

Date:- 9th October, 2022

(14)

MACHINE LEARNING (Day-2)

Agenda :-

- 1) Revision of Day-1
- 2) Cost Function
- 3) Loss Function
- 4) Performance Metrics
- 5) Overfitting and Underfitting

1) Revision of Day-1 :-

* Linear Regression Algorithm :-

a) Simple Regression

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

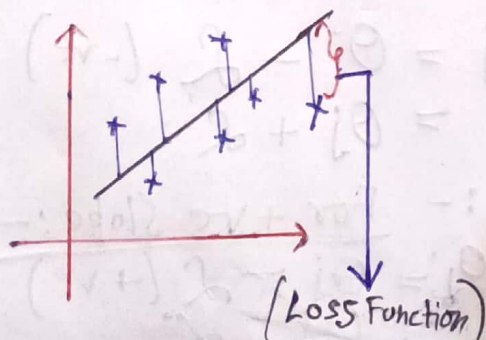
b) Multiple Regression

$$h_{\theta}(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_n x_n$$

* Convergence Algorithm :-

• Cost Function (MSE) \Rightarrow

$$J(\theta_0, \theta_1) = \frac{1}{m} \sum_{i=1}^m \left(\underbrace{h_{\theta}(x)^i}_{\text{Predicted Value}} - \underbrace{y^{(i)}}_{\text{Actual Value}} \right)^2$$



• Loss Function = $(h_{\theta}(x)^i - y^{(i)})^2$

$$= (\hat{y}_i - y_i)^2$$

Predicted value

Actual Value

★ > For Convergence Algorithm :-

Repeat Until Convergence

$$\left\{ \begin{array}{l} \theta_j = \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_j) \\ \end{array} \right.$$

$$\frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1) = \frac{\partial}{\partial \theta_0} \left[\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x)^{(i)} - y^{(i)})^2 \right]$$

$$h_{\theta}(x) = \theta_0 + \theta_1 x \quad \text{--- Eqn-10 (1)}$$

$$\text{Let, } \underline{J=0}; \quad = \frac{\partial}{\partial \theta_0} \left[\frac{1}{m} \sum_{i=1}^m ((\theta_0 + \theta_1 x)^{(i)} - y^{(i)})^2 \right] \rightarrow \text{Using Eqn-10 (1)}$$

$$= \frac{2}{m} \sum_{i=1}^m [(\theta_0 + \theta_1 x)^i - y^{(i)}] \times 1$$

$$\text{Let, } \underline{J=1}; \quad = \frac{\partial}{\partial \theta_1} \left[\frac{1}{m} \sum_{i=1}^m ((\theta_0 + \theta_1 x)^i - y^{(i)})^2 \right]$$

$$\Rightarrow \frac{2}{m} \sum_{i=1}^m [(\theta_0 + \theta_1 x)^i - y^i] x$$

Repeat Until Convergence

{

$$\theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x)^{(i)} - y^{(i)})$$

$$\theta_1 := \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x)^{(i)} - y^{(i)}) x$$

}

2) Cost Function :-

⇒ A Cost Function is an Important Parameter that Determines how well a ML Model performs for a given Dataset.

It's ~~calculated~~ ^{the} measures ~~the~~ Error between Predicted and their Actual Values Across the Whole Dataset.

★) Different Types of Cost Function are :-

1) MSE

2) MAE

3) RMSE

1A) MSE (Mean Squared Error) :-

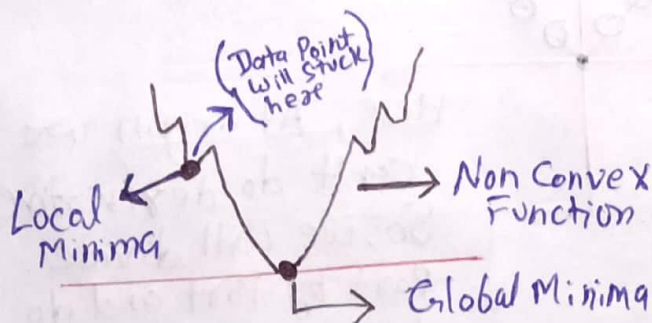
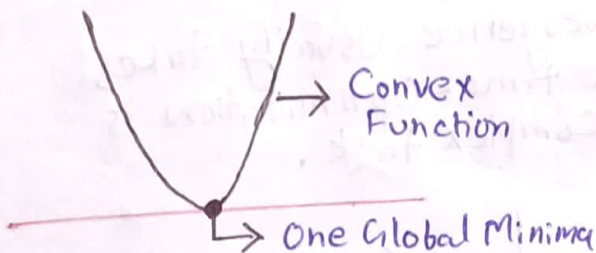
⇒ MSE (Mean Squared Error) represents the Average of the Squared Difference between the Original and Predicted Values in the dataset. It measures the Variance of the residuals.

$$\underline{\text{MSE}} = \sum_{i=1}^n \frac{(y - \hat{y})^2}{n}, \quad \text{Here, } \hat{y} = \theta_0 + \theta_1 x$$

(Quadratic Equation) (Predicted Value)

Advantages :-

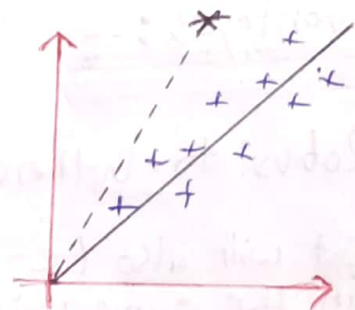
- i) This Equation is differentiable.
- ii) This Equation also has only one - Global Minima.



Note :- Our work is to work with Convex-function because there is not any local minima present.

Disadvantages :-

- ① This Equation is not robust to outliers.



Here,

Because of outlier the line will switch more towards outliers.

So, we can Remove Outliers.

- ② Penalizing the error or Changing the Unit.

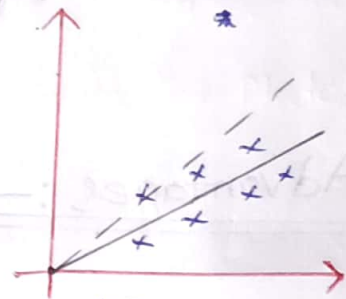
2) MAE (Mean Absolute Error) :-

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⇒ MAE (Mean Absolute Error) represents the Average of the absolute different between the Actual and Predicted Values in the dataset.

It measures the Average of the residuals in the Dataset.

$$\underline{\underline{MAE}} = \frac{1}{n} \sum_{i=1}^n |y - \hat{y}|$$



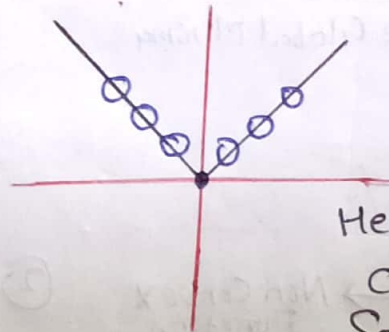
It will not more attracted to outlier because here $(y - \hat{y})$ is not Squaring.

Advantages :-

- ① Robust to Outliers.
- ② It will also be in the same unit.

DisAdvantages :-

- ① Convergence Usually takes more time - Optimization is a complex task.



Here, At origin we can't do derivative So, we will divide Part by Part and do derivative, this is called Subgradient Concept.

- ② Time Consuming.

3) RMSE (Root Mean Squared Error) :-

⇒ RMSE (Root Mean Squared Error) is the Square Root of Mean Squared Error. It measures the Standard-Deviation of residuals.

$$\underline{\underline{RMSE = \sqrt{MSE}}}$$

Advantages:-

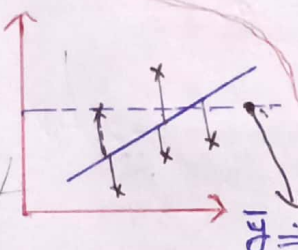
- i) It is not Robust to Outliers.
- ii) It is differentiable.

⊛ Loss Function :- MAE, MSE, RMSE, Huber Loss.

⊛ R-Squared [Performance Matrix] :-

⇒ R-Squared (or The Coefficient of determination) Represents the proportion of the variance in the dependent Variable which is explained by the Linear Regression Model. It is a Scale-Free Score i.e irrespective of the values being small or large, the value of R-Square will be less than one.

$$\underline{\underline{R-Squared = 1 - \frac{SS_{Res}}{SS_{Total}}}}, \text{ where}$$



$$= 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2}$$

SS_{Res} = Sum of Square residual
 SS_{Total} = Sum of Square Average

★ If the model is fitted, then $= 1 - \frac{\text{Small Number}}{\text{Bigger Number}}$
 ↓ outcome

If, $R^2 = 0.85$ mean 85% ^{accurate} n

If, $R^2 = 0.75$ mean model is 75% accurate.

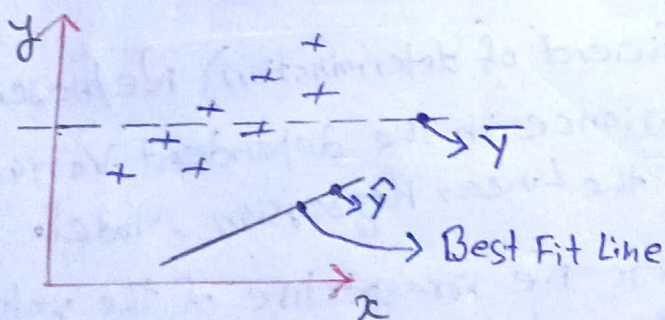
∴ R^2 measures the Performance of the Model.

Q) Can R^2 value -ve?

⇒ If it is happening then the model is very bad.

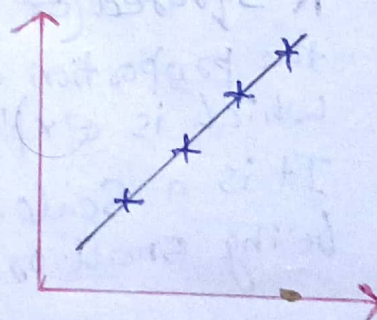
Scenario - 1 :-

If, $R^2 = -ve$



Scenario - 2 :-

If, $R^2 = 1$



In this case $R^2 = -ve$

Worth Model

here, \bar{y} is better than Best Fit Line.

2) Adjusted R-Squared :-

⇒ Adjusted R-Squared is a modified Version of R-Square, and it is adjusted for the number of Independent Variables in the model, and it will always be less than or Equal to R^2 .

Dataset :-

Size of House	City Location	No. of Bedrooms	Gender	Price
—	—	—	—	—
—	—	—	—	—
—	—	—	—	—
—	—	—	—	—

65%
75%
85%

By Including Features Accuracy is jumping, But Gender Feature is not correlating to Price Prediction.

↓ So, here we have to handle with these - accuracy.

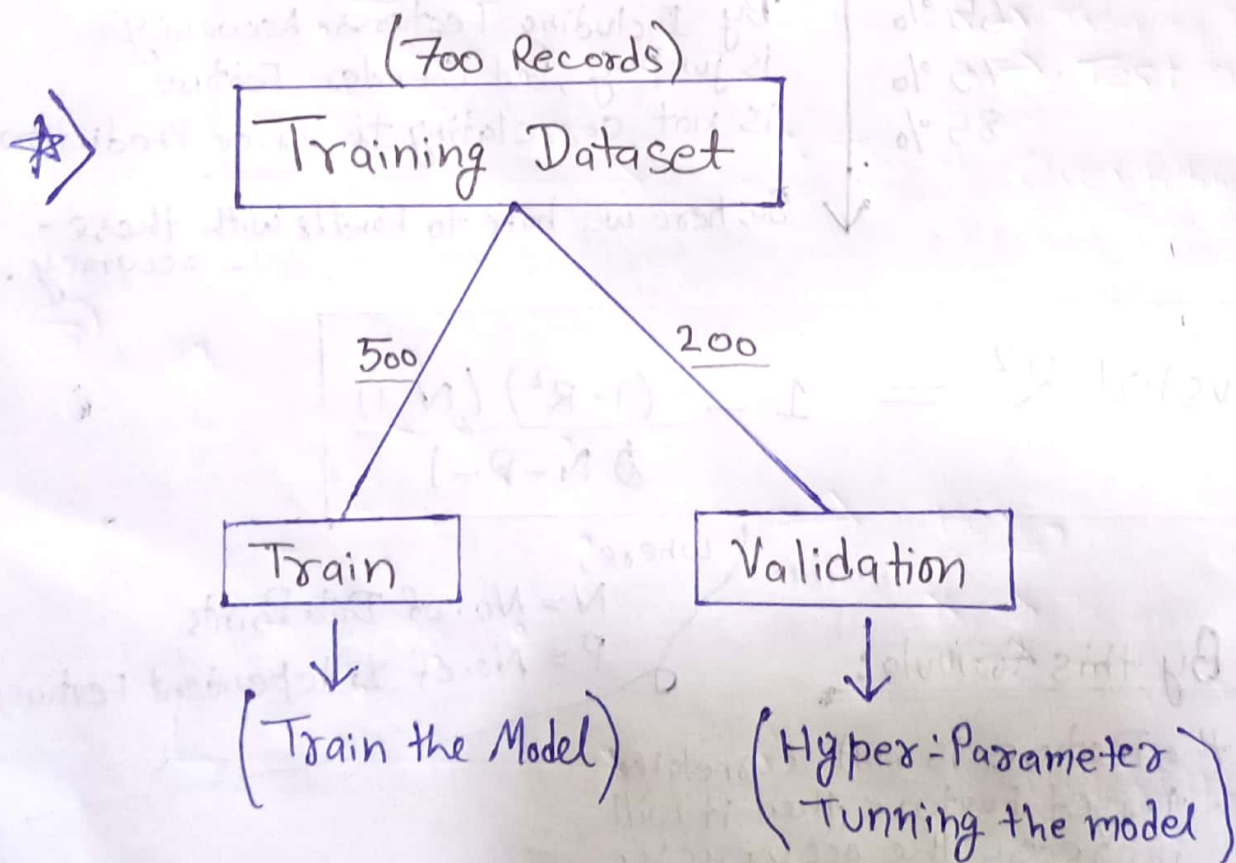
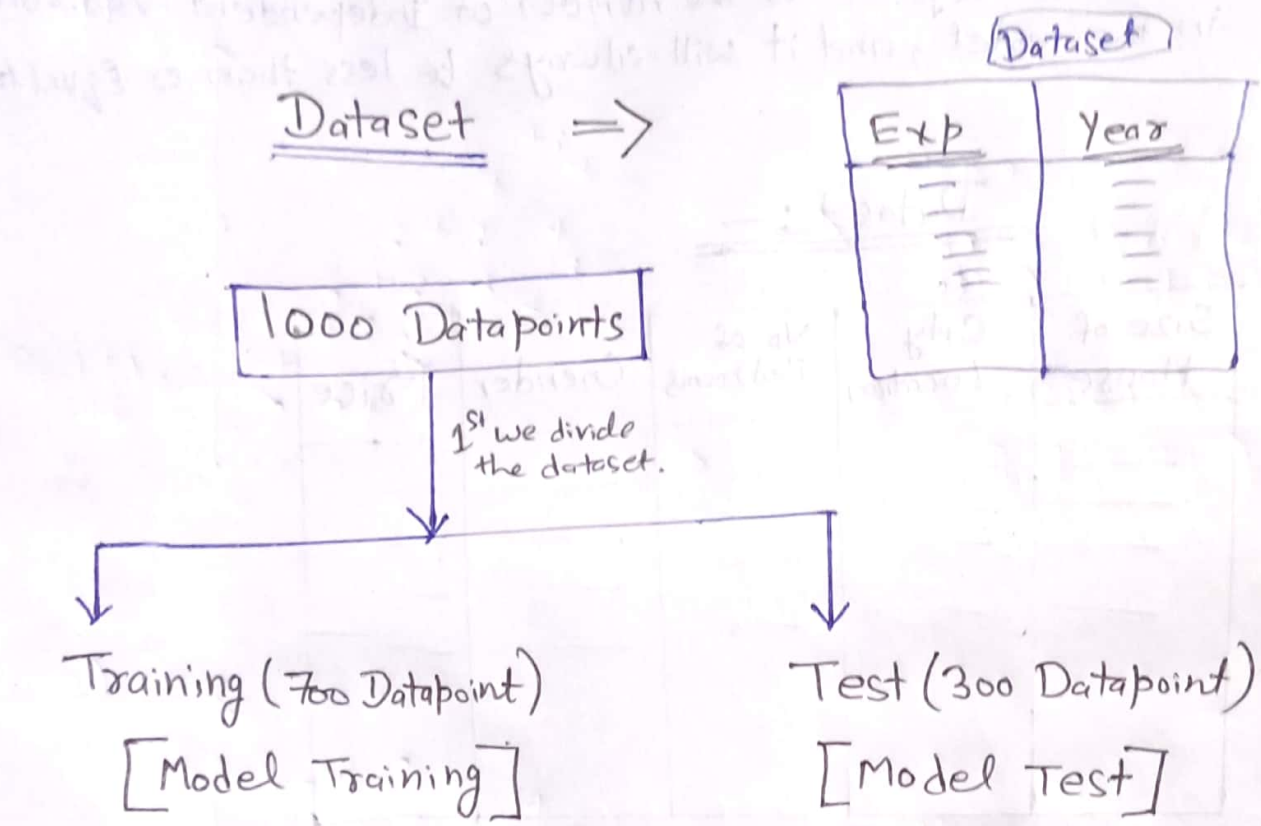
$$\text{Adjusted } R^2 = 1 - \frac{(1 - R^2)(N - 1)}{N - P - 1}$$

where,
N = No. of Data Points
P = No. of Independent Features.

Here By this formula:

, if the Feature is not correlated with target Feature then it will not increase the accuracy, and we will able to adjust the Value.

5) Overfitting And Underfitting [Bias and Variance]:



Model :-

Train Data	Very Good Accuracy (90%)	→ [Low Bias]
Test Data	Very Good Accuracy (85%)	→ [Low Variance]

∴ This kind of accuracy creates Generalized Model.

Scenario - 1 :-

a) For Training Data :- We have Very Good Accuracy (90%).

⇒ In this case, it will come Low Bias.

b) For Test Data :- We have Bad Accuracy (50%).

⇒ In this case, it will come High Variance.

Hence, For Such Type of Model where Training Data is very Good and has Bad Test Data then, this Condition is called Overfitting.

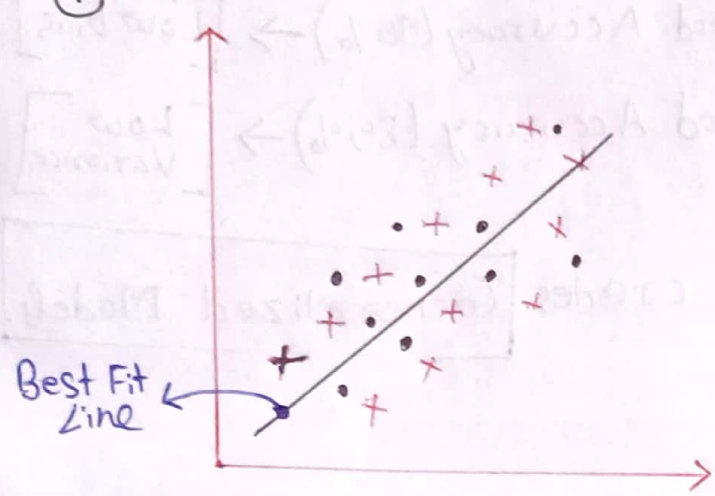
Scenario - 2 :-

Train Data	Model Accuracy is Low	→ [High Bias]
Test Data	Model Accuracy is Low/High	→ [Low or High Variance]

∴ This Type of Accuracy Model is Underfitting.

★ Graphical Representation of Model :-

①

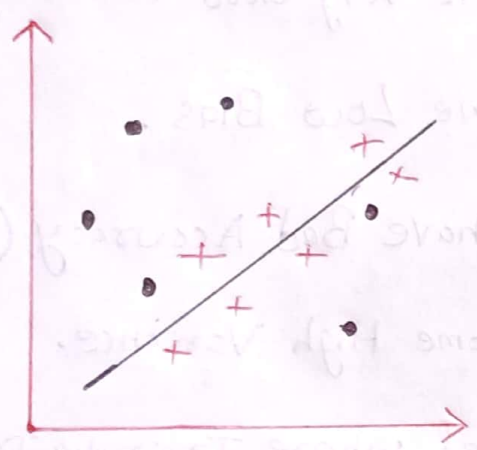


Here,

⇒
+ → Training Data
• → Test Data

This is Generalized Model
(Best Fitting)

②

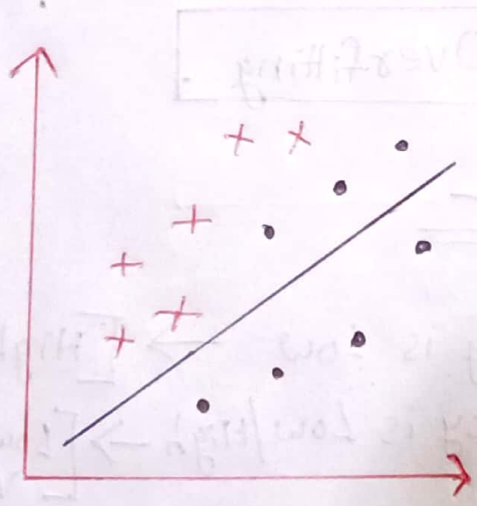


Here,

⇒
+ → Training Data
• → Test Data

∴ This is Overfitting Model.

③



Here,

⇒
+ → Training Data
• → Test Data

∴ This is Underfitting Model.