

⇒ Subarray with B odd numbers

Time:  $O(n)$

Space:  $O(n)$

Hashing we can do

Use hashmap to track frequency  
of prefix subarrays with given  
cnt of odd numbers

#### Subarray with B odd numbers

Programming Hashing

Medium 63.0% Success

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Asked In:

#### Problem Description

Given an array of integers A and an integer B.

Find the total number of subarrays having exactly B odd numbers.

#### Problem Constraints

$1 \leq \text{length of the array} \leq 10^5$

$1 \leq A[i] \leq 10^9$

$0 \leq B \leq A$

```
//Idea is to use Hashmaps to track the frequency of prefix subarrays with a given count of odd numbers
int solve(vector<int> &arr, int b) {
    //Subarray with B odd numbers
    //Return Total number of subarray with exactly b odd numbers
    int res = 0;
    unordered_map<int,int> data;
    int odd_cnt = 0;
    data[odd_cnt] = 1;
    for(int i = 0;i < arr.size();i++){
        if(arr[i] & 1) odd_cnt += 1;
        if(data.find(odd_cnt - b) != data.end()){
            res += data[odd_cnt - b];
        }
        data[odd_cnt] += 1;
    }
    return res;
}
```

Time:  $O(n)$

Space:  $O(n)$

Best Approach

Time:  $O(n)$

Space:  $O(1)$

2 Pointers

Sliding Window

We can find :

1) At Most  $x$



2) At Most  $x - 1$

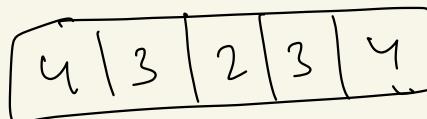
Exactly  $x$

At Most  $x$  odd numbers

```
//TO Find the subarray with atMost x odd elements
int atMostX(vector<int> &arr,int x){
    int n = arr.size();
    int odd = 0;
    int ans = 0;
    int start = 0;
    for(int i = 0;i < n;i++){
        if(arr[i] % 2){
            odd +=1;
        }
        //If count of odd elements is greater than x
        //then remove elements from the start
        while(odd > x){
            if(arr[start] %2){
                odd --;
            }
            start += 1;
        }
        //Add the number of subarray with atMost X
        //Odd elements ending at the current index
        ans += (i - start + 1);
    }
    return ans;
}
```

# Example :

arr:



$$k = 2$$

Great! Let's do a very clear and slow dry run for:

ini

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```
arr = [4, 3, 2, 3, 4]  
k = 2
```

Odd numbers are:

3 (index 1), 3 (index 3)

We will do:

- 1 atMost(2)
- 2 atMost(1)
- 3 exactly K = atMost(2) - atMost(1)

## STEP 1 — Dry Run of atMost(2)

Initial:

```
ini  
  
start = 0  
odd = 0  
ans = 0
```

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★ i = 3 → arr[3] = 3 (odd)

makefile

Copy code

```
odd = 2  
Window = [0..3]  
odd = 2 → valid  
Subarrays ending at i = (3 - 0 + 1) = 4  
ans = 6 + 4 = 10
```

Valid subarrays:

[4,3,2,3], [3,2,3], [2,3], [3]

★ i = 0 → arr[0] = 4 (even)

```
makefile  
  
odd = 0  
Window = [0..0]  
Valid since odd ≤ 2  
Subarrays ending at i = (0 - 0 + 1) = 1  
ans = 1
```

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★ i = 4 → arr[4] = 4 (even)

makefile

Copy code

```
odd = 2  
Window = [0..4]  
Subarrays ending at i = (4 - 0 + 1) = 5  
ans = 10 + 5 = 15
```

Valid subarrays:

[4,3,2,3,4], [3,2,3,4], [2,3,4], [3,4], [4]

★ i = 1 → arr[1] = 3 (odd)

```
makefile  
  
odd = 1  
Window = [0..1]  
Still odd ≤ 2 → valid  
Subarrays ending at i = (1 - 0 + 1) = 2  
ans = 1 + 2 = 3
```

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Valid subarrays:

[4,3], [3]

★ i = 2 → arr[2] = 2 (even)

```
makefile  
  
odd = 1  
Window = [0..2]  
Subarrays ending at i = (2 - 0 + 1) = 3  
ans = 3 + 3 = 6
```

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Valid subarrays:

[4,3,2], [3,2], [2]

Total : 15

atMost(2) = 15

## ● STEP 2 — Dry Run of atMost(1)

Reset:

```
ini  
  
start = 0  
odd = 0  
ans = 0
```

[Copy code](#)

### ★ i = 0 → arr[0] = 4

```
makefile  
  
odd = 0  
Valid  
Subarrays = 1  
ans = 1
```

[Copy code](#)

### ★ i = 1 → arr[1] = 3 (odd)

```
makefile  
  
odd = 1  
Valid  
Subarrays = (1 - 0 + 1) = 2  
ans = 1 + 2 = 3
```

[Copy code](#)

### ★ i = 2 → arr[2] = 2

```
ini  
  
odd = 1 ~ valid  
Subarrays = (2 - 0 + 1) = 3  
ans = 3 + 3 = 6
```

[Copy code](#)

### ★ i = 3 → arr[3] = 3 (odd)

```
makefile  
  
odd = 2 ~ NOT valid for atMost(1)  
We must reduce odds:  
  
start = 0 ~ arr[0]=4 even ~ move start ~ 1  
start = 1 ~ arr[1]=3 odd ~ odd-- ~ odd=1  
start = 2  
  
Now window = [2..3]  
odd = 1 ~ valid  
Subarrays = (3 - 2 + 1) = 2  
ans = 6 + 2 = 8
```

[Copy code](#)

### ★ i = 4 → arr[4] = 4 (even)

```
ini  
  
odd = 1 ~ valid  
Window = [2..4]  
Subarrays = (4 - 2 + 1) = 3  
ans = 8 + 3 = 11
```

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## ● FINAL RESULT of atMost(1) = 11

## ● STEP 3 — EXACTLY K = atMost(2) – atMost(1)

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15 – 11 = 4

## // Edge Case

If  $k = 0$

atMost (0) - atMost (-1)



It can give wrong result

Add condition



```
if Cx < 0  
    return 0;
```

~~Test Case failed~~

[68, 35], 0

Run It

# Final Code :

```
//TO Find the subarray with atMost x odd elements
int atMostX(vector<int> &arr,int x){
    //Edge Case
    if (x < 0) return 0; ← Err
    int n = arr.size();
    int odd = 0;
    int ans = 0;
    int start = 0;
    for(int i = 0;i < n;i++){
        if(arr[i] % 2){
            odd +=1;
        }
        //If count of odd elements is greater than x
        //then remove elements from the start
        while(odd > x){
            if(arr[start] %2){
                odd --; ← This will run
            }                                infinite
            start += 1;
        }
        //Add the number of subarray with atMost X
        //Odd elements ending at the current index
        ans += (i - start + 1);
    }
    return ans;
}
```