# Thermodynamics Water Heating System

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### Abstract

A solar collector is a device that captures the energy of the sun's rays and converts it into heat. It typically consists of a flat or curved panel made of a material that can absorb sunlight, such as metal or glass. The absorbed energy is then transferred to a fluid, such as water or air, which is then circulated through a system to provide heat or hot water for a building or home. Solar collectors are typically more effective in areas with high levels of sunlight and are commonly used for domestic hot water and space heating.

A thermodynamic water heating system on the other hand is an innovative technology that uses the principles of thermodynamics to efficiently heat water. The system consists of a compressor, a heat exchanger, and a refrigerant fluid that circulates through a closed loop. The refrigerant fluid absorbs heat from the surrounding environment, which is then transferred to the water via the heat exchanger. This process allows the system to provide hot water even in low ambient temperatures, making it a reliable and cost-effective alternative to traditional water heating systems. We have the tried and tested to design a reliable, efficient and cost-effective thermodynamic water heating system that can work in any weather conditions. We have developed a comprehensive thermodynamics water heating system incorporating thermodynamic solar panel, condenser, compressor, valve, pump, etc.

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#### 1 Introduction

This report aims to provide an overview of thermodynamic solar systems, their functionality, and the potential benefits they offer. The report will examine the technology behind these systems, how they work, and the different types of applications for which they can be used. Additionally, the report will consider the economic and environmental advantages of utilizing thermodynamic solar systems in buildings, including reduced energy costs and carbon emissions.

The use of renewable energy sources has become increasingly important in recent years, as concerns about climate change and rising energy costs continue to grow. Thermodynamic solar systems offer a promising solution for sustainable energy generation and can significantly reduce a building's reliance on traditional energy sources. With this report, we hope to provide readers with a comprehensive understanding of thermodynamic solar systems and encourage wider adoption of this innovative technology.

#### 2 Literature Survey

We read a litraure on energy balance calculation for a heat exchanger, From the article we got idea about the concepts of heat exchangers and basic energy balance calculations. Energy balance calculation involves accounting for the energy inputs and outputs of the heat exchanger, and determining the heat transfer rate.

The article explains the two basic types of energy balance calculations: the overall energy balance and the individual energy balance. The overall energy balance considers the entire heat exchanger as a single entity, while the individual energy balance considers each section of the heat exchanger separately.

The document given in the reference table contains a technical data sheet for R407C, a refrigerant used as a replacement for R22 in refrigeration and air conditioning systems. It provides detailed information on the physical and thermodynamic properties of the refrigerant, its chemical composition, and compatibility with different materials and lubricants. The document also includes information on the safety and handling of R407C. It concludes by summarizing the key properties and advantages of R407C as a replacement for R22 in refrigeration and air conditioning systems.

The document is a brochure for the Arctic Open Frame compressor series, which are compressors designed for industrial and commercial refrigeration applications. The brochure introduces the series and its features, provides an overview of the different models and their specifications, and highlights the advanced technology used in the compressors. The brochure also includes information on installation and maintenance, and concludes by emphasizing the benefits of choosing the Arctic Open Frame compressor series for its energy efficiency, reliability, and advanced technology. Now, we

are describing about the technology.

#### 2.1 Solar Water Heater

Traditional collectors that heat a refrigerant or water directly, are used in solar hot water systems. The water or refrigerant can be moved through the system passively using gravity or actively through a controller pump. These collectors need full sunshine. Because SAHPs have a compressor, which pressurizes and concentrates the heat in the gaseous refrigerant, and a thermal exchange valve, which controls how quickly the refrigerant flows through the evaporator to maximize the extraction of energy, they are more efficient.

#### 2.2 Thermodynamic solar panels

Unlike conventional solar panels, thermodynamic solar panels operate on a different principle. Thermodynamic solar panels employ a thermodynamic cycle to produce electricity, contrary to conventional solar panels, which use the photovoltaic effect to convert sunlight directly into electricity.

A heat pump, which draws heat from the air, water, or ground, initiates the process. After that, this heat is transferred to a working fluid, like a refrigerant. A pressure difference caused by the working fluid expanding as it warms up drives a turbine. Electricity is produced by the turbine and can either be used right away or stored in batteries for later use.

As long as there is a temperature difference between the heat source and the environment, the heat pump will continue to operate and generate energy. The heat pump enables thermodynamic solar panels to produce energy even under low-light scenarios, in contrast to conventional solar panels that need direct sunlight to function.

Thermodynamic solar panels do not require placement in direct sunlight, unlike photovoltaics or conventional thermal solar panels. They may draw heat from the surrounding air as well as absorb heat from direct sunlight. Consequently, despite the fact that thermodynamic solar panels are technically solar panels, they resemble air source heat pumps more in some ways. The caveat here is that if you live in a cold region, they will likely perform optimally in full sunlight because the ambient air temperature may not be warm enough to satisfy your home's heating demands. Thermodynamic solar panels can be installed on roofs or walls, in full sun, or in complete shade.

Thermodynamic solar panels, in contrast to solar hot water systems, are still an emerging technology and have not undergone as much testing. The effectiveness of thermodynamic solar panels was tested in 2014 in Blyth, United Kingdom, by a single autonomous lab, Narec Distributed Energy. The experiments were conducted from January to July in Blyth, which has a reasonably temperate climate with a lot of

rainfall.

The results indicate when the heat lost from the heat-exchanging tank is taken into account the thermodynamic SAHP system's coefficient of performance, or COP, is 2.2. When heat pumps attain COPs above 3.0, they are often regarded as being highly efficient. This study showed that thermodynamic solar panels weren't very effective in 2014 in a moderate climate, but they are more effective in warmer regions. Furthermore, given how far advances in technology have come, a fresh unbiased investigation of thermodynamic solar panels is certainly necessary.

#### 2.3 Advantages of Thermodynamic Solar Panels

One of the main advantages of thermodynamic solar panels is their ability to generate electricity in low-light conditions. This makes them ideal for use in areas with long, dark winters or in locations where sunlight is scarce.

Another advantage is their ability to generate electricity even when the temperature is low. Traditional solar panels become less efficient as the temperature drops, but thermodynamic solar panels continue to produce electricity as long as there is a temperature difference between the source of heat and the environment. This makes them ideal for use in cold climates or at high altitudes.

Thermodynamic solar panels also have a higher energy density than traditional solar panels. This means that they can produce more electricity per unit of surface area, making them ideal for use in space-constrained applications.

Finally, thermodynamic solar panels can generate electricity at night by using heat stored in the thermal mass of the system. This means that they can provide a continuous source of electricity, even when the sun is not shining.

#### 2.4 Disadvantages of Thermodynamic Solar Panels

While thermodynamic solar panels have many advantages, they also have some disadvantages. One of the main disadvantages is their cost. Thermodynamic solar panels are more complex and expensive to install than traditional solar panels. They require a heat pump, which can be expensive to operate, and the system must be carefully designed to ensure maximum efficiency.

Another disadvantage is that they require a constant energy source to drive the heat pump. This means that they are not entirely self-sufficient and cannot generate electricity when the energy source is not available.

Finally, thermodynamic solar panels are less efficient than traditional solar panels under optimal conditions. While they are more efficient in low-light and low-temperature conditions, they are less efficient than traditional solar panels when the sun is shining brightly.

# 2.5 Cost-Effective Water Heating Using Thermodynamic Panels

A straightforward way to lower heating and gas bills is to install a thermodynamic water heating system. Only a heat collector panel and a compressor require to be installed and linked to your pre-existing hot water tank, and the system becomes fully operational.

The thermodynamic panel's technique is based on basic heat exchange. Similar to air-to-water heat pumps, household hot water is heated in a tank by transferring heat from the surrounding air through a specific working fluid and a compressor. As a result, your kitchen and bathroom sinks, tubs and pools, and other appliances now have a very affordable source of hot water.

#### 2.6 How Much Do Thermodynamic Panels Cost?

The thermodynamic cost of the panel, its components, and installation for a fourperson family is a reasonable £5,000 to £6,000. The method guarantees a consistent return rate over time with minimal to no maintenance costs.

Only the compressor of the thermodynamic water heating system requires electricity, therefore operating costs are likewise minimal. The compressor consumes 360 watts per hour under normal circumstances, which is comparable to the use of a bigger refrigerator. The compressor's energy consumption, however, varies continually with the weather, time of day, month, and water use, yet it always operates efficiently.

Typically, the compressor usage only costs £8–10 per month, or £96–120 per year, with a typical domestic hot water demand. Even intensive use, such as running the thermodynamic heating system constantly, would only cost £14 per month or £168 per year. The operating costs might theoretically be eliminated if a solar panel was employed in addition to the thermodynamic panels to produce the necessary electricity.

The weekly electricity usage can be reduced below £4 a month or £48 a year without much trouble if the compressor is configured to only run during specific hours, such as when the ambient air is the hottest (11 am to 5 pm).

# 2.7 Savings with Thermodynamic Panels Compared with Other Heating Systems

The unit price, installation expenses, and running costs are calculated, and the savings from installing thermodynamic panels are shown in the accompanying table 2.

#### 2.8 What Maintenance Is Required?

Thermodynamic water heating systems require minimum maintenance due to the straightforward, environmentally friendly product design. There is no requirement for refilling because the refrigerant fluid cycles in a closed cycle and does not deteriorate over time.

One or two check-ups every ten years would be sufficient to keep the system in good working order over the long term. If the compressor breaks down, it can be repaired or replaced for a price starting at £150.

The system's water tank should be maintained similarly to other water tanks: Depending on how hard the water is, it needs to be flushed anywhere from once a year to every few months. To avoid the accumulation of limescale, this needs to be done.

Depending on the weather, the thermodynamic panels themselves might need to be cleaned occasionally. They don't need any special cleaning products, and washing merely serves to keep objects away from the panel so that it can perform as effectively as possible by receiving the full ambient temperature. If frequent precipitation is received the panels are cleansed, this step is not necessary.

As a result, thermodynamic water heating is a great way to cut your expenses and carbon footprint without having to spend a lot of time or money maintaining the system—it will always be there for you.

#### 3 Problem Statement

The thermal solar collectors are highly effective at generating heat energy from the sun's radiation on hot and sunny days. However, these collectors become completely inefficient when there is no sun, such as on cloudy or rainy days, during the nighttime, or in regions with low sunlight intensity. This limits their usability as a reliable source of heat energy throughout the year and in areas with varying weather patterns. As a result, there is a need to find alternative or supplementary sources of heat energy that can be used in conjunction with thermal solar collectors to ensure a consistent and reliable supply of heat energy.

#### 4 Working Principle

A thermodynamic solar panel system involves capturing heat energy from the surrounding air and converting it into usable thermal energy. The system works through a closed loop circuit that contains a fluid, usually a refrigerant or heat transfer fluid, that is circulated through a thermodynamic solar panel, a compressor, a heat exchanger, and an expansion valve.

The thermodynamic solar panel consists of a heat collector plate that absorbs heat from the air, even in the absence of direct sunlight, through natural convection. The fluid in the closed loop circuit is then circulated through the heat collector plate, where it absorbs the heat energy and evaporates.

The evaporated fluid then travels to the compressor, where it is compressed, increasing its pressure and temperature. The hot, pressurized fluid is then passed through a heat exchanger, where the heat is transferred to water or another medium that can be used for space heating, hot water supply, or industrial processes.

After releasing the heat energy, the fluid is passed through an expansion valve, where its pressure and temperature drop, causing it to revert to its liquid state. The liquid fluid then travels back up to the thermodynamic solar panel, where the cycle begins again.

The system can capture heat energy from the air regardless of weather factors, making it highly efficient and reliable. The thermodynamic principles behind this system allow it to operate efficiently even in low-temperature environments, making it suitable for a wide range of applications in various industries, including hotels, hostels, sports complexes, hospitals, and more.

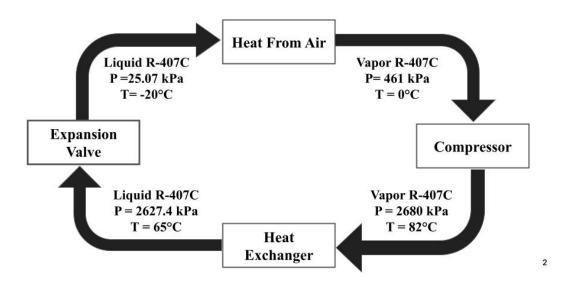


Figure 1: Flow Diagram

(Derived using Figure 14)

#### 5 Coolant R-407C

It is a zeotropic mixture of 1,1,1,2-tetrafluoroethane  $(CF_3CH_2F)$ , pentafluoroethane  $(CF_3CHF_2)$ , and difluoromethane  $(CH_2F_2)$ .

- R407C has a better Coefficient of Performance in tightly sealed systems than R134a because it operates at a higher pressure.
- Direct expansion air conditioning systems and residential & light air conditioning are both suited for R407C. In refrigeration systems for medium temperatures, it is also utilised.
- Refrigerant R407C has a good energy efficiency ratio as well as a low compression pressure and Global Warming Potential(GWP).

| Molecular Weight (kg/kmol)                    |       |  |  |  |
|---|-------|--|--|--|
| Boiling point ${}^{\circ}C$ at 1 atm pressure |       |  |  |  |
| Saturated liquid density (25°C), $kg/m^3$     | 1138  |  |  |  |
| Saturated vapour density (25°C), kg/m3        |       |  |  |  |
| Critical temperature (°C)                     |       |  |  |  |
| Critical pressure, bar                        | 46.3  |  |  |  |
| Liquid heat capacity @ 25°C, (kJ/(kg·K))      | 1.533 |  |  |  |
| Vapour heat capacity @ 1.013 bar (kJ/(kg·K))  | 1.107 |  |  |  |

Table 1: Properties of R-407C

#### 6 Results and Discussion

#### 6.1 Heat Exchanger

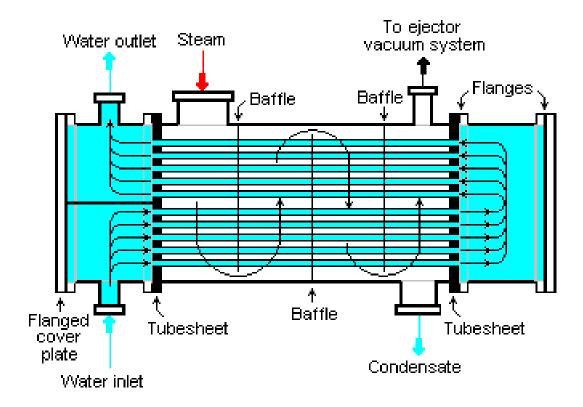


Figure 2: Condenser https://www.researchgate.net/figure/Desalination-process-and-heat-exchanger-condenser  $fig3_221926191$ 

A heat exchanger is a device designed to transfer heat from one fluid to another while keeping them separated by a wall. In chemical processes, it's essential to calculate the heat balance by adding or removing heat via exchangers with hot and cold process streams.

The energy balance equation is a useful tool to determine the heat transfer rate  $(\dot{Q})$  if you know the mass flow rates, specific heat capacities, and inlet and outlet temperatures of the two fluid streams. Similarly, it can help calculate the outlet temperatures of the fluid streams if you have the heat transfer rate and inlet temperatures.

The energy balance equation can be used to determine the heat transfer rate  $(\dot{Q})$  if the mass flow rates, specific heat capacities, and inlet and outlet temperatures of the two fluid streams are known. It can also be used to determine the outlet temperatures of the fluid streams if the heat transfer rate and the inlet temperatures are known.

#### 6.1.1 Design Calculation

We have assumed  $60,000\frac{Kg}{h}$  of water is flowing in tube side of a horizontal condenser. The coolant vapor enter the condenser saturated at  $82^{\circ}C$  and condensation will be completed at  $65^{\circ}C$ . Water is available from  $0^{\circ}C$  to  $56^{\circ}C$ . The vapor are to be totally condensed. Using **Triangular Pitch** arrangement, starting design assuming overall heat coefficient =  $575\frac{W}{m^2 \circ C}$  and we are optimizing the computation until U(Overall heat transfer coefficient) will be within  $\pm 30\%$  range.

Now, from the given upper information we are calculating heat duty  $(\dot{Q})$ 

$$\dot{Q} = \dot{m}C_p \Delta T \tag{1}$$

Where,

 $\dot{m}$  is mass flow rate of water

 $C_p$  is molar heat capacity of water is  $4.18 \frac{kJ}{kq}^{\circ}$ 

 $\Delta T$  is  $56^{\circ}C$ .

So, we get  $\dot{Q} = 3,901.33 \text{ kW}$ 

After that, we have calculated  $\Delta T_{LMTD}$  and corrected  $\Delta T_{LMTD}$  by using  $F_t$  correction factor:

$$\Delta T_{LMTD} = \frac{\Delta T_1 - \Delta T_2}{ln\frac{\Delta T_1}{\Delta T_2}} \tag{2}$$

$$\Delta T_{LMTD} = \frac{(82 - 56) - (65 - 0)}{ln\frac{82 - 56}{65 - 0}} \tag{3}$$

Now, using 3 we got  $\Delta T_{LMTD} = 42.56^{\circ}C$ 

We have to calculate R and S for the given temperature difference to find out  $F_t$  correction factor from the graph.

$$R = \frac{T_1 - T_2}{t_2 - t_1} = 0.30 \tag{4}$$

$$S = \frac{t_2 - t_1}{t_2 - t_1} = 0.68 \tag{5}$$

From graph, we got  $F_t = 0.91$ 

So, corrected  $\Delta T_{LMTD}$  is  $F_t * \Delta T_{LMTD}$  i.e. 0.91 \* 42.56 = 38.72°C

We have assumed that overall heat coefficient  $U_{assumed} = 575 \frac{W}{m^2 {}^{\circ}C}$ 

Now, we calculated overall area:

$$OverallArea = \frac{\dot{Q}}{U_{assumed} * \Delta T_{LMTD}} = 175.18m^2$$
 (6)

Surface area of a tube =  $\pi d_o L_{effective}$ 

Where, tube dimension:

 $d_o = 20mm = 0.78inch$ 

 $d_i = 16.8mm = 0.66inch$ 

$$L = 4.88m = 6feet$$

So, surface area of one tube is  $0.30m^2$ 

Now, the total number of tubes:

$$\frac{OverallArea}{SurfaceArea of one tube} \approx 580 \tag{7}$$

Tube bundle diameter Calculation:

$$Tube bundle diameter = d_o(\frac{Total Number of tubes}{k_1})^{\frac{1}{n_1}} = 671.01$$
 (8)

Clearance = 17 mm (Fixed and U tube)

Shell diameter = Tube Bundle Diameter + Clearance Area = 688.01 mm

Now, calculating the value of  $\frac{L}{D_s}$  which is equal to  $\frac{4.88}{0.688} \approx 7.09$ .

So, it's in between 5 and 10 and according to rule of thumb we can proceed further.

#### **Tube Side Coefficient Calculation**

 $T_{water_{mean}} = 28^{\circ}C$ 

Tube cross sectional area:

$$\frac{\pi}{4} * 16.8^2 = 221.67mm^2 \tag{9}$$

Number of tubes per pass:

$$\frac{580}{2} = 290\tag{10}$$

So, total tube cross section area:

$$290 * 221.77 = 64284.52mm^2 = 0.064284m^2 \tag{11}$$

Tube velocity:

$$\frac{Massflowrate}{Density * Cross section area of pass} = 0.26 \frac{m}{s}$$
 (12)

But velocity should be between 1.0 to 2.5. So we have to increase tube passes from 2 to 4 keeping shell pass unchanged and in this case  $F_t$  will not change. Bundle diameter will change. We have to take  $K_1$  and  $n_1$  values as 0.175 and 2.285 respectively.

BundleDiameter = 
$$d_o(\frac{N_1}{K_1})^{\frac{1}{n_1}} = 694.51mm = 0.6945m$$
 (13)

Clearance = 17mm and Shell Diameter = 711.51 mm. So,  $L/D_S = 6.86$  which is

lie between 5 to 10. So, it has no issues.

Number of tubes per pass:

$$\frac{580}{4} = 145\tag{14}$$

Total tube cross section area =  $0.032142 \ m^2$ 

Tube velocity = 0.522 m/s using all above details and it is not coming in the range. Now increasing to tube passes from 4 to 6, keeping shell pass unchanged.

Bundle Diameter:

$$20(\frac{582}{0.0743})^{\frac{1}{2.499}} = 723.14mm \tag{15}$$

For this bundle diameter we  $k_1 = 0.0743$  and  $n_1 = 2.499$ 

Clearance = 19 mm

Shell diameter = 723.14 mm

$$\frac{L}{D_S} = \frac{4.88}{0.742147} = 6.57\tag{16}$$

it is in the range of 5 to 10.

Number of tubes fer pass:

$$\frac{582}{6} = 97\tag{17}$$

Cross sectional area of all tubes:

$$91 * 221.67mm^2 = 21501.99mm^2 = 0.02150199m^2$$
 (18)

Tube velocity:

$$\frac{60,000}{360*993*0.021501} \frac{m}{s} = 0.7806 \frac{m}{s} \tag{19}$$

Now, increase the tubes 6 to 8 keeping shell unchanged.

Bundle Diameter:

$$20\left(\frac{584}{0.0365}\right)^{\frac{1}{2.675}} = 745.87mm\tag{20}$$

Clearance = 17 mm

Shell Diameter = 764.87 mm

$$\frac{L}{D_s} = \frac{4.88}{0.764} = 6.30\tag{21}$$

It's in the range of 5 to 10.

Number of tubes per pass:

$$\frac{584}{8} = 73\tag{22}$$

So, Total cross-sectional area of all tubes:

$$73 * 221.67mm^2 = 16181.91mm^2 = 0.16181m^2 \tag{23}$$

Tube Velocity:

$$\frac{6000}{3600 * 993 * 0.16181} = 1.03$$

We are proceeding with this value.

Now, calculating inner heat transfer coefficient:

$$h_i = \frac{4200(1.35 + 0.02t)(u_t)^{0.5}}{(d_i)^{0.2}}$$
(25)

$$=\frac{4200(1.35+0.02*28)(1.03)^{0.5}}{(16.8)^{0.2}}$$
(26)

$$=4630.622 \frac{W}{m^{2} {}^{\circ}C} \tag{27}$$

#### **Shell Side Coefficient Calculation**

Number of tubes in entire row:

$$N_r = \frac{D_b}{P_t},\tag{28}$$

$$P_t' = 0.87 * P_t \tag{29}$$

$$N_r = \frac{745.87}{0.87 * 1.25 * 20} = 34.29 \approx 34 \tag{30}$$

$$N_r' = \frac{2}{3}N_r = 22.66 \tag{31}$$

Heat Capacity( $\dot{Q}$ ):

$$\dot{Q} = W_C * (Enthalpy of coolent vapour - Enthalpy of coolent liquid)$$
 (32)

$$W_C = \frac{\dot{Q}}{Enthalpyof coolent vapour - Enthalpyof coolent liquid}$$
(33)

$$W_C = \frac{3907.866}{(423 - 314.6)} = 36.05 \frac{kg}{s} \tag{34}$$

Tube Loading:

$$T_H = \frac{W_c}{L_{eff} * N_t} \tag{35}$$

$$= \frac{36.05}{(4.88 - 0.05) * 584} = 0.012 \frac{kg}{s.m}$$
 (36)

Now, calculating outer heat transfer coefficient:

$$h_o = 0.95 * K_L * \left[ \frac{g * \rho_L * (\rho_L - \rho_V)}{\mu_L * T_H} \right]^{\frac{1}{3}} * N_r^{,-1/6}$$
(37)

Where, 
$$\rho_L = 833.8 \frac{kg}{m^3}$$
  
 $\rho_v = 194.2 \frac{kg}{m^3}$   
 $\mu = 95.96 * 10^{-6} Pa.s$ 

$$h_o = 0.95 * 0.13 * \left[ \frac{9.81 * 833.8 * (833.8 - 194.2)}{95.96 * 10^{-6} * 0.01278} \right]^{\frac{1}{3}} * 22.666^{-1/6}$$
(38)

$$h_o = 1194.68 \frac{W}{m^2 {}^{\circ}C} \tag{39}$$

#### Overall Heat Transfer Coefficient

$$\frac{1}{U_o} = \frac{1}{h_o} + \frac{1}{coefficienth_o} + \frac{d_o * \ln \frac{d_o}{d_i}}{2K_w} + \frac{d_o}{d_i} * \frac{1}{coefficienth_i} + \frac{d_o}{d_i} \frac{1}{h_i}$$
(40)

$$\frac{1}{U_o} = \frac{1}{1194.68} + \frac{1}{5000} + \frac{20}{16.8} \left[ \frac{1}{4630.6222} + \frac{1}{4500} \right] \tag{41}$$

$$\frac{1}{U_0} = 0.00155868\tag{42}$$

$$U_o = 641.56 \frac{W}{m^{2} \circ C} \tag{43}$$

$$Error = \frac{641.5685 - 575}{575} = 11.57\% \tag{44}$$

Error is 11.57% which is acceptable.

#### Tube Side Pressure Drop

$$\Delta P_t = N_p \left[8j_f \frac{L}{d_i} \left(\frac{\mu}{\mu_w}\right)^{-0.14} + 2.5\right] \frac{\rho \mu_t^2}{2} (45)$$

$$R_e = \frac{\rho \mu_t d_i}{\mu} \tag{46}$$

$$R_e = \frac{999 * 1.03 * 16.8 * 10^{-3}}{0.6 * 10^{-3}} = 28638.12$$
 (47)

 $j_f = 3.8 * 10^3$ , putting vlues of  $R_e$  and  $j_f$  in equation 45

$$\Delta P_t = 4[8 * 3.8^{-3} \frac{4.88}{0.016} + 2.5] \frac{993 * 1.03^2}{2}$$
(48)

$$\Delta P_t = 23872.71 \frac{N}{m^2} = 23.872kPa \tag{49}$$

#### Shell Side Pressure Drop

Baffle spacing = Shell diameter

$$G_s = \frac{129781.5}{3600} * \frac{1}{A_s} = 308.83 \frac{kg}{s.m^2} \tag{50}$$

Where,

$$A_s = \frac{P_t - D_o}{P_t} * D_s * BaffleSpacing$$
 (51)

$$A_s = \frac{1.25d_o - d_o}{1.25d_o} * D_s^2 \tag{52}$$

Where,  $D_s = 0.764$  m. So, Value of  $A_s$  is 0.1167392  $m^2$ .

$$d_e = \frac{1.1}{d_o} [P_t^2 - 0.917d_o^2] \tag{53}$$

Where,  $P_t = 25$  mm and  $d_o = 20$  mm, So value of  $d_e = 0.014201$  m.

$$R_e = \frac{G_s d_e}{\mu} \tag{54}$$

By using, value of  $G_s$  and  $d_e$  we got  $R_e = 548220.72$ ,  $\rho_t = 2.7 * 10^{-2}$  (25% baffle cut)

$$\mu_s = \frac{G_s}{\rho_v} = 1.59 \frac{m}{s} \tag{55}$$

$$\Delta P_s = 8 * j_t * \frac{D_s}{d_e} \frac{L_{eff}}{L_B} * \frac{\rho * \mu^2}{2} \left(\frac{\mu}{\mu_w}\right)^{0.14}$$
 (56)

$$\Delta P_s = 8(2.7 * 10^{-2}) * \frac{0.764}{0.014201} \frac{4.88 - 0.05}{0.764} * \frac{194.2 * 1.59^2}{2} = 18034.139 Pa$$
 (57)

Taking 50% of  $\Delta P_s$  for vapour velocity:

$$\Delta P_s = \frac{18034.139}{2} = 9017.06Pa \tag{58}$$

#### 6.2 Compressor

An air compressor is a type of mechanical device that increases gas pressure by reducing its volume. Among gas compressors, air compressors are a commonly used variety.

While pumps and compressors share the common feature of increasing fluid pressure and moving it through a pipe, the key distinction is that compressors alter the density or volume of gases, which is generally not feasible with liquids due to their limited compressibility. For this reason, compressors are frequently utilized for gases.

Scroll compressors are increasingly being used in heating, ventilation, and air conditioning (HVAC) systems since they are more dependable and efficient than reciprocating models. A scroll compressor consists of two scrolls: a fixed scroll that remains stationary and a rotating scroll that rotates through a swing link. As the refrigerant

pockets between the two scrolls are gradually forced to the center of the scrolls, the gas volume decreases, and it is then discharged through the center port to the condenser.

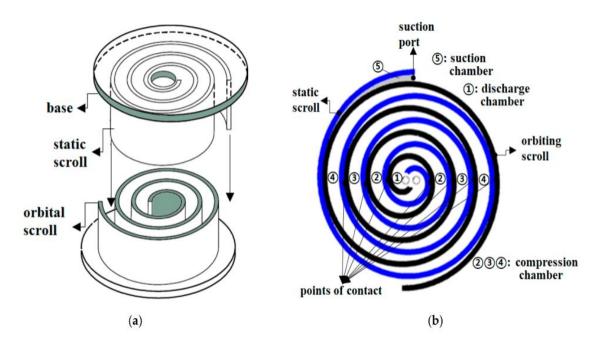


Figure 3: Schematic diagram of a scroll structure. (a) A scroll set. (b) the geometry of a scroll chamber

https://www.mdpi.com/1996-1073/13/15/3911

#### 6.2.1 Compressor Energy Calculation

Using Energy Equation,

Input - Output + Consumption = Accumulation

$$\dot{m} * C_p(T) * dT = d\dot{Q} \tag{59}$$

Here,

 $\dot{m} = \text{mass flow rate}$ 

 $C_p(T)$  = specific heat at constant pressure w.r.t temperature

dT = Change in Temperature

 $\dot{Q} = \text{Heat transfer per unit time}$ 

Integrating both sides, we get

$$\dot{m} * C_p(T) * \Delta T = \dot{Q} \tag{60}$$

$$\dot{m} * C_p(T) * (T_f - T_i) = \dot{Q}$$
 (61)

We Know ,  $\dot{m}=36~\mathrm{kg/sec}$   $C_p(T)=1.64~\mathrm{KJ/kgK}$  Initial Temperature(T<sub>i</sub>) = 0°C Oulet Temperature(T<sub>f</sub>) = 82°C So,After applying the Values, we get

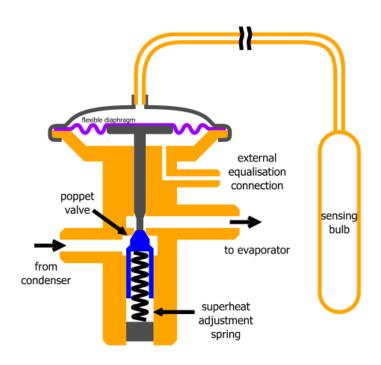
$$36 * 1.64 * (82 - 0) = \dot{Q}$$

$$\dot{Q} = 4857.423KJ/sec \tag{62}$$

#### 6.3 Expansion Valve

Expansion valves are mechanical devices employed in refrigeration systems to regulate the flow of refrigerant. Their primary function is to facilitate the conversion of liquid refrigerant at high pressure in the condensing unit to low-pressure gas refrigerant in the evaporator.

In refrigeration systems, the term "low side" refers to the section that operates at low pressure, while the term "high side" is used to describe the section that operates at high pressure.



#### 6.3.1 Expansion Valve Energy Calculation

Using Energy Equation,

Input - Output + Consumption = Accumulation

$$\dot{m} * C_p(T) * dT = d\dot{Q} \tag{63}$$

Here,

 $\dot{m} = \text{mass flow rate}$ 

 $C_p(T)$  = specific heat at constant pressure w.r.t temperature

dT = Change in Temperature

 $\dot{Q} = \text{Heat transfer per unit time}$ 

Integrating both sides, we get

$$\dot{m} * C_p(T) * \Delta T = \dot{Q} \tag{64}$$

$$\dot{m} * C_p(T) * (T_f - T_i) = \dot{Q}$$
 (65)

We Know,

 $\dot{m} = 36 \text{ kg/sec}$ 

 $C_p(T) = 1.53 \text{ KJ/kgK}$ 

Initial Temperature $(T_i) = 65^{\circ}C$ 

Oulet Temperature( $T_f$ ) =  $-20^{\circ}C$ 

So, After applying the Values,

we get

$$36 * 1.53 * ((-20) - 65) = \dot{Q}$$

$$\dot{Q} = -4193.66KJ/sec \tag{66}$$

#### 6.4 Thermodynamics Solar Panel

#### 6.4.1 Design Calculation

Here the inlet coolant is distributed into 4 pipes

Assuming the panel surface temperature equal to  $T_1$  as of the outer surface temperature of the pipe and the temperature at any point along the pipe is some over a length "d" perpendicular to the flow (mass flow coolant).

Now considering an element length "dx" along the pipe and heat transfer over the

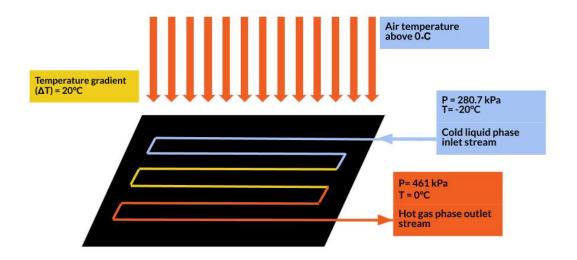


Figure 5: Thermodynamic Solar Panel Flow Diagram

area corresponding length "dx" is given by,

$$h_A * dx * d * (T_A - T_1) = \frac{2\pi k * dx * (T_1 - T_2)}{\ln \frac{r_o}{r_i}}$$
(67)

Here,  $H_A = \text{Air convective heat transfer coefficient}$ 

 $T_A = Air temperature$ 

k = Aluminium thermal conductivity

 $T_2 =$ Inner surface temperature of pipe

 $r_o = \text{Outer pipe radius}$ 

 $r_i = \text{Inner pipe radius}$ 

Considering worst case scenario  $T_A = 0$ °C, then we have

$$h_A * d * (-T_1) = \frac{2\pi k(T_1 - T_2)}{\ln \frac{r_0}{r_i}}$$
(68)

Heat transfer equation for inner pipe surface for coolant is given by,

$$\frac{2\pi k(T_1 - T_2)dx}{\ln\frac{r_o}{r_i}} = h_c * (2\pi r_i) * dx * (T_2 - T_c)$$
(69)

$$\frac{2\pi k(T_1 - T_2)}{\ln\frac{r_o}{r_i}} = h_c * (2\pi r_i) * (T_2 - T_c)$$
(70)

Here,  $h_c$  = Coolant convective heat transfer coefficient

 $T_c = \text{Coolant temperature}$ 

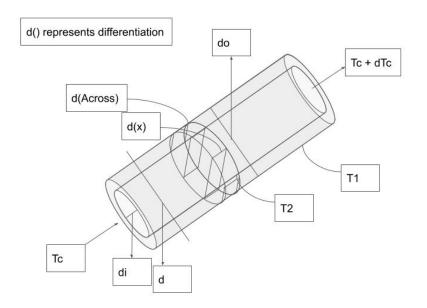


Figure 6: Schematic of a Single Pipe

From equation 68  $T_1 \& T_2$  are related by

$$T_1 = \frac{2\pi k T_2}{2\pi k + h_A d \ln \frac{r_o}{r_i}} = C_1 T_2 \tag{71}$$

Where

$$C_1 = \frac{2\pi k}{2\pi k + h_A d \ln \frac{r_o}{r_i}} \tag{72}$$

Now,  $h_c$  is dependent on temperature of coolant and is given by,

$$h_c = h'_{fc} + h'_{nb}$$
 (73)

$$h'_{fc} = h_{fc} * f_c \tag{74}$$

$$\frac{h_{fc} * d_i}{k_f} = J_h * Re * Pr^{0.33} * \frac{\mu}{\mu_w}^{0.14}$$
 (75)

Here,  $k_f =$  fluid (coolant) thermal conductivity

 $f_c = \text{Correction Factor}$ 

$$h'_{nb} = h_{nb} * f_s \tag{76}$$

 $f_s = \text{Factor}$ 

$$h_{nb} = 0.00122 * \frac{k_L^{0.79} * Cp_L^{0.45} * \rho_L^{0.49}}{\sigma^{0.5} \mu_L^{0.29} \lambda^{0.24} \rho_v^{0.24}} (T_2 - Tc)^{0.24} (P_2 - P_c)^{0.75}$$
(77)

Where

 $k_L = \text{Conductivity of coolant } W/m^{\circ}C$ 

 $Cp_L = \text{Liquid heat capacity } J/kg^{\circ}C$ 

 $\rho_L = \text{Liquid density } kg/m^3$ 

 $\mu_L = \text{Liquid viscosity } N.s/m^2$ 

 $\lambda = \text{Latent heat J/kg}$ 

 $\rho_v = \text{Vapour density } kg/m^3$ 

 $P_2 = \text{Saturated pressure corresponding to the } T_c \ N/m^2$ 

 $\sigma = \text{Surface tension } N/m$ 

From equation 70 we get

$$\frac{2\pi k(C_1 T_2 - T_2)}{\ln \frac{r_o}{r_i}} = h_c(2\pi r_i)(T_2 - T_c)$$
 (78)

$$T_2 = \frac{h_c * r_i * \ln \frac{r_o}{r_i}}{h_c * r_i * \ln \frac{r_o}{r_i} + k(1 - C_1)} T_c$$
 (79)

Now, since  $h_c = h_c(T_2 - T_s)$  (Function of temperature difference), therefore we use a good assumed temperature for  $T_2 = 0^{\circ}C$  & calculate  $h_c$  & then calculate  $T_{2new}$  using equation 79 and intering the above calculations for  $T_2 = T_{2new}$  until error between  $T_{2new}$  &  $T_2$  is less then 5%

We obtain temperature profile of  $T_2$  (wall temperature for a given temperature profile of  $T_c$ .

Now,

$$\dot{m}_c * C_p * dT_c + \lambda(d\dot{m}_c) = \frac{2\pi * k(T_1 - T_2) * dx}{\ln \frac{r_o}{r_i}} = \frac{2\pi * k(dx) * T_2(C_1 - 1)}{\ln \frac{r_o}{r_i}}$$
(80)

$$\int_{0}^{l} dx = \frac{\ln \frac{r_{o}}{r_{i}}}{2\pi k [C_{1} - 1]} \left[ \int_{-20^{\circ}c}^{0^{\circ}C} \frac{\dot{m}_{CL} * C_{PL} * (dT_{c})}{C_{2}T_{2}} + \int_{-20^{\circ}c}^{0^{\circ}C} \frac{\dot{m}_{CG} * C_{PG}(dT_{c})}{C_{2}T_{c}} + \int_{0}^{\dot{m}_{c}} \lambda (d\dot{m}_{CG}) \right]$$
(81)

From equation 79

$$C_2 = \frac{h_c r_i * \ln \frac{r_o}{r_i}}{h_c r_i \ln \frac{r_o}{r_i} + k(1 - C_1)}$$
(82)

And therefor we get required length "l" of the pipe

#### 6.4.2 Thermodynamic Panel Energy Calculations

Using Energy Equation, Input - Output + Consumption = Accumulation

$$\dot{m} * C_p(T) * dT + d\dot{m} * \lambda = d\dot{Q}$$
(83)

Here,

 $\dot{m} = \text{mass flow rate}$ 

 $C_p(T) =$  specific heat at constant pressure w.r.t temperature

dT = Change in Temperature

 $\lambda = \text{Latent Heat of Vapourisation}$ 

 $\dot{Q} = \text{Heat transfer per unit time}$ 

Integrating both sides, we get

$$\dot{m} * C_p(T) * \Delta T + \dot{m} * \lambda = \dot{Q} \tag{84}$$

$$\dot{m} * C_p(T) * (T_f - T_i) + \dot{m} * \lambda = \dot{Q}$$
(85)

We Know,

 $\dot{m} = 36 \text{ kg/sec}$ 

 $C_p(T) = 1.38 \text{ KJ/kgK}$ 

Initial Temperature $(T_i) = -20^{\circ}C$ 

Oulet Temperature( $T_f$ ) =  $0^{\circ}C$ 

 $\lambda = 248 \text{ KJ/kg}$ 

So, After applying the Values,

we get

$$36 * 1.38 * (0 - (-20)) + 36 * 248 = \dot{Q}$$
  
 $\dot{Q} = 992.188 + 8935.92$   
 $\dot{Q} = 9928.11KJ/sec$  (86)

#### 6.5 Expenditure

#### 6.5.1 Capital Expenditure(CAPEX)

For Thermodynamic Panel,

Price of each solar panel = 7500\$

So Cost of 20 solar panel = 150000\$

$$C_E = C_B * (\frac{Q}{Q_B})^M \tag{87}$$

For the compressor,

using appendix 15, we got

Base cost for 250 kW power = \$98400

So for 4857kW will be calculated using (equation 87)

where ,value of M = 0.46

Applying Values,

$$C_E = 98400 * \left(\frac{4857}{250}\right)^{(0.48)}$$

$$C_E = \$408733$$
(88)

For Heat exchanger, We get,

Base cost for  $80m^2$  heat transfer area =\$32800

For  $175.18m^2$  will be calculated using equation 87

where value of M=0.68

Applying Values,

$$C_E = 32800 * (\frac{175.18}{80})^{(0.68)}$$

$$C_E = \$56000$$
(89)

For thermostatic expansion valve,

We get that for our purpose the required expansion valve will cost around \$12000

Total Cost = \$150000 + \$408733 + \$56000 + \$12000 = \$626733

And piping and installation cost will be taken as 70% of total cost

Therefore, Cost of piping and installation =  $\$626733 * \frac{70}{100} = \$438713$ 

Final cost after piping =\$626733 + \$438713 = \$1065446

So, the Capital Expenditure of the process will be \$1065446

#### 6.5.2 Operational Expenditure(OPEX)

OPEX includes maintenance cost, electricity cost, pumping cost.

So, Maintenance cost is 6% of total capital expenditure

Therefore, Maintenance Cost = \$1065446 \*  $\frac{6}{100}$  = \$63927

For Electricity Cost,

Cost of per kWh in india is \$0.105

So, the cost for 1000kWh will be \$105

If the compressor is running for 8hr per day cost will be \$840

And it is running for 3months cost will be \$75600

For Pumping cost,

The cost for running pump for 3months and each day 8hr will be \$28800

Total Operational cost = \$28800 + \$75600 + \$63927

So, the Operational Expenditure of the process will be \$168327 for one year

#### 7 Conclusion

We have developed a comprehensive thermodynamics water heating system incorporating thermodynamic solar panel, condenser, compressor, valve, pump, etc. As it is a type of renewable energy technology that has gained popularity in recent years due to their energy efficiency and cost-effectiveness.

To begin, we are absorbing heat from the air using thermodynamic solar panel of dimensions (2m\*0.8m) to increase the temperature of coolant R407C from  $-20^{\circ}C$  to  $0^{\circ}C$ . Then we are compressing the coolant R407C using scroll compressor to increase the temperature and pressure from  $0^{\circ}C$  and 461kPa to  $82^{\circ}C$  and 2680kPa. Further, it passes to condenser where coolant is losing heat to heat up water of flow rate 62,000Kg/h and raising its temperature to  $56^{\circ}C$  which is the used for commercial use. After losing heat, coolant passes through expansion valve where the temperature and pressure is further decreased.

Overall, thermodynamic water heating systems are a reliable and sustainable way to provide hot water for residential and commercial use. They offer a great alternative to traditional heating systems and can help reduce our reliance on fossil fuels, saving money and reducing carbon emissions in the process.

#### 8 Future Scope

In the future, emerging technologies will continue to transform the water heating industry, enabling us to create more efficient, reliable, and sustainable systems. Here are some additional points on the future scope:

- Integration of Artificial Intelligence: With the advent of artificial intelligence, water heating systems can be optimized in real-time, resulting in improved energy efficiency, reduced downtime, and lower operating costs.
- Use of Renewable Energy Sources: Renewable energy sources such as wind and solar power can be harnessed to provide energy for water heating systems. This approach will reduce the reliance on fossil fuels, resulting in lower greenhouse gas emissions and a more sustainable future.
- Internet of Things (IoT) Integration: IoT sensors can be integrated into water heating systems, enabling remote monitoring and control. This feature will facilitate predictive maintenance and prevent equipment failure, thereby reducing repair costs and downtime.
- Heat Recovery: Heat recovery systems can be integrated into water heating systems, allowing the heat generated from the system to be repurposed for other

applications. This approach will reduce energy consumption and lower operating costs.

• Energy Storage: Energy storage systems can be used to store excess energy generated by water heating systems. This approach will ensure a consistent supply of energy and reduce the reliance on the power grid.

In conclusion, the water heating industry is poised for significant transformation in the near future. By leveraging emerging technologies and sustainable practices, we can create more efficient, reliable, and eco-friendly systems that meet the evolving needs of our society.

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#### A Code

Code for thermodynamic solar panel for length of tube tube in solar panel

```
#include<bits/stdc++.h>
using namespace std;
class Node {
public:
    float data;
    Node* next;
};
void Data(Node* head, float T) {
  Node* headref = head;
  int i = 0;
  float A[7];
 A[0] = 560 + 18.2*pow(T,1) + 0.222
*pow(T,2) + 1.09e-03*pow(T,3);//P
  A[1] = 1.40 + (3.975e-3)*pow(T,1) +
(3.14e-5)*pow(T,2) +
(9.14e-7)*pow(T,3);//Cpl
 A[2] = 93.4-0.333*T;//K1
 A[3] = 1233 - 3.81*pow(T,1) -
4.08e-03*pow(T,2) + 1.38e-04*pow(T,3)
+ 5.37e-06*pow(T,4);//rhol
 A[4] = 18.9 + 0.644*pow(T,1) +
8.84e-03*pow(T,2) + 5.96e-05*pow(T,3)
+ 1.11e-07*pow(T,4);//rhov
 A[5] = 218 - 2.83*pow(T,1) + 2.20e-2
*pow(T,2);//mul
 A[6] = 214 - 0.907*pow(T,1) -
8.57e-03*pow(T,2) - 1.38e-04
*pow(T,3);//lambdal
```

Figure 7: Code 1

```
*pow(T,3);//lambdal
  while (1) {
    headref->data = A[i];
    if(i==6) \{break;\}
    headref->next = new Node();
    headref=headref->next;
    i++;
  }
}
float Cpq(float T) {
  float A[3] = \{12.268, 11.701, 4.636\};
  float B[3] = \{-0.0699, 0.0216,
0.0618;
  float C[3] = \{0.000394,
0.0000868, -0.0000309;
  float D[3]=
\{-0.000000837, -0.000000112, 0\};
  float X[3] = \{0.381, 0.179, 0.439\};
  float Sum=0;
  for (int i=0; i<3; i++) {
   float Cp = 4.184
*((A[i]*T)+(B[i]*(pow(T,2)))+(C[i]*(pol))
w(T,3))+(D[i]*(pow(T,4)));
   Sum+=Cp*X[i];
  }
  Sum/=86.2;
  return Sum;
}
```

Figure 8: Code 2

```
return Sum;
}
float wall temp(float Ti, float Ts) {
  float
To, Tn, ri, k, ro, mcg, dmcg, C1, C3, ha, d, hc, P
,siqma;
  ri=1e-2;//m
  ro=1.25e-2;//m
  k=247; //W/m.K
  ha=35; //W/m^2.K
  d=4e-2;//m
  C1=(2*3.142*k)/(ha*d*log(ro/ri)+2*
3.142*k);
  //Let the fractional phase change of
coolant be given by following equation
(function of temperature varying along
length)
  mcq = pow((exp(Ts/Ti+
1)-1)/(\exp(1)-1),4);
  /*The differentiation of mass
changing phase with respect to
temperature is given by following
equation
    (function of temperature varying
along length) */
  dmcq = 4*pow((exp(Ts/Ti+
1)-1),3)*exp(Ts/Ti+
1) / (Ti*pow((exp(1)-1),4));
  //Let the initial guess for wall
```

Figure 9: Code 3

```
1) / (Ti*pow((exp(1)-1), 4));
  //Let the initial guess for wall
temperature To be 0°C
  To=0;
  Node* head = new Node();
  //Import the data of coolant for
temperature Ts
  Data(head, Ts);
  int i=0;
  float A[7];
  while (head!=NULL) {
    Node* temp = head;
    A[i] = head -> data;
    head = head->next;
    delete temp;
    i++;
  }
  sigma=11.8*1e-3;
  C3=0.00122*(pow(A[2]*
1e-3,0.79)*pow(A[1]*
1e3, 0.45) *pow(A[3], 0.49)/(pow(sigma, 0.49))
5)*pow(A[5]*1e-6,0.29)*pow(A[6]*
1e3, 0.24) *pow(A[4], 0.24)));
  while(1){
    P = (560 + 18.2*pow(To,1) + 0.222
*pow(To,2) + 1.09e-03*pow(To,3))*1e3;
    hc = C3*pow(To-Ts, 0.24)*pow(P-
A[0]*1e3, 0.75);
    hc*=0.05;//factor fs of 0.05
    hc+=68599;//hfc'=68599 W/m^2.K
```

Figure 10: Code 4

```
hc+=68599;//hfc'=68599 W/m^2.K
    //We get new wall temperature
using following equation
    Tn =
(ri*log(ro/ri)*(Ts)*hc)/(k*(hc*ri*log(
ro/ri)/k+1-C1);
    if (Tn==0) {break; }
    if((((Tn/To)-1)*
100>-5) && (((Tn/To)-1)*100<5)) {break;}
    To=Tn;
  }
  //Using simpson's rule for 2nd
degree polynomial to solve for length
  //heat absorbed by coolant in liquid
phase (CpL.dT) is given by following
  float sum = (-1)*A[1]*1e3*(36.05/(4*)
90))*(1-mcq)*(hc*ri*log(ro/ri)/k+1-
C1)/((Ts+273)*hc*2*3.142*ri*(C1-1));
  //heat absorbed by coolant in gas
phase (CpG.dT) is given by following
  sum+=(-1)*Cpq(Tn)*1e3*(36.05/(4*)
90)) *mcq* (hc*ri*log(ro/ri)/k+1-
C1)/((Ts+273)*hc*2*3.142*ri*(C1-1));
  //heat absorbed by coolant during
phase transition (lambdaL.(dm/dT)) is
given by following
  sum+=(-1)*A[6]*1e3*(36.05/(4*)
90))*dmcg*(hc*ri*log(ro/ri)/k+1-
C1)/((Ts+273)*hc*2*3.142*ri*(C1-1));
  return sum•
```

Figure 11: Code 5

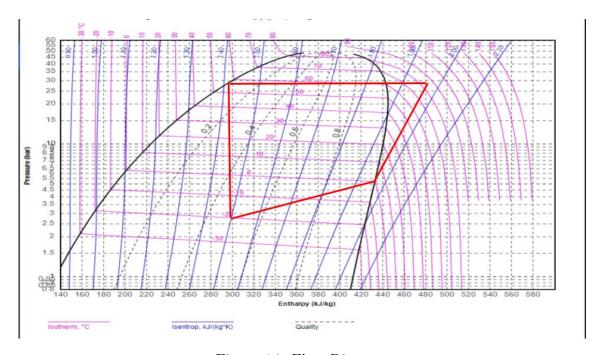
```
return sum;
}
int main(){
  float Ts, Ti;
  cout << "Please enter the coolant
inlet temperature in K"<<endl;
  cin>>Ts:
  Ts = 273;
  Ti = (-1) *Ts;
  //Using simpson's rule to solve with
n=1000
  float p = (-1) *Ts/1000;
  float C0=wall temp(Ti,Ts);
  cout << "Ts (K) " << " | " << "length
(m) "<<endl;
  cout<<Ts+273<<" "<<C0
*p/3<<endl;
  int i=1;
  while (Ts \le (-1) *p)  {
    Ts+=p;
    if(i%2==1){
      C0 += 4*wall temp(Ti,Ts);
      cout<<Ts+273<<" "<<C0
*p/3<<endl;
    }
    else if(i%2 = = 0){
      C0 += 2*wall temp(Ti,Ts);
      cout<<Ts+273<<" "<<C0
*p/3<<endl;
```

Figure 12: Code 6

```
C0 += 4*wall temp(Ti,Ts);
      cout<<Ts+273<<" "<<C0
*p/3<<endl;
    }
    else if(i\%2 = = 0){
      C0 += 2*wall_temp(Ti,Ts);
      cout<<Ts+273<<" "<<C0
*p/3<<endl;
    }
    i++;
  }
  Ts=0;
  C0 += wall temp(Ti,Ts);
  cout << Ts + 273 << " << C0*p/3 << endl;
  C0*=p/3;
  cout<<"length = "<<C0<<" meters";</pre>
  return 0;
}
```

Figure 13: Code 7

# B Reference Graphs



 $\label{eq:figure 14: Flow Diagram} Figure \ 14: \ Flow \ Diagram \\ https://www.flycarpet.net/en/phonline$ 

### C Reference Tables

Typical equipment capacity delivered capital cost correlations.

| Equipment   | Material of construction | Capacity<br>measure  | Base<br>size Q <sub>B</sub> | Base cost<br>C <sub>B</sub> (\$) | Size range     | Cost<br>exponent M |
|---|--------------------------|--|-----------------------------|----------------------------------|----------------|--------------------|
| Agitated reactor                                  | CS                       | Volume (m³)  | 1                           | 1.15×10 <sup>4</sup>             | 1-50           | 0.45               |
| Pressure vessel                                   | SS                       | Mass (t)   | 6                           | 9.84×10 <sup>4</sup>             | 6–100          | 0.82               |
| Distillation column (empty shell)                 | CS                       | Mass (t)   | 8                           | 6.56×10 <sup>4</sup>             | 8-300          | 0.89               |
| Sieve trays (10 trays)                            | CS                       | Column diameter (m)  | 0.5                         | 6.56×10 <sup>3</sup>             | 0.5-4.0        | 0.91               |
| Valve trays (10 trays)                            | CS                       | Column diameter (m)  | 0.5                         | 1.80×10 <sup>4</sup>             | 0.5-4.0        | 0.97               |
| Structured packing (5 m height)                   | SS (low grade)           | Column diameter (m)  | 0.5                         | 1.80×10 <sup>4</sup>             | 0.5-4.0        | 1.70               |
| Scrubber (including random packing)               | SS (low grade)           | Volume (m <sup>3</sup> )                                   | 0.1                         | $4.92 \times 10^{3}$             | 0.1-20         | 0.53               |
| Cyclone   | CS                       | Diameter (m)   | 0.4                         | $1.64 \times 10^{3}$             | 0.4-3.0        | 1.20               |
| Vacuum filter                                     | CS                       | Filter area (m <sup>2</sup> )                              | 10                          | $8.36 \times 10^4$               | 10-25          | 0.49               |
| Dryer   | SS (low grade)           | Evaporation rate<br>(kg H <sub>2</sub> O·h <sup>-1</sup> ) | 700                         | 2.30×10 <sup>5</sup>             | 700–3000       | 0.65               |
| Shell-and-tube heat exchanger                     | CS                       | Heat transfer<br>area (m <sup>2</sup> )                    | 80                          | 3.28×10 <sup>4</sup>             | 80-4000        | 0.68               |
| Air-cooled heat exchanger                         | CS                       | Plain tube heat<br>transfer area (m <sup>2</sup> )         | 200                         | 1.56×10 <sup>5</sup>             | 200–2000       | 0.89               |
| Centrifugal pump (small, including motor)         | SS (high grade)          | Power (kW)   | 1                           | 1.97×10 <sup>3</sup>             | 1–10           | 0.35               |
| Centrifugal pump (large, including motor)         | CS                       | Power (kW)   | 4                           | 9.84×10 <sup>3</sup>             | 4–700          | 0.55               |
| Compressor (including motor)                      |                          | Power (kW)   | 250                         | 9.84×10 <sup>4</sup>             | 250-10,000     | 0.46               |
| Fan (including motor)                             | CS                       | Power (kW)   | 50                          | 1.23×10 <sup>4</sup>             | 50-200         | 0.76               |
| Vacuum pump (including motor)                     | CS                       | Power (kW)   | 10                          | 1.10×10 <sup>4</sup>             | 10-45          | 0.44               |
| Electric motor                                    |                          | Power (kW)   | 10                          | $1.48 \times 10^{3}$             | 10-150         | 0.85               |
| Storage tank (small atmospheric)                  | SS (low grade)           | Volume (m <sup>3</sup> )                                   | 0.1                         | $3.28 \times 10^{3}$             | 0.1-20         | 0.57               |
| Storage tank (large atmospheric)                  | CS                       | Volume (m <sup>3</sup> )                                   | 5                           | 1.15×10 <sup>4</sup>             | 5-200          | 0.53               |
| Silo  | CS                       | Volume (m <sup>3</sup> )                                   | 60                          | 1.72×10 <sup>4</sup>             | 60-150         | 0.70               |
| Package steam boiler (fire-tube boiler)           | CS                       | Steam generation (kg·h <sup>-1</sup> )                     | 50,000                      | 4.64×10 <sup>5</sup>             | 50,000-350,000 | 0.96               |
| Field erected steam boiler<br>(water-tube boiler) | CS                       | Steam generation (kg·h <sup>-1</sup> )                     | 20,000                      | 3.28×10 <sup>5</sup>             | 10,000-800,000 | 0.81               |
| Cooling tower (forced draft)                      |                          | Water flowrate<br>(m <sup>3</sup> ·h <sup>-1</sup> )       | 10                          | $4.43 \times 10^3$               | 10-40          | 0.63               |

CS = carbon steel; SS (low grade) = low-grade stainless steel, for example, type 304; SS (high grade) = high-grade stainless steel, for example, type 316.

Figure 15: Equipment Capacity Delivered Capital Cost Correlation Chemical Process Design and Integration, 2nd Edition by Robin and Smith

| Year              | Electric | Electric Immersion | Heating | Bottled | LPG Gas | Mains Gas |  |  |  |
|-------------------|----------|--------------------|---------|---------|---------|-----------|--|--|--|
|                   | Boiler   | Heater             | Oil     | Gas     |         |           |  |  |  |
| 1 year            | -2,993   | -3,644             | -1,889  | -1,815  | -2,888  | -3,019    |  |  |  |
| 2 years           | -2,576   | -2,439             | -1,734  | -522    | -2,668  | -2,931    |  |  |  |
| 3 years           | -2,158   | -1,233             | -1,580  | 772     | -2,448  | -2,842    |  |  |  |
| 4 years           | -1,741   | -28                | -1,425  | 2,065   | -2,228  | -2,753    |  |  |  |
| 5 years           | -1,324   | 1,178              | -1,271  | 3,358   | -2,008  | -2,665    |  |  |  |
| 6 years           | -907     | 2,384              | -1,117  | 4,651   | -1,787  | -2,576    |  |  |  |
| 7 years           | -490     | 3,589              | -962    | 5,944   | -1,567  | -2,487    |  |  |  |
| 8 years           | -72      | 4,795              | -808    | 7,238   | -1,347  | -2,398    |  |  |  |
| 9 years           | 345      | 6,000              | -653    | 8,531   | -1,127  | -2,310    |  |  |  |
| 10 years          | 762      | 7,206              | -499    | 9,824   | -907    | -2,221    |  |  |  |
| Needs replacement |          |                    |         |         |         |           |  |  |  |
| 11 years          | 2,769    | 8,562              | -345    | 11,117  | -687    | -2,132    |  |  |  |
| 12 years          | 3,186    | 9,767              | -190    | 12,410  | -467    | -2,044    |  |  |  |
| 13 years          | 3,604    | 10,973             | -36     | 13,704  | -247    | -1,955    |  |  |  |
| 14 years          | 4,021    | 12,178             | 119     | 14,997  | -27     | -1,866    |  |  |  |
| 15 years          | 4,438    | 13,384             | 273     | 16,290  | 193     | -1,778    |  |  |  |
| Needs replacement |          |                    |         |         |         |           |  |  |  |
| 16 years          | 4,855    | 14,590             | 3,384   | 19,475  | 2,306   | 203       |  |  |  |
| 17 years          | 5,272    | 15,795             | 3,539   | 20,768  | 2,526   | 292       |  |  |  |
| 18 years          | 5,690    | 17,001             | 3,693   | 22,062  | 2,746   | 381       |  |  |  |
| 19 years          | 6,107    | 18,206             | 3,848   | 23,355  | 2,966   | 469       |  |  |  |
| 20 years          | 6,524    | 19,412             | 4,002   | 24,648  | 3,186   | 558       |  |  |  |

Table 2: Cost Calculation Table