

Grey WolfAlgorithm:-

Initialize the population of wolves (positions) randomly within the search space

Define the max no. of iterations (F) and population size (N)

Define the fitness function to evaluate solutions

Evaluate the fitness of each wolf in the population

Identify the alpha (best solution), beta (second-best) and delta (third-best) wolves

For $t = 1$ to T:

For each wolf i in the population:

For each dimension d :

$$A1 = 2 * a * rand() - a$$

$$C1 = 2 * rand()$$

$$D = \alpha = [C1 * x - \alpha[d], x - i[d]]$$

$$X2 = x - \beta[d] - A2 * D - \delta$$

$$A3 = 2 * a * rand() - a$$

$$C3 = 2 * rand()$$

$$D - \delta = C3 * x - \delta[d] - x - 1[d]$$

$$X3 = x - \delta[d] - A3 * D - \delta$$

$$x_i[d] = (x_i + x2 + x3) / 3$$

end for

end for

$$a = 2 - (2 * t / T)$$

Update alpha, beta and delta wolves based on fitness

Program :-

```
import numpy as np
def grey_wolf_optimizes (fitness_function, num_wolves,
    num_dimensions, max_iterations, bounds):
    lower_bound, upper_bound = bounds
    wolves = np.random.uniform (lower_bound, upper_bound,
        (num_wolves, num_dimensions))
    alpha, beta, delta = None, None, None
    fitness = np.array ([fitness_function (wolf) for wolf in
        wolves])
```

```
    sorted_indices = fitness.argsort ()
```

```
    alpha, beta, delta = wolves [sorted_indices [:3]]
```

```
    a = 2
```

```
    for iteration in range (max_iterations):
```

```
        for i in range (num_wolves):
```

```
            for d in range (num_dimensions):
```

```
                r1, r2 = np.random.rand (), np.random.rand ()
```

```
                A1 = 2 * a * r1 - a
```

```
                C1 = 2 * r2
```

```
                D_alpha = abs (C1 * alpha [d] - wolves [i, d])
```

```
                x1 = alpha [d] - A1 * D_alpha
```

```
                r1, r2 = np.random.rand (), np.random.rand ()
```

```
                A2 = 2 * a * r1 - a
```

```
                C2 = 2 * r2
```

```
                D_beta = abs (C2 * beta [d] - wolves [i, d])
```

```
                x2 = beta [d] - A2 * D_beta
```


$x1, x2 = np.random.rand(), np.random.rand()$

$A3 = 2 * a * x1 - a$

$C3 = 2 * x2$

$D_delta = abs(C3 * delta[d] - wolves[i, d])$

$x3 = delta[d] - A3 * D_delta$

$wolves[i, d] = (x1 + x2 + x3) / 3$

$wolves[i] = np.clip(wolves[i], lower_bound, upper_bound)$

$fitness = np.array([fitness_function(wolf) for wolf in wolves])$

$sorted_indices = fitness.argsort()$

$alpha, beta, delta = wolves[sorted_indices[:3]]$

$a = 2 - (2 * iteration / max_iterations)$

$best_solution = alpha$

$best_fitness = fitness_function(alpha)$

$return best_solution, best_fitness$

$if _name == _main:$

$def fitness_function(x):$

$return np.sum(x**2)$

$num_wolves = 30$

$num_dimensions = 5$

$max_iterations = 100$

$bounds = (-10, 10)$

$best_solution, best_fitness =$

$grey_wolf_optimizer(fitness_function, num_wolves,$

$num_dimensions, max_iterations, bounds)$

$print("Best solution:", best_solution)$

$print("Best fitness:", best_fitness)$

Outputs: Best solution: $[-7.85e^{-11}, -7.36e^{-12}, -8.765e^{-12},$
 $8.354e^{-12}, 8.366e^{-12}]$

Best fitness: $3.3249e^{-22}$