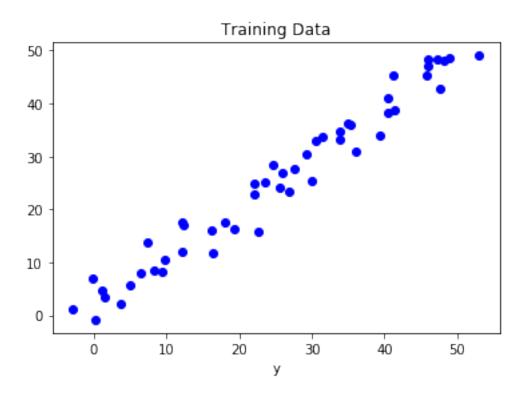
## LAB5

### August 25, 2019

```
[0]: import numpy as np
     import tensorflow as tf
     import matplotlib.pyplot as plt
     from sklearn.datasets import load_boston
     import pandas as pd
     import seaborn as sns
 [0]: x = np.linspace(0,50,50)
     y = np.linspace(0,50,50)
 [0]: x += np.random.uniform(-4, 4, 50)
     y += np.random.uniform(-4, 4, 50)
     n = len(x)
[11]: plt.scatter(x, y, color='blue')
     plt.xlabel('x')
     plt.xlabel('y')
     plt.title("Training Data")
     plt.show()
```



```
[0]: X = tf.placeholder(tf.float32)
Y = tf.placeholder(tf.float32)

[0]: W = tf.Variable(np.random.randn(), name = "W")
b = tf.Variable(np.random.randn(), name = "b")

[0]: learning_rate = 0.01
training_epochs = 1500

[15]: y_pred = tf.add(tf.multiply(X, W), b)
cost = tf.div(tf.reduce_sum(tf.square(y_pred-Y)),(2 * n))
optimizer = tf.train.GradientDescentOptimizer(learning_rate).minimize(cost)
init = tf.global_variables_initializer()
```

WARNING: Logging before flag parsing goes to stderr.
W0825 10:37:18.480022 139839722747776 deprecation.py:323] From <ipython-input-15-0315d83416be>:2: div (from tensorflow.python.ops.math\_ops) is deprecated and will be removed in a future version.
Instructions for updating:
Deprecated in favor of operator or tf.math.divide.

```
[16]: with tf.Session() as sess:
    merged = tf.summary.merge_all()
    writer = tf.summary.FileWriter("logs", sess.graph)
    sess.run(init)
```

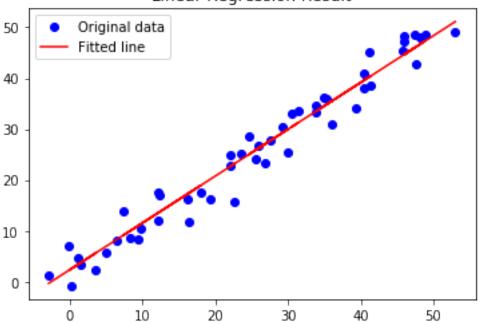
```
for epoch in range(training_epochs):
         for (_x, _y) in zip(x, y):
           sess.run(optimizer, feed_dict = {X : _x, Y : _y})
         if (epoch+1) \% 50 == 0:
           c = sess.run(cost, feed_dict = {X : x, Y : y})
           print("Epoch", (epoch+1), ": cost =", c, "W =", sess.run(W), "b =", sess.
      \rightarrowrun(b))
      training_cost = sess.run(cost, feed_dict ={X: x, Y: y})
       weight = sess.run(W)
       bias = sess.run(b)
    Epoch 50 : cost = 6.781017 W = 1.0048156 b = -1.9276061
    Epoch 100 : cost = 6.135523 W = 0.9947624 b = -1.4226213
    Epoch 150 : cost = 5.637338 W = 0.98585576 b = -0.97522396
    Epoch 200 : cost = 5.25382 W = 0.97796464 b = -0.5788447
    Epoch 250 : cost = 4.959443 W = 0.9709735 b = -0.22766782
    Epoch 300 : cost = 4.73428 \text{ W} = 0.9647795 \text{ b} = 0.0834629
    Epoch 350 : cost = 4.562768 W = 0.95929193 b = 0.3591139
    Epoch 400: cost = 4.432778 W = 0.9544301 b = 0.6033299
    Epoch 450: cost = 4.3348465 W = 0.9501227 b = 0.8196979
    Epoch 500 : cost = 4.261615 W = 0.9463064 b = 1.0113928
    Epoch 550 : cost = 4.2073536 W = 0.94292545 b = 1.1812264
    Epoch 600 : cost = 4.1676173 W = 0.93992996 b = 1.3316915
    Epoch 650 : cost = 4.1389556 W = 0.93727607 b = 1.4649987
    Epoch 700 : cost = 4.1186976 W = 0.9349249 b = 1.5831044
    Epoch 750 : cost = 4.104782 W = 0.9328418 b = 1.6877413
    Epoch 800 : cost = 4.0956173 W = 0.93099624 b = 1.7804458
    Epoch 850 : cost = 4.0899816 W = 0.92936116 b = 1.862578
    Epoch 900 : cost = 4.0869384 W = 0.92791253 b = 1.9353461
    Epoch 950 : cost = 4.085772 W = 0.92662907 b = 1.9998158
    Epoch 1000 : cost = 4.08594 W = 0.9254919 b = 2.056933
    Epoch 1050 : cost = 4.0870333 W = 0.9244846 b = 2.1075342
    Epoch 1100 : cost = 4.0887394 W = 0.92359203 b = 2.1523685
    Epoch 1150 : cost = 4.0908327 W = 0.9228014 b = 2.1920836
    Epoch 1200 : cost = 4.0931444 W = 0.9221007 b = 2.227279
    Epoch 1250 : cost = 4.09555 W = 0.9214801 b = 2.2584536
    Epoch 1300 : cost = 4.097961 W = 0.92093027 b = 2.286073
    Epoch 1350 : cost = 4.10032 W = 0.92044294 b = 2.3105524
    Epoch 1400 : cost = 4.1025815 W = 0.9200113 b = 2.3322346
    Epoch 1450: cost = 4.1047196 W = 0.919629 b = 2.3514392
    Epoch 1500: cost = 4.106723 W = 0.9192901 b = 2.3684573
[17]: predictions = weight * x + bias
     print("Training cost =", training_cost, "Weight =", weight, "bias =", bias, ⊔
```

Training cost = 4.106723 Weight = 0.9192901 bias = 2.3684573

 $\leftrightarrow$  '\n')

```
[18]: plt.plot(x, y, 'ro', color = 'blue', label = 'Original data')
     plt.plot(x, predictions, color = 'red', label ='Fitted line')
     plt.title('Linear Regression Result')
     plt.legend()
     plt.show()
```

# Linear Regression Result



```
[19]: from sklearn.metrics import r2_score
     R2 = r2_score(y, predictions, multioutput='variance_weighted')
     print("R2 value:",R2)
```

R2 value: 0.9626758714904278

```
[20]: '''
     Exercise 1:
     Predict Y values for given X values.
     predictions1 = weight * np.array([3.987, 19.235, 23.098, 36.5, 22.765]) + bias
     predictions1
```

[20]: array([ 6.03366705, 20.05100288, 23.60222063, 35.92254689, 23.29609702])

```
[21]:
     Exercise 2:
     Change Stopping criterion to delta(J) <= 0.000001
```

```
with tf.Session() as sess:
       merged = tf.summary.merge_all()
       writer = tf.summary.FileWriter("logs", sess.graph)
       sess.run(init)
      prev = 0.0
       iters = 1
       while(iters):
         for (x, y) in zip(x, y):
           sess.run(optimizer, feed_dict = {X : _x, Y : _y})
         c = sess.run(cost, feed_dict = {X : x, Y : y})
         if iters % 50 == 0:
           print("Epoch", (iters), ": cost =", c, "W =", sess.run(W), "b =", sess.
      \rightarrowrun(b))
         if(abs(c-prev)<0.000001):
           break
         prev = c
         iters+=1
       training_cost = sess.run(cost, feed_dict ={X: x, Y: y})
       weight = sess.run(W)
       bias = sess.run(b)
    Epoch 50 : cost = 6.781017 W = 1.0048156 b = -1.9276061
    Epoch 100 : cost = 6.135523 W = 0.9947624 b = -1.4226213
    Epoch 150 : cost = 5.637338 W = 0.98585576 b = -0.97522396
    Epoch 200 : cost = 5.25382 W = 0.97796464 b = -0.5788447
    Epoch 250 : cost = 4.959443 W = 0.9709735 b = -0.22766782
    Epoch 300 : cost = 4.73428 W = 0.9647795 b = 0.0834629
    Epoch 350 : cost = 4.562768 W = 0.95929193 b = 0.3591139
    Epoch 400: cost = 4.432778 W = 0.9544301 b = 0.6033299
    Epoch 450: cost = 4.3348465 W = 0.9501227 b = 0.8196979
    Epoch 500 : cost = 4.261615 W = 0.9463064 b = 1.0113928
    Epoch 550: cost = 4.2073536 W = 0.94292545 b = 1.1812264
    Epoch 600 : cost = 4.1676173 W = 0.93992996 b = 1.3316915
    Epoch 650 : cost = 4.1389556 W = 0.93727607 b = 1.4649987
    Epoch 700 : cost = 4.1186976 W = 0.9349249 b = 1.5831044
    Epoch 750 : cost = 4.104782 \text{ W} = 0.9328418 \text{ b} = 1.6877413
    Epoch 800 : cost = 4.0956173 W = 0.93099624 b = 1.7804458
    Epoch 850 : cost = 4.0899816 W = 0.92936116 b = 1.862578
    Epoch 900 : cost = 4.0869384 W = 0.92791253 b = 1.9353461
    Epoch 950 : cost = 4.085772 W = 0.92662907 b = 1.9998158
[22]: '''
     Exercise 3
     Diffrent alpha values for 1500 epoches:
     learning rate: 0.01 --> R2 value: 0.9618197718107743
     learning rate: 0.05 --> R2 value: -0.9297278609667908
```

learning rate: 0.2 --> All values are Nan

```
learning rate: 0.5 --> All values are Nan
     111
[22]: '\nExercise 3\nDiffrent alpha values for 1500 epoches:\nlearning rate: 0.01 -->
     R2 value: 0.9618197718107743\nlearning rate: 0.05 --> R2 value:
     -0.9297278609667908\nlearning rate: 0.2 --> All values are Nan\nlearning rate:
     0.5 --> All values are Nan\n'
[23]: boston = load_boston()
     df = pd.DataFrame(
         data= np.c_[boston['data']],
         columns= boston['feature names'])
     df.insert(13, 'target', boston['target'], True)
     print(boston['DESCR'])
     df.head()
    .. _boston_dataset:
    Boston house prices dataset
    **Data Set Characteristics:**
        :Number of Instances: 506
        :Number of Attributes: 13 numeric/categorical predictive. Median Value
    (attribute 14) is usually the target.
        :Attribute Information (in order):
            - CRIM
                       per capita crime rate by town
            - ZN
                       proportion of residential land zoned for lots over 25,000
    sq.ft.
                       proportion of non-retail business acres per town
            - INDUS
            - CHAS
                       Charles River dummy variable (= 1 if tract bounds river; 0
    otherwise)
            - NOX
                       nitric oxides concentration (parts per 10 million)
                       average number of rooms per dwelling
            - RM
                       proportion of owner-occupied units built prior to 1940
            - AGE
            - DIS
                       weighted distances to five Boston employment centres
            - RAD
                       index of accessibility to radial highways
                       full-value property-tax rate per $10,000
            - TAX
            - PTRATIO
                       pupil-teacher ratio by town
            - B
                       1000(Bk - 0.63)^2 where Bk is the proportion of blacks by
    town
            - LSTAT
                       % lower status of the population
            - MEDV
                       Median value of owner-occupied homes in $1000's
```

:Missing Attribute Values: None

:Creator: Harrison, D. and Rubinfeld, D.L.

This is a copy of UCI ML housing dataset.

https://archive.ics.uci.edu/ml/machine-learning-databases/housing/

This dataset was taken from the StatLib library which is maintained at Carnegie Mellon University.

The Boston house-price data of Harrison, D. and Rubinfeld, D.L. 'Hedonic prices and the demand for clean air', J. Environ. Economics & Management, vol.5, 81-102, 1978. Used in Belsley, Kuh & Welsch, 'Regression diagnostics ...', Wiley, 1980. N.B. Various transformations are used in the table on pages 244-261 of the latter.

The Boston house-price data has been used in many machine learning papers that address regression problems.

#### .. topic:: References

- Belsley, Kuh & Welsch, 'Regression diagnostics: Identifying Influential Data and Sources of Collinearity', Wiley, 1980. 244-261.
- Quinlan, R. (1993). Combining Instance-Based and Model-Based Learning. In Proceedings on the Tenth International Conference of Machine Learning, 236-243, University of Massachusetts, Amherst. Morgan Kaufmann.

```
[23]:
          CRIM
                       INDUS CHAS
                                      NOX
                   ZN
                                                  TAX PTRATIO
                                                                     В
                                                                        LSTAT
                                                                               target
                                           . . .
     0 0.00632 18.0
                        2.31
                               0.0 0.538
                                                296.0
                                                          15.3 396.90
                                                                         4.98
                                                                                 24.0
                                           . . .
     1 0.02731
                  0.0
                        7.07
                                                242.0
                                                                         9.14
                                                                                 21.6
                               0.0 0.469
                                                          17.8 396.90
                               0.0 0.469
     2 0.02729
                  0.0
                       7.07
                                                                         4.03
                                                                                 34.7
                                           ... 242.0
                                                          17.8 392.83
     3 0.03237
                  0.0
                        2.18
                               0.0 0.458
                                           . . .
                                                222.0
                                                          18.7
                                                                394.63
                                                                         2.94
                                                                                 33.4
     4 0.06905
                  0.0
                        2.18
                               0.0 0.458
                                                222.0
                                                          18.7 396.90
                                                                         5.33
                                                                                 36.2
                                           . . .
```

[5 rows x 14 columns]

```
[24]: corr = df.corr() corr
```

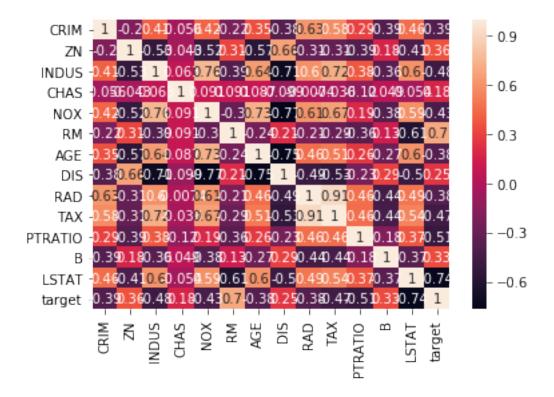
```
[24]:
                  CRIM
                                     INDUS ...
                              ZN
                                                        В
                                                              LSTAT
                                                                       target
     CRIM
              1.000000 -0.200469
                                 0.406583 ... -0.385064 0.455621 -0.388305
     ZN
             -0.200469 1.000000 -0.533828
                                           ... 0.175520 -0.412995
                                                                    0.360445
     INDUS
              0.406583 - 0.533828 \ 1.000000 \ \dots - 0.356977 \ 0.603800 - 0.483725
     CHAS
            -0.055892 -0.042697 0.062938 \dots 0.048788 -0.053929
                                                                     0.175260
    NOX
                                           ... -0.380051 0.590879 -0.427321
              0.420972 -0.516604 0.763651
    RM
            -0.219247 0.311991 -0.391676
                                           ... 0.128069 -0.613808 0.695360
```

```
AGE
          0.352734 - 0.569537 \quad 0.644779 \quad \dots \quad -0.273534 \quad 0.602339 \quad -0.376955
DIS
        -0.379670 0.664408 -0.708027
                                          ... 0.291512 -0.496996 0.249929
RAD
          0.625505 -0.311948 0.595129 ... -0.444413 0.488676 -0.381626
          0.582764 - 0.314563 \ 0.720760 \ \dots - 0.441808 \ 0.543993 - 0.468536
TAX
PTRATIO 0.289946 -0.391679 0.383248 ... -0.177383 0.374044 -0.507787
         -0.385064 0.175520 -0.356977
                                                1.000000 -0.366087 0.333461
LSTAT
          0.455621 - 0.412995 \quad 0.603800 \quad \dots \quad -0.366087 \quad 1.000000 \quad -0.737663
target -0.388305 0.360445 -0.483725
                                          ... 0.333461 -0.737663 1.000000
```

[14 rows x 14 columns]

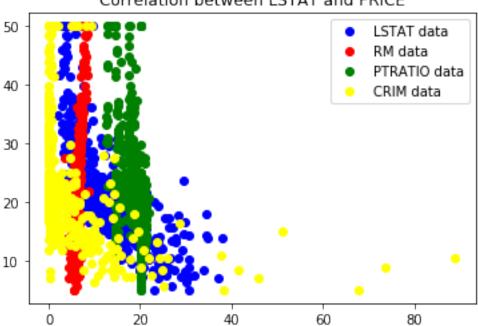
[25]: sns.heatmap(corr,annot=True)

[25]: <matplotlib.axes.\_subplots.AxesSubplot at 0x7f2ead68b0b8>



```
plt.legend()
plt.show()
```

### Correlation between LSTAT and PRICE



90 22.6 373 13.8 273 35.2