

Report5

计算方法--第五次程序作业

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牛顿迭代法

"hw_newton.m"是利用牛顿迭代法求根，输出结果包括：初值，根，迭代次数。并且利用最后一次迭代检验二阶收敛性。

"Newton.m"是牛顿迭代法的函数模块

结果：

牛顿迭代法

初值:0.100000, 根: -0.0000000000000000, 迭代次数: 3

初值:0.200000, 根: 0.0000000000000000, 迭代次数: 4

初值:0.900000, 根: -1.732050807568877, 迭代次数: 7

初值:9.000000, 根: 1.732050807568877, 迭代次数: 9

取最后一轮的迭代结果来验证是否为2阶收敛的

k = 1, xk = 6.075000000000000, ek = 4.342949192431123, C = NULL

k = 2, xk = 4.162795697053038, ek = 2.430744889484161, C = 0.128875357807854

k = 3, xk = 2.945153623683457, ek = 1.213102816114580, C = 0.205314134292457

k = 4, xk = 2.219293671090175, ek = 0.487242863521297, C = 0.331093202872011

k = 5, xk = 1.856453816154091, ek = 0.124403008585214, C = 0.524010403990703

k = 6, xk = 1.743532447579469, ek = 0.011481640010591, C = 0.741894512898189

k = 7, xk = 1.732163235312751, ek = 0.000112427743874, C = 0.852836233413889

k = 8, xk = 1.732050818513779, ek = 0.000000010944901, C = 0.865894265361425

分析收敛阶

如程序输出结果所示，我选择了初值为9的迭代序列，因为这个迭代次数比较多，可以更加清楚的看到收敛的结果。

我先预设了收敛阶次数为2，然后利用

```
fprintf("k = %d, xk = %.15f, ek = %.15f, C = %.15f\n", ii, x1, error, error/e^2); %C是渐近误差常数
```

来输出渐近误差常数的结果，最后可以看到，渐近误差常数明显在收敛，收敛值大致为 0.86左右

弦截迭代法

"hw_tang.m"是利用弦截迭代法求根，输出结果包括：初值，根，迭代次数。并且利用最后一次迭代检验收敛性满足 $(1 + \sqrt{5})/2$

"Tangent.m"是弦截迭代法的函数模块

结果：

弦截法

初值: $x_0=-0.100000$, $x_1=0.100000$, 根: 0.0000000000000000 , 迭代次数: 1

初值: $x_0=-0.200000$, $x_1=0.200000$, 根: 0.0000000000000000 , 迭代次数: 1

初值: $x_0=-2.000000$, $x_1=0.900000$, 根: 1.732050807568877 , 迭代次数: 12

初值: $x_0=0.900000$, $x_1=9.000000$, 根: 1.732050807568877 , 迭代次数: 14

这里取最后一次迭代, 验证弦截法迭代收敛阶是否为 $(1+\sqrt{5})/2$

```
k = 1, xk = 0.922678633068692, ek = 8.077321366931308, C = NULL
k = 2, xk = 0.945425651622759, ek = 0.022747018554067, C = 0.000774345988665
k = 3, xk = -4.260255841874963, ek = 5.205681493497723, C = 2371.535483065387325
k = 4, xk = 1.111142329459913, ek = 5.371398171334876, C = 0.372222181489314
k = 5, xk = 1.279507739861510, ek = 0.168365410401598, C = 0.011090387765539
k = 6, xk = 2.627632903195471, ek = 1.348125163333961, C = 24.081268764321550
k = 7, xk = 1.475358392278638, ek = 1.152274510916833, C = 0.710637396087242
k = 8, xk = 1.597341561251019, ek = 0.121983168972381, C = 0.096984042848802
k = 9, xk = 1.772723874716548, ek = 0.175382313465529, C = 5.276957459490521
k = 10, xk = 1.726991772050257, ek = 0.045732102666291, C = 0.764676687530142
k = 11, xk = 1.731876796901183, ek = 0.004885024850926, C = 0.718909896388291
k = 12, xk = 1.732051572649817, ek = 0.000174775748634, C = 0.959341601223050
k = 13, xk = 1.732050807453568, ek = 0.000000765196249, C = 0.919530229430167
k = 14, xk = 1.732050807568877, ek = 0.000000000115309, C = 0.908087801932059
```

分析收敛阶

如程序输出结果所示, 我选择了初值为 $x_0=0.9$, $x_1=9$ 的迭代序列, 因为这个迭代次数比较多, 可以更加清楚的看到收敛的结果。

我先预设了收敛阶次数为 $(1 + \sqrt{5})/2$, 然后利用

```
a = (1+sqrt(5))/2;

fprintf("k = %d, xk = %.15f, ek = %.15f, C = %.15f\n", k, x2, error,
error/e^(a)); %C是渐近误差常数
```

来输出渐近误差常数的结果, 最后可以看到, 渐近误差常数明显在收敛, 收敛值大致为 **0.91**左右