

Question 3

Suppose m is any even integer.

Hence, $m = 2k$ for some $k \in \mathbb{Z}$.

$$\begin{aligned}\text{Thus, } m^2 + 2m + 4 &= (2k)^2 + 2(2k) + 4 \\ &= 4k^2 + 4k + 4 \\ &= 2(2k^2 + 2k + 2) \\ &= 2x \text{ where } x = (2k^2 + 2k + 2)\end{aligned}$$

Since $m^2 + 2m + 4$ is even, therefore, the statement is true.