

⇒ Subarray with B odd numbers

Time: $O(n)$ Space: $O(n)$
Hashing we can do

Use hashmap to track frequency of prefix subarrays with given cnt of odd numbers

```
// Idea is to use Hashmaps to track the frequency of prefix subarrays with a given count of odd numbers
int solve(vector<int> &arr, int b) {
    // Subarray with B odd numbers
    // Return Total number of subarray with exactly b odd numbers
    int res = 0;
    unordered_map<int, int> data;
    int odd_cnt = 0;
    data[odd_cnt] = 1;
    for(int i = 0; i < arr.size(); i++){
        if(arr[i] & 1) odd_cnt += 1;
        if(data.find(odd_cnt - b) != data.end()){
            res += data[odd_cnt - b];
        }
        data[odd_cnt] += 1;
    }
    return res;
}
```

Time: $O(n)$
Space: $O(n)$

Subarray with B odd numbers

Programming • Hashing

Medium 63.0% Success

288 9 Bookmark

Asked In:

Problem Description

Given an array of integers A and an integer B.

Find the total number of subarrays having exactly B odd numbers.

Problem Constraints

$1 \leq \text{length of the array} \leq 10^5$

$1 \leq A[i] \leq 10^9$

$0 \leq B \leq A$

Best Approach Time: $O(n)$
Space: $O(1)$

2 Pointers Sliding Window

We can find :

1) At Most x

2) At Most $x-1$

Exactly x

At Most x odd numbers

```
//TO Find the subarray with atMost x odd elements
int atMostX(vector<int> &arr,int x){
    int n = arr.size();
    int odd = 0;
    int ans = 0;
    int start = 0;
    for(int i = 0; i < n; i++){
        if(arr[i] % 2){
            odd += 1;
        }
        //If count of odd elements is greater than x
        //then remove elements from the start
        while(odd > x){
            if(arr[start] % 2){
                odd --;
            }
            start += 1;
        }
        //Add the number of subarray with atMost X
        //Odd elements ending at the current index
        ans += (i - start + 1);
    }
    return ans;
}
```

Example :

arr:

4	3	2	3	4
---	---	---	---	---

$k = 2$

Great! Let's do a very clear and slow dry run for:

ini

[Copy code](#)

```
arr = [4, 3, 2, 3, 4]
k = 2
```

Odd numbers are:

3 (index 1), 3 (index 3)

We will do:

- 1) atMost(2)
- 2) atMost(1)
- 3) exactly K = atMost(2) - atMost(1)

STEP 1 — Dry Run of atMost(2)

Initial:

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```
start = 0
odd = 0
ans = 0
```

★ $i = 0 \rightarrow arr[0] = 4$ (even)

makefile

[Copy code](#)

```
odd = 0
Window = [0..0]
Valid since odd ≤ 2
Subarrays ending at i = (0 - 0 + 1) = 1
ans = 1
```

★ $i = 1 \rightarrow arr[1] = 3$ (odd)

makefile

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```
odd = 1
Window = [0..1]
Still odd ≤ 2 - valid
Subarrays ending at i = (1 - 0 + 1) = 2
ans = 1 + 2 = 3
```

Valid subarrays:

[4,3], [3]

★ $i = 2 \rightarrow arr[2] = 2$ (even)

makefile

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```
odd = 1
Window = [0..2]
Subarrays ending at i = (2 - 0 + 1) = 3
ans = 3 + 3 = 6
```

Valid subarrays:

[4,3,2], [3,2], [2]

★ $i = 3 \rightarrow arr[3] = 3$ (odd)

makefile

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```
odd = 2
Window = [0..3]
odd ≤ 2 - valid
Subarrays ending at i = (3 - 0 + 1) = 4
ans = 6 + 4 = 10
```

Valid subarrays:

[4,3,2,3], [3,2,3], [2,3], [3]

★ $i = 4 \rightarrow arr[4] = 4$ (even)

makefile

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```
odd = 2
Window = [0..4]
Subarrays ending at i = (4 - 0 + 1) = 5
ans = 10 + 5 = 15
```

Valid subarrays:

[4,3,2,3,4], [3,2,3,4], [2,3,4], [3,4], [4]

Total : 15

atMost(2) = 15

🔴 STEP 2 — Dry Run of atMost(1)

Reset:

ini

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```
start = 0
odd = 0
ans = 0
```

★ $i = 0 \rightarrow \text{arr}[0] = 4$

makefile

Copy code

```
odd = 0
Valid
Subarrays = 1
ans = 1
```

★ $i = 3 \rightarrow \text{arr}[3] = 3$ (odd)

makefile

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```
odd = 2 - NOT valid for atMost(1)
We must reduce odds:

start = 0 - arr[0]=4 even - move start - 1
start = 1 - arr[1]=3 odd - odd--- -> odd=1
start = 2

Now window = [2..3]
odd = 1 - valid
Subarrays = (3 - 2 + 1) = 2
ans = 6 + 2 = 8
```

★ $i = 4 \rightarrow \text{arr}[4] = 4$ (even)

ini

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```
odd = 1 - valid
Window = [2..4]
Subarrays = (4 - 2 + 1) = 3
ans = 8 + 3 = 11
```



★ $i = 1 \rightarrow \text{arr}[1] = 3$ (odd)

makefile

Copy code

```
odd = 1
Valid
Subarrays = (1 - 0 + 1) = 2
ans = 1 + 2 = 3
```

★ $i = 2 \rightarrow \text{arr}[2] = 2$

ini

Copy code

```
odd = 1 -> valid
Subarrays = (2 - 0 + 1) = 3
ans = 3 + 3 = 6
```

🔴 FINAL RESULT of atMost(1) = 11

🟢 STEP 3 — EXACTLY K = atMost(2) - atMost(1)

Copy code

```
15 - 11 = 4
```

// Edge case

if $k = 0$

at most (0)

at most (-1)

It can give very small

Add condition

if $C \leq 0$

return 0;

~~Test Case failed~~

[68, 35], 0

Run It

Final Code :

```
//To Find the subarray with atMost x odd elements
int atMostX(vector<int> &arr,int x){
    //Edge Case
    if (x < 0) return 0;
    int n = arr.size();
    int odd = 0;
    int ans = 0;
    int start = 0;
    for(int i = 0;i < n;i++){
        if(arr[i] % 2){
            odd +=1;
        }
        //If count of odd elements is greater than x
        //then remove elements from the start
        while(odd > x){
            if(arr[start] %2){
                odd --;
            }
            start += 1;
        }
        //Add the number of subarray with atMost X
        //Odd elements ending at the current index
        ans += (i - start + 1);
    }
    return ans;
}
```

← This will sm infinite