

* Time Complexity -

```

Count = 0
① for (i=0; i < N; i++)
{
    for (j=i+1; j < N; j++)
        {
            {
                Count++;
            }
        }
    Print (Count)
}

```

The deepest statement, How many times it is running.

$$\begin{aligned}
&= (N-1) + (N-2) + (N-3) + (N-4) \\
&\quad + (N-5) \\
&= 4 + 3 + 2 + 1 + 0
\end{aligned}$$

{ Sum of first $(N-1)$ Natural Numbers }

Formula for sum of N Natural Nos. = $\frac{N(N+1)}{2}$

$$= \frac{(N-1)(N-1+1)}{2}$$

$$= \frac{N(N-1)}{2}$$

$$= \frac{1}{2}N^2 - \frac{N}{2}$$

$$= O(N^2)$$

{: Ignore Non-dominating term & constants
↑(floor value)

② $\text{for}(i=n; i>0; i=\lfloor i/2 \rfloor)$,

{

$\text{for}(j=0; j<i; j++)$

 { $\text{Print}(x)$ }

}

let $n=128$

Floor Values $\rightarrow 128 - 64 - 32 - 16 - 8 - 4 - 2 - 1 - 0$

Let $n=343$

Floor Value $\rightarrow 343 - 171 - 85 - 42 - 21 - 10 - 5 - 2 - 1 - 0$

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$$i = N$$

$$j = \lfloor N/2 \rfloor$$

$$i = \lfloor N/4 \rfloor$$

↓

↓

$$j = 1$$

Inner loop running till

$$\lfloor N/2 \rfloor$$

$$\lfloor N/4 \rfloor$$

↓

↓

↓

deepest statement Running.

$$= N + \lfloor N/2 \rfloor + \lfloor N/4 \rfloor + \dots + 1$$

$$= N + \frac{N}{2} + \frac{N}{4} + \dots + 1 \quad (\text{G.P.})$$

$$\left\{ \begin{array}{l} \text{Sum of } N \text{ terms of a G.P.} = \frac{a(1-r^n)}{1-r} \quad (r < 1) \\ \text{Sum of Infinite terms of a G.P.} = \frac{a}{1-r} \end{array} \right.$$

$$\left\{ \begin{array}{l} \text{Sum of Infinite terms of a G.P.} = \frac{a}{1-r} \end{array} \right.$$

(Let assume there are infinite terms)

$$= \frac{N}{1 - \frac{1}{2}}$$

(for higher input, it will work)

$$= \frac{N}{\frac{1}{2}}$$

$$\boxed{T.C = O(N)}$$

③ $a = 0$
 $i = n$
while ($i > 0$)
{
 $a = a + i$
 $i = \lceil \frac{i}{2} \rceil$
}
Print(a)

$N = 5 ; a = 0$
 $i = 5 \rightarrow 2 \rightarrow 1 \rightarrow 0$
 $- N \rightarrow \lceil \frac{N}{2} \rceil, \lceil \frac{N}{4} \rceil, \dots$

while loop is running
for single iteration

After how much time i becomes 1 Number of times, this while loop.

Let 1 After K steps, i becomes 1

$$= \frac{N}{2^0}, \frac{N}{2^1}, \frac{N}{2^2}, \dots, \frac{N}{2^K}$$

Calculating K

$$\frac{N}{2^K} = 1$$

$$K = \log_2 N$$

$$2^K = N$$

$$\log_2 N = \log N$$

$$K = \frac{\log N}{\log 2}$$

time Complexity = $O(\log_2(n))$

Home Work

① $\text{for}(i = N/2; i \leq N; i++)$

{
 for($i=2; i \leq N; i=i \times 2$)
 }
 $2^k = N$
 $k = \log_2(N)$

Point(i, i)

{
 $(10) = N$ deepest statement (No. of
 generation)
 $\log_2(N)$

Soln. $i = N/2$

$i = N/2 + 1$ $\log_2(N)$

$i = N$ $\log_2(N)$

time complexity = $\log_2(N) + \dots + \log_2(N)$
 ($N/2$ times)

$$= \frac{N}{2} \log_2(N)$$

$T.C. = O(N \log_2(N))$

③

Space Complexity - Space as a resource.

- Extra space (memory)

- Extra space used \propto Input size.

ans
whi
S

① $a = 0$
 $j = N$

T.C. $\rightarrow \log(N)$
S.C. $\rightarrow O(1)$

while ($j > 0$)

{
 $a = a + j$
 $j = \lceil j/2 \rceil$

}

Print(a)

{ because when we are increasing the size of input, but space which is used is constant i.e. space is not depending on size of input}

②

ans = []

T.C. $\Rightarrow O(N)$

for ($i = 0$; $i < N$; $i++$), S.C. $\Rightarrow O(1)$

{
 $ans[i] = N + i$
}

{ In this case, the size of ans is depending on size of input}

Print(ans)

③

```
a = 0  
i = N  
ans = []  
while (i > 0)  
{  
    a = a + i  
    ans.push(a)  
  
    i = [i / 2]  
}  
  
print(ans)
```

iteration of while loop
= $\log_2(N)$

T.C $\rightarrow O(\log_2(N))$
S.C $\rightarrow O(\log_2(N))$

* Two Pointers

① Detect Palindrome.

function detectPalindrome(str) {

left = 0

right = str.length - 1

while (left < right) {

if (str[left] != str[right]) {

return "not a palindrome"

}

left++;

right--;

}

return "Palindrome"

$$T.C = O\left(\frac{N}{2}\right) \rightarrow O(N)$$

$$S.C = O(1) \rightarrow O(1)$$

② Two Sum

```
function twoSum(arr) {  
    left = 0;  
    right = arr.length - 1;  
    while (left < right) {  
        sum = arr[left] + arr[right];  
        if (sum == k) {  
            return {left, right};  
        }  
        else if (sum > k) {  
            right--;  
        }  
        else {  
            left++;  
        }  
    }  
    return {-1, -1};  
}
```

T.C $\Rightarrow O(N)$
S.C $\Rightarrow O(1)$

③ Reverse of array -

Function reverseOfArray(arr) {

 while (left < right)

 {

 var temp = arr[left]

 arr[left] = arr[right]

 arr[right] = temp.

 }

 }

T.C $\Rightarrow O(N)$
S.C $\Rightarrow O(1)$

④ Rotate the array -

[1 2 3 4 5]

↓ Reverse the array.

[{5, 4 3 2} 1]

↓ Reverse the array from (0) to (k-1)

[2 3 4 5 {1}]

↓ Reverse the array from (k) to (N-1)

[2 3 4 5 1]

Time Complexity:

Reverse - $O(N)$

(0, $k-1$) - $O(k)$

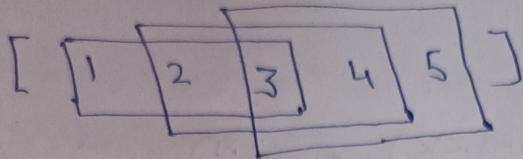
($x, N-1$) - $O(N-i-k) = O(N)$

$$T.C \Rightarrow O(N) + O(k) + O(N)$$

$$\boxed{T.C \Rightarrow O(N)}$$

$$\boxed{S.C \Rightarrow O(1)}$$

* Sliding Window Technique



```
function takeoutMaximum (arr[], K) {
```

```
    max = 0;
```

```
    sum = 0;
```

```
    for (i=0; i < K; i++) {
```

```
        sum += arr[i];
```

```
}
```

```
    if (sum > max) {
```

```
        max = sum;
```

```
}
```

```
    for (i=K; i < arr.length; i++) {
```

```
        sum += arr[i];
```

```
        sum -= arr[i-K];
```

```
        if (sum > max) {
```

```
            max = sum;
```

```
}
```

```
{}
```

```
print(max);
```

```
}
```

T.C $\Rightarrow O(N)$
S.C $\Rightarrow O(1)$