

# Railway Engineering Mathematics

## Tutorial Sheet 13

1. Differentiate the following with respect to the appropriate variable, using either the product rule or the quotient rule as required:

(a)  $y = 8x^5 \sin(2x)$

(b)  $y = e^{-2t} \cosh(7t)$

(c)  $y = \frac{9x^{-3} + 27}{3 \sin(6x)}$

(d)  $x = \frac{7 + \cos(t)}{6t^3} - 5t^2 + 7t - 9$

(e)  $\Delta = (12t^3 - 5t + 3)(3 \cos(4t) + 8t)$

(f)  $Q = 4\sqrt{T} + \frac{6e^{-3T}}{8T + 9}$

(g)  $Z = (2x^3 - 5)e^{-7x}$

(h)  $y = \frac{5 - 6e^{-7x}}{10x - \cos\left(\frac{8x}{3}\right)}$

2. Determine the gradient of the following functions at the point specified:

(a)  $y = \frac{2x^3 - 5x + 7}{5e^{8x}}$  at  $x = 3.5$

(b)  $y = (8x^2 - 5x + 7) \ln(4x) + 9x$  at  $x = 7$