BIRLA INSTITUTE OF TECHNOLOGY AND SCIENCE, PILANI HYDERABAD CAMPUS MATH F444:NUMERICAL SOLUTIONS TO ORDINARY DIFFERENTIAL EQUATIONS First Semester, 2015–16

ASSIGNMENT-1

- 1. Write the MATLAB code to a second order accurate finite difference method to solve the following two point boundary value problems
- (i). $Y'' = \frac{-2x}{1+x^2}Y' + Y + \frac{2}{1+x^2} \log(1+x^2)$ 0 < x < 1 $Y(0) = 0; Y(1) = \log(2)$ (Exact solution : $Y(x) = \log(1+x^2)$).
- (ii). $Y'' = Y + 6x x^3$; Y(0) = 0, Y'(1) = 3.
- (iii). $Y'' + Y = \sin(3x); Y(0) + Y'(0) = -1, Y'(\frac{\pi}{2}) = 1.$
- 2. Compare (graphically) the numerical solution with exact solution for different values of h for the given BVP's.
- 3. Tabulate the global error in max norm in the approximate solution for different step sizes $h = \frac{1}{2^k}, k = 1, ...6$ and verify the rate of convergence of the finite difference method.