

CS 372/469 – Spring 2022

Lab 4

Due: 04/17/2022 11:59 pm

For each of the following questions, write a successful running code in any programming language that you prefer. Your code should run without any errors for any *valid* input.

All problems are borrowed from GeeksForGeeks.

Question 1 (30 points):

The goal of this question is to implement the Fractional Knapsack problem. The more popular 0-1 Knapsack problem (https://en.wikipedia.org/wiki/Knapsack_problem) will be part of Lab 5.

Given weights and values of n items, we need to put these items in a knapsack of capacity W to get the maximum total value in the knapsack. In the Fractional Knapsack problem, we can break items for maximizing the total value of knapsack.

Source (Open at your own risk – solution is also on this page):

<https://www.geeksforgeeks.org/fractional-knapsack-problem/>

Input and Output Example (from the above source):

Input will include Items as (value, weight) pairs and Knapsack capacity W
{ {60, 10}, {100, 20}, {120, 30} }, $W = 50$

Output:

Maximum possible value = 240

Items to take full: :Item 1, 2

Items to take partially: 0.66 Item 3

Here, Item 1 is the first item in the list, i.e. {60, 10}, and so on.

Your code should be able to traverse the above input format (e.g. { {60, 10}, {100, 20}, {120, 30} }, $W = 50$) **from a given text file.**

Your algorithm must have a time complexity of $O(n \log n)$

Question 2 (35 points):

The goal of this question is to implement Kruskal's Minimum Spanning Tree algorithm. You have to use the code for detecting a cycle that you wrote for Lab 2 (aka do not blindly copy from the solutions).

Source (Open at your own risk – solution is also on this page):

<https://www.geeksforgeeks.org/kruskals-minimum-spanning-tree-algorithm-greedy-algo-2/>

Input and Output Example (modified from the above source):

Input: $n = 5$, $e = 9$

$A \rightarrow B (4)$, $B \rightarrow C (3)$, $C \rightarrow B (1)$, $B \rightarrow D (2)$, $B \rightarrow E (3)$, $C \rightarrow E (5)$, $E \rightarrow D (1)$, $A \rightarrow C (2)$, $C \rightarrow D (4)$

Output (this is the format of the Output --- not the actual output of this example):

The MST will include the following edges:

$A \rightarrow B (4)$, $B \rightarrow C (3)$, $C \rightarrow B (1)$

The total cost of the MST is 8.

Your code should be able to traverse the above input format (e.g. $A \rightarrow B (4)$, $B \rightarrow C (3)$, $C \rightarrow B (1)$, $B \rightarrow D (2)$, $B \rightarrow E (3)$, $C \rightarrow E (5)$, $E \rightarrow D (1)$, $A \rightarrow C (2)$, $C \rightarrow D (4)$) **from a given text file** and create edges and its weights in your data structure.

Your algorithm must have a time complexity of $O(E \log E)$ or $O(E \log V)$

Question 3 (35 points):

The goal of this question is to get practice at job scheduling algorithms.

There are n servers. You are given 2 arrays, $A1$ and $A2$. Array $A1$ contains information about amount of requests for each server. Hence, each server i is currently processing $A1[i]$ amount of requests. There is another array $A2$ in which $A2[i]$ represents the number of incoming requests that are scheduled to server i . Reschedule the incoming requests in such a way that each server i

holds an equal amount of requests after rescheduling. An incoming request to server i can be rescheduled only to server $i-1$, i , $i+1$. If there is no such rescheduling possible then output -1 else print number of requests hold by each server after rescheduling.

Source (Open at your own risk – solution is also on this page):
<https://www.geeksforgeeks.org/schedule-jobs-server-gets-equal-load/>

Input and Output Example (from the above source):

Input : $A1 = \{6, 14, 21, 1\}$

$A2 = \{15, 7, 10, 10\}$

Output : 21

$A2(0)$ scheduled to $a(0) \rightarrow a(0) = 21$

$A2(1)$ scheduled to $a(1) \rightarrow a(1) = 21$

$A2(2)$ scheduled to $a(3) \rightarrow a(3) = 11$

$A2(3)$ scheduled to $a(3) \rightarrow a(3) = 21$

$A1(2)$ remains unchanged $\rightarrow a(2) = 21$

Input : $A1 = \{1, 2, 3\}$

$A2 = \{1, 100, 3\}$

Output : -1

No rescheduling will result in equal requests.

Your algorithm must have a time complexity of $O(n)$

Submission Instructions: Put all your solutions in a properly commented file named *lab4_lastname_firstname.EXTENSION*, where EXTENSION = the appropriate extension for the programming language that you chose.