

# Relational Algebra and SQL

## 2.4 and 6.1.

Recall:

Relational Algebra (RA)

- Operations on Relations.

Projection

$\pi_{\langle \text{List Expr} \rangle} R$

list of expressions on the attributes of a relation.

Ex.  $R(a,b)$

a	b
1	9
3	3

①  $\pi_a R$

a
1
3

②  $\pi_{a+s, -b} R$

a+s	-b
6	-9
8	-3

name of attributes

$$\textcircled{3} \pi_{b,a} R$$

b	a
9	1
3	3

$$\textcircled{4} \pi_{-1,a} R$$

"-1", a
-1
-1

SQL:

select <list expr> from R

① SELECT a FROM R

② SELECT a+5, -b FROM R

③ SELECT b, a FROM R

④ SELECT -1, a FROM R

Name of Relation optional!!

SELECT 3; 

3
3

 Creates table of

one tuple!!

SELECT 'abc', 5.2

=> 

abc	5.2
'abc'	5.2

name of attribute.

Tupler.

The result of SELECT is always a relation

Renaming Relations and their attributes.

Sometimes we need to rename tables or their attributes.

$\rho_{\langle \text{new schema} \rangle} R$

Ex:

$R(a, b)$

$\rho_{S(c, d)} R$

renames  $R(a, b)$  to

$S(c, d)$

ding notation: you can rename during the projection.

If we want to rename the projected expression we can do it:

$\pi_{a \rightarrow c, b \rightarrow d} R \rightarrow S$

Result schema  $S(c, d)$

Ex: ①  $\Pi_{a+5 \rightarrow x, -b \rightarrow y} R$

x	y
6	-9
8	-3

SQL.

Given  $R(a,b)$   $\rho_{S(c,d)} R$

SELECT a, b FROM R as S(c,d)

or

SELECT a as c, b as d FROM R

①

SELECT a+5 AS x, -b AS y FROM R

## SELECTION

$$\sigma_p R$$

$p$  is a predicate on attributes of  $R$

Expressions:

$<, >, <=, =, >=, <=$   
different equal

AND, NOT and many others.

Ex:

	a	b
$R(a,b)$	3	2
	1	$\emptyset$

$p$  evaluated at each tuple.

$$\textcircled{1} \sigma_{a > 1 \text{ OR } b > 1} R$$

a	b
3	2

SQL.

SELECT \* FROM  $R$  WHERE  $p$

original attributes of  $R$

Ex:

① SELECT \* FROM R  
WHERE  $a > 1$  OR  $b > 1$

We can combine  $\Pi$  and  $\sigma$ :

Ex:  $\Pi_a \sigma_{a > 1 \text{ OR } b > 1} R$

SELECT a FROM R  
WHERE  $a > 1$  OR  $b > 1$

NOT equivalent to.

$\sigma_{a > 1 \text{ OR } \underline{b > 1}} \Pi_a R$

b is not part of  $\Pi_a R$ .

### Questions

What does this return?

1)  $\sigma_{\text{FALSE}} R$

2)  $\sigma_{\text{TRUE}} R$

Other expressions in predicates.

IN

$a \in \text{IN (List)}$

Ex.:

$a \in \text{IN (3, 2, 5)}$

$\Rightarrow$  equivalent to  $(a = 3 \text{ or } a = 2 \text{ or } a = 5)$

But we can also use a query:

$a \in \text{in } (\Pi_c S)$

SQL:

$a \in \text{IN (SELECT c FROM S)}$

EXISTS

$\text{EXISTS (R)}$  true if R not empty

Ex:

$\text{EXISTS } (\sigma_{ass} R)$

## Operations on 2 Relations.

Union	$\cup$
Intersection	$\cap$
Difference (Exapt)	$-$

### Union Compatible

R and S are "union compatible" iff  
 $|\text{attrs}(R)| = |\text{attrs}(S)|$

and the type of the  $i$ -th attribute of S. is **type compatible** with the type of the  $i$ -th attribute of R.

One type- $t_1$  is type compatible with type  $t_2$  if  $t_1$  can be converted to type  $t_2$ .

$A \cup B$   
 $A \cap B$   
 $A - B$  } Defined only iff  
A & B are  
union compatible.



# UNION

$$t \in R \cup S \Leftrightarrow t \in R \text{ or } t \in S$$

$$t \in R \cap S \Leftrightarrow t \in R \text{ and } t \in S$$

$$t \in R - S \Leftrightarrow t \in R \text{ and } t \notin S$$

Schema of result is schema of first relation.

Ex:

R (a, b)		S (c, d)
1   a		1   e
3   x		3   x
		4   f

R ∪ S

a   b
1   a
3   x
1   e
4   f

R ∩ S

a   b
3   x

R - S

a   b
1   a

S - R

c   d
1   e
4   f

SQL

TABLE R { UNION  
INTERSECT  
EXCEPT } TABLE S

or

<QUERY> { UNION  
INTERSECT  
EXCEPT } <QUERY>

SELECT a, b FROM R

UNION

SELECT c, d FROM S;

## NULLS (6.1)

SQL has a special value: NULL .

⇒ unknown.

Example :

- Next year champion of the Stanley Cup.
- Grades of students currently enrolled in this course.
- SQL has special considerations for expressions involving NULL
- SQL Logic 3 valued:
  - True
  - False
  - Unknown
- Any expression involving NULL results into UNKNOWN

### IMPORTANT

$$\left. \begin{array}{l} X = \text{NULL} \\ X > \text{NULL} \end{array} \right\} \Rightarrow \text{UNKNOWN} .$$

To test if attr is NULL use  
$$X \text{ IS NULL}$$

Ex:

$\text{NULL} > 5 \Rightarrow \text{UNKNOWN}$

$X \text{ IS NULL} \Rightarrow \text{True if } X \text{ contains NULL}$

UNKNOWN is NOT TRUE

Ex:

$\text{UNKNOWN OR TRUE} \Rightarrow \text{TRUE}$

$\text{UNKNOWN AND TRUE} \Rightarrow \text{FALSE}$

See exercise !!

Text Matching.

Regular expressions. (Postgres)

$\text{expr} \sim \text{RegExp}$

Ex

$a \sim '^ab'$

attribute a starts with string ab

$a \sim '\.txt\$'$

attribute a end with string .txt

Cross product:  $\times$

Given relations  $R$  and  $S$ .

$(r, t) \in R \times S$  iff  $r \in R$  and  $s \in S$

$R(a, b)$

a	b
1	x
2	y

$S(c, d)$

c	d
5	8
2	12

$T = R \times S$

a	b	c	d
1	x	5	8
1	x	2	12
2	y	5	8
2	y	2	12

What is schema of  $T$ ?

# Natural Join $\bowtie$

Given relations  $R$  and  $S$

$C$  is set of attributes of both  $S$  and  $R$   
with the same name

• if  $C$  is empty.

$$R \bowtie S = R \times S$$

• otherwise

$$\pi_{\text{Attr}(R), \text{Attr}(S) - C}$$

$\uparrow$

Do not project  
both common  
attributes (only  
the first).

$$\sigma_{\bigwedge_{a_i \in C} R_{a_i} = S_{a_i}} (R \times S)$$

$\uparrow$

match tuples  
with same value in  
common attributes.

conjunction over  
all common attributes

Ex:

$R(a, b)$

a	b
1	x
2	y

$S(a, c)$

a	c
5	8
2	12

Common attributes =  $\{a\}$

$$T = R \bowtie S = \Pi_{a,b,c} \sigma_{R.a=S.a}(R \times S)$$

$R \times S$

R.a	R.b	S.a	S.c
1	x	5	8
1	x	2	12
2	y	5	8
2	y	2	12

$\} R.a = S.a$

$R \bowtie S$

a	b	c
2	y	12

## Theta Join

$$R \bowtie_p S = \sigma_p (R \times S)$$

```
SELECT * FROM  
  R JOIN S ON (p);
```

## Cross Product X

$R \times S$

SQL

```
SELECT * FROM R, S;
```

## NATURAL JOIN

$R \bowtie S$

SQL.

```
SELECT * FROM R NATURAL JOIN S
```

## Theta Join

$$R \bowtie_p S = \sigma_p (R \times S)$$

SQL:

```
SELECT * FROM  
  R JOIN S ON (p);
```



FULL { NATURAL JOIN  $R \bowtie S$   
 THETA JOIN  $R \bowtie_P S$

- Compute non-full join
- Add tuples in R not in join padded with NULL
- Add tuple in S not in join padded with NULL

$\therefore R(a,b)$ 

a	b
3	x
1	y

 $S(a,c)$ 

a	c
2	3.1
1	2.5

$R \bowtie S$

a	b	c
1	y	2.5
3	x	<u>⊥</u>
2	<u>⊥</u>	3.1

← Represents NULL in RA

SELECT \* FROM R NATURAL FULL JOIN S

$R \bowtie S$   
 $R.a < S.a$

R.a	b	S.a	c
1	y	2	3.1
3	x	<u>⊥</u>	<u>⊥</u>
<u>⊥</u>	<u>⊥</u>	1	2.5

SELECT \* FROM R FULL JOIN S  
 ON (R.a > S.a)

•  $\left\{ \begin{array}{l} \text{LEFT} \\ \text{RIGHT} \end{array} \right\} \text{ JOIN}$

$R \overset{\circ}{\underset{L}{\bowtie}} S$   
 $R \overset{\circ}{\underset{R}{\bowtie}} S$

- Compute. non-full join
- Add tuples in **LEFT** or **RIGHT** relation, padding other attributes with NULL

Example:

$\therefore R(a,b) \quad \begin{array}{c|c} a & b \\ \hline 3 & x \\ 1 & y \end{array} \quad S(a,c) \quad \begin{array}{c|c} a & c \\ \hline 2 & 3.1 \\ 1 & 2.5 \end{array}$

$R \overset{\circ}{\underset{L}{\bowtie}} S$

a	b	c
1	y	2.5
3	x	1

SELECT \* FROM

R NATURAL LEFT JOIN S;

$R \bowtie_R S$

a	b	c
1	y	2.5
2	⊥	3.1

SELECT \* FROM

R NATURAL RIGHT JOIN S;

$R \bowtie_{L_{R.a < S.a}} S$

R.a	R.b	S.a	S.b
1	y	2	3.1
3	x	⊥	⊥

SELECT \* FROM

R LEFT JOIN S ON  
(R.a < S.a);

## JOIN USING

SQL provides a special variant of NATURAL JOIN in which we can specify the attribute to join by. Ex.

$R(a, b, c)$  and  $S(a, b, d)$

The schema of  $R \bowtie S$   
is  $(a, b, c, d)$

We can specify a join only on  $a$  as follows

SELECT \* FROM

$R$  JOIN  $S$  USING.

The schema is  $(a, R.b, S.b, c, d)$   
We write it as.

$R \bowtie_a S.$

In practice it is a good idea  
to write NATURAL JOINS as  
JOIN USING.

Eg.  $R \bowtie S$

SELECT \* FROM  
R NATURAL JOIN S

The common attributes are  
a, b.

It is better to write it as

SELECT \* FROM  
R JOIN S USING (a, b)

$R \bowtie_{a,b} S$

$\nwarrow$  my notation

For these relations

$R \bowtie S = R \bowtie_{a,b} S$