

Assignment = 9

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~~Ex~~

$$1. \quad T(n) = 2T\left(\frac{n}{2}\right) + n \Rightarrow \begin{array}{ll} a=2 & k=1 \\ b=2 & p=0 \end{array}$$

$$\log_2^2 = 1 = k \quad (\text{case 2})$$

$$p > -1 \rightarrow \Theta(n \cdot \log((1+1) \cdot n)) = \Theta(n \log n)$$

$$2. \quad T(n) = 2T\left(\frac{n}{2}\right) + n \log n \Rightarrow \begin{array}{ll} a=2 & k=1 \\ b=2 & p=1 \end{array}$$

$$\log_2^2 = 1 = k \quad (\text{case 2})$$

$$p > -1 \rightarrow \Theta(n \cdot \log((1+1) \cdot n)) \rightarrow \Theta(n \log 2n)$$

$$3. \quad T(n) = 2T\left(\frac{n}{2}\right) + n^2 \Rightarrow \begin{array}{ll} a=2 & k=2 \\ b=2 & p=0 \end{array}$$

$$\log_2^2 = 1 < k \quad (\text{case 3}).$$

$$p > 0 \rightarrow \Theta(n^2)$$

$$4. \quad T(n) = 8T\left(\frac{n}{2}\right) + n^2 \Rightarrow \begin{array}{ll} a=8 & k=2 \\ b=2 & p=0 \end{array}$$

$$\log_2^3 = 3 > k (k=2) \quad (\text{case 1})$$

$$\Theta(n^3)$$