, y)))$

2) $\text{Cat}(\text{Tom})$

3) $\text{Mouse}(\text{Jerry})$

4) $\forall x (\text{LovesToChase}(x, \text{Jerry}) \rightarrow \text{TriesToCatch}(x, \text{Jerry}))$

5) $\text{RunFast}(\text{Jerry})$

6) $\forall x \forall y ((\text{Mouse}(y) \wedge \text{RunFast}(y) \wedge \text{TriesToCatch}(x, y)) \rightarrow \text{FailsToCatch}(x, y))$

⇒ 7) Does Tom fail to catch Jerry?

FOL: $\text{FailsToCatch}(\text{Tom}, \text{Jerry})$

⇒ (i) From statement 2 and 1, we can infer

→ Since Tom is a cat, there exists some $y(\text{mouse})$ such that $\text{Mouse}(y) \wedge \text{LovesToChase}(\text{Tom}, y)$

(ii) Using statement 3 $\Rightarrow y = \text{Jerry}$

Conclusion $\Rightarrow \text{LovesToChase}(\text{Tom}, \text{Jerry})$

(iii) From statement 4 and the fact that $\text{LovesToChase}(\text{Tom}, \text{Jerry})$
 conclusion: $\text{TriesToCatch}(\text{Tom}, \text{Jerry})$

(iv) From statement 5 and 3, Jerry satisfies the conditions of statement
 Since, $\text{Mouse}(\text{Jerry})$, $\text{RunsFast}(\text{Jerry})$ and $\text{TriesToCatch}(\text{Tom}, \text{Jerry})$,
 we conclude $\Rightarrow \text{FailsToCatch}(\text{Tom}, \text{Jerry})$

$\rightarrow \therefore$ The unification is successful, and $\text{FailsToCatch}(\text{Tom}, \text{Jerry})$
 is true based on the knowledge base.

$\therefore (\text{mouse } x, \text{runs_fast } y, \text{tries_to_catch } z) \text{ is a fact}$
 $(\text{mouse } x, \text{runs_fast } y) \text{ is a fact}$

$\therefore (\text{fact}) \text{ is a fact}$

$\text{fact} - \text{mouse } x \text{ was}$

$\text{mouse } x \text{ was}$

$\text{fact} - \text{mouse } x \text{ was}$

$\text{fact} - \text{mouse } x \text{ was}$

$\therefore (\text{mouse } x, \text{runs_fast } y, \text{tries_to_catch } z) \text{ is a fact}$

$\text{fact} - \text{mouse } x \text{ was}$

$(\text{mouse } x, \text{runs_fast } y, \text{tries_to_catch } z) \text{ is a fact}$

$\text{fact} - \text{mouse } x \text{ was}$

$\therefore (\text{mouse } x, \text{runs_fast } y, \text{tries_to_catch } z) \text{ is a fact}$

$\text{fact} - \text{mouse } x \text{ was}$

(i) $\text{mouse } x \text{ was}$

(ii) $\text{mouse } x \text{ was}$

(iii) $\text{mouse } x \text{ was}$

(iv) $\text{mouse } x \text{ was}$

(v) $\text{mouse } x \text{ was}$

(vi) $\text{mouse } x \text{ was}$

(vii) $\text{mouse } x \text{ was}$


```

Knowledge-base = [
    { "type": "rule", "rule": " $\forall x \forall y (\text{Programmer}(x) \wedge \text{Project}(y) \rightarrow \text{WritesCodeFor}(x, y))$ " },
    { "type": "fact", "fact": "Programmer(Alice)" },
    { "type": "fact", "fact": "Project(Project x)" },
    { "type": "rule", "rule": " $\forall x \forall y (\text{WritesCodeFor}(x, y) = \text{AssignedTo}(x, y))$ " },
    { "type": "rule", "rule": " $\forall x \forall y (\text{AssignedTo}(x, y) \rightarrow \text{CanAccess}(x, y))$ " },
    { "type": "fact", "fact": "AssignedTo(Dob, Project x)" }
]

```

```

query = { "predicate": "canAccess", "arguments": [ "?", "Project x" ] }

```

```

def unify(kb, query):

```

```

    predicate = query["predicate"]

```

```

    target_project = query["arguments"][1]

```

```

    result = []

```

```

    for item in kb:

```

```

        if item["type"] == "rule" and predicate

```

```

            in item["rule"]:

```

```

                rule = item["rule"]

```

```

    if "AssignedTo(x, y)" is rule and "canAccess(x, y)" is rule:

```

```

    for fact in kb:

```

```

        if fact["type"] == "fact" and "AssignedTo"
           is fact["fact"]

```

```

fact_parts = fact["fact"].split("(")[1].strip("(").split

```

```

    person, project = fact_parts

```

```

    if project == target_project:

```

```

        result.append(person)

```

if result:

return f "The query '{query ['predicate']}'
({query ['arguments'] [0]}, {target-project})'
is unified: f, join (result) can access {target-project}."

else:

return f "The query '{query ['predicate']}'
({query ['arguments'] [0]}, {target-project})'
could not be unified with the knowledge base."

result = unify (knowledge_base, query)
print (result)

Output:-

The query 'Can Access?, Project^x' is unified: Bob can access Project^x

DM
26/4/21