

# COMP1036 – Revision

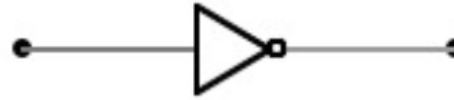
# General Information

- Exam – 50% of the total mark
- 1 hour – 2 questions
- Postpone to the beginning of next semester

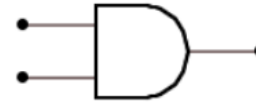
# Part 1

# Elementary Logic Gates

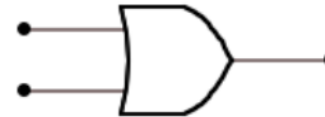
$$A = \bar{A}$$



$$A \text{ AND } B = A \cdot B$$



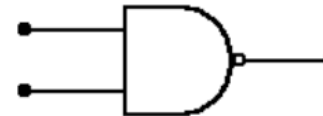
$$A \text{ OR } B = A + B$$



$$A \text{ XOR } B = A \oplus B$$



$$A \text{ NAND } B = \overline{A \cdot B}$$



$$A \text{ NOR } B = \overline{A + B}$$



# Collection of Elementary Logic Gates

$$A = \bar{A} \quad \text{---} \triangle \text{---}$$

A	$\bar{A}$
0	1

$$A \text{ XOR } B = A \oplus B \quad \text{---} \text{---} \text{---} \text{---} \text{---}$$

A	B	$A \oplus B$
0	0	0
0	1	1
1	0	1
1	1	0

$$A \text{ AND } B = A \cdot B \quad \text{---} \text{---} \text{---} \text{---}$$

A	B	$A \cdot B$
0	0	0
0	1	0
1	0	0
1	1	1

$$A \text{ NAND } B = \overline{A \cdot B} \quad \text{---} \text{---} \text{---} \text{---}$$

A	B	$\overline{A \cdot B}$
0	0	1
0	1	1
1	0	1
1	1	0

$$A \text{ OR } B = A + B \quad \text{---} \text{---} \text{---} \text{---}$$

A	B	$A + B$
0	0	0
0	1	1
1	0	1
1	1	1

$$A \text{ NOR } B = \overline{A + B} \quad \text{---} \text{---} \text{---} \text{---}$$

A	B	$\overline{A + B}$
0	0	1
0	1	0
1	0	0
1	1	0

# Boolean Logic

## All chips constructed from elementary logic gates

- Every chip can be built from a combination of:
  - AND
  - OR
  - NOT
  - No integration, division, differentiation...
  - “**Canonical Representation**”
- AND, OR and NOT can be built from NAND
- Therefore every possible chip can be built from just the NAND gates!!!!



George Boole, 1815-1864  
(*"A Calculus of Logic"*)

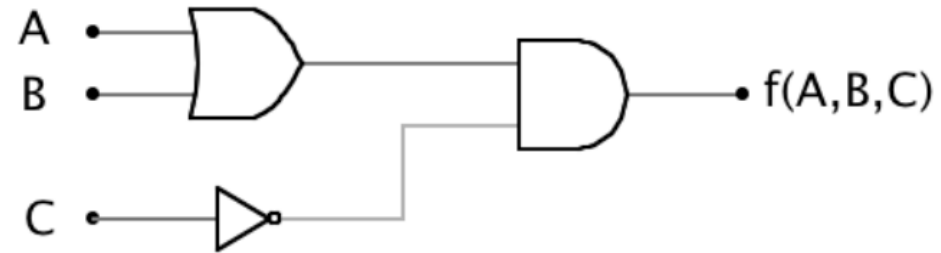
# Boolean Function

- A Boolean function is a function that operates on binary inputs and return binary outputs
- Truth table is **every possible function evaluation** of the input variables
- [note 0 and 1 used to define false and true]
- Everything can be defined by a truth table

# Composite Gates

$$f(A,B,C) = (A + B) \cdot \overline{C}$$

(A OR B) AND NOT C



A	B	C	$f(A,B,C)$
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0



# Precedence

- Precedence

**Parentheses** evaluated first

Then **Not**

Then **And**

Then **Or**

**Not X Or Y And Z = (Not X) Or (Y And Z)**

**Not X And Y Or Z = ((Not X) And Y) Or Z**

Brackets over-rule everything...use when in doubt

**((Not (X)) And (Y)) Or (Z)**

# Laws of Boolean Algebra

## 1. Law of Identity

$$A = A$$

$$\bar{A} = \bar{A}$$

## 2. Commutative Law

$$A \cdot B = B \cdot A$$

$$A + B = B + A$$

## 3. Associative Law

$$(A \cdot B) \cdot C = A \cdot (B \cdot C)$$

$$(A + B) + C = A + B + C$$

## 4. Idempotent Law

$$A \cdot A = A$$

$$A + A = A$$

## 5. Double Negative Law

$$\bar{\bar{A}} = A$$

## 6. Complementary Law

$$A \cdot \bar{A} = 0$$

$$A + \bar{A} = 1$$

## 7. Law of Intersection

$$A \cdot 1 = A$$

$$A \cdot 0 = 0$$

## 8. Law of Union

$$A + 1 = 1$$

$$A + 0 = A$$

## 9. Distributive Law

$$A \cdot (B + C) = (A \cdot B) + (A \cdot C)$$

$$A + (B \cdot C) = (A + B) \cdot (A + C)$$

## 10. Law of Absorption

$$A \cdot (A + B) = A$$

$$A + A \cdot B = A$$

## 11. Law of Common Identities

$$A \cdot (\bar{A} + B) = AB$$

$$A + (\bar{A} \cdot B) = A + B$$

## 12. De Morgan's Law

$$\overline{A \cdot B} = \bar{A} + \bar{B}$$

$$\overline{A + B} = \bar{A} \cdot \bar{B}$$

# Simplify Boolean Expression

$\text{Not}(\text{Not}(x) \text{ And } \text{Not}(x \text{ Or } y)) =$

$\text{Not}(\text{Not}(x) \text{ And } (\text{Not}(x) \text{ And } \text{Not}(y))) =$

$\text{Not}((\text{Not}(x) \text{ And } \text{Not}(x)) \text{ And } \text{Not}(y)) =$

$\text{Not}(\text{Not}(x) \text{ And } \text{Not}(y)) =$

$\text{Not}(\text{Not}(x \text{ Or } y)) =$

double negation

$x \text{ Or } y$

# Boolean Arithmetic

# Binary to Decimal

- Each binary digit corresponds to a power of 2:

Place	7 <sup>th</sup>	6 <sup>th</sup>	5 <sup>th</sup>	4 <sup>th</sup>	3 <sup>rd</sup>	2 <sup>nd</sup>	1 <sup>st</sup>	0 <sup>th</sup>
Weight	$2^7$ = 128	$2^6$ = 64	$2^5$ = 32	$2^4$ = 16	$2^3$ = 8	$2^2$ = 4	$2^1$ = 2	$2^0$ = 1

- Where the digit is 1, we add the corresponding weight
- Example: convert  $1100\ 1010_2$  into decimal

$$\begin{aligned}1100\ 1010_2 &= 1 \times 128 + 1 \times 64 + 0 \times 32 + 0 \times 16 \\&\quad + 1 \times 8 + 0 \times 4 + 1 \times 2 + 0 \times 1 \\&= 128 + 64 + 8 + 2 = 202_{10}\end{aligned}$$

# Decimal to Binary

- Repeatedly divide by 2, until we reach 0
- The **right/left**-most binary digit is the **first/last** remainder
- E.g.  $101_{10} = 1100101_2$

101	Remainder
50	1
25	0
12	1
6	0
3	0
1	1
0	1

- Example: convert  $163_{10}$  into binary
- $10100011_2$

# Decimal to Binary (look-up table)

- $87 = 64$  ( $64 = 2^6$ , the biggest  $2^n$  that 87 is divisible by) + 23 (remainder)
- $87 = 64 + 16$  ( $16 = 2^4$ , the biggest  $2^n$  that 23 is divisible by) + 7 (remainder)
- $87 = 64 + 16 + 4$  ( $4 = 2^2$ , the biggest  $2^n$  that 7 is divisible by) + 3 (remainder)
- $87 = 64 + 16 + 4 + 2$  ( $2 = 2^1$ , the biggest  $2^n$  that 3 is divisible by) + 1 (remainder)
- $87 = 64 + 16 + 4 + 2 + 1$  ( $1 = 2^0$ , the biggest  $2^n$  that 1 is divisible by) + 0 (remainder)
- Stop when remainder = 0

# Representing Negative Numbers

- So far, unsigned numbers
  - How are negative numbers represented on a computer?
- What we use in decimal notation
  - +/– and 0, 1, 2, . . .
- Such a representation is called **sign and magnitude**
- For binary numbers – define **leftmost** bit to be the **sign**
  - $0 \Rightarrow +$ ,  $1 \Rightarrow -$
  - Rest of bits can be numerical value of number
  - Hence, only seven bits are left in a byte (apart from the sign bit), the magnitude can range from 0000000 (0) to 1111111 (127)
- Problems?



# One's Complement

- Alternatively, a system known as **one's complement** can be used to represent negative numbers
- A negative binary number is the bitwise **NOT** applied to it — the "**complement**" of its positive counterpart
- E.g. the ones' complement form of 00101011 ( $43_{10}$ ) becomes 11010100 ( $-43_{10}$ )
- Still has two representations of 0: 00000000 (+0) and 11111111 (-0)
- The range of signed numbers using one's complement is represented by  $-(2^{N-1} - 1)$  to  $(2^{N-1} - 1)$  and  $\pm 0$ 
  - A conventional eight-bit byte is  $-127_{10}$  to  $+127_{10}$  with zero being either 00000000 (+0) or 11111111 (-0)

# Excess- $n$

- **Excess- $n$** , also called offset binary or biased representation, uses a pre-specified number  $n$  as a biasing value
- A value is represented by the unsigned number which is  $n$  greater than the intended value
- Therefore 0 is represented by  $n$ , and  $-n$  is represented by the all-zeros bit pattern
- E.g. Excess-3
  - 0 is represented by 0011 (3)
  - +1 is represented by 0100 (4), +2 is represented by 0101(5)...
  - -1 is represented by 0010 (2), -2 is represented by 0001 (1)
  - -3 is represented by 0000 (0)

# Two's Complement

- The **two's complement** of an  $N$ -bit binary number is defined as the complement with respect to  $2^N$ 
  - It is the result of subtracting the number from  $2^N$
  - $-x$  is represented as  $2^N - x$
- There's a quicker way to calculate  $2^N - x$ :
  - $x + (1\text{'s complement of } x) = 2^N - 1$  (all 1 bits)
  - $2^N - x = (1\text{'s complement of } x) + 1$
  - Take the bitwise inverse (**NOT**) of  $x$ , then add 1 to result
- An  $N$ -bit two's-complement numeral system can represent every integer in the range  $-(2^{N-1})$  to  $+(2^{N-1} - 1)$ 
  - One's complement:  $-(2^{N-1} - 1)$  to  $(2^{N-1} - 1)$
- The sum of a number and its two's complement will always equal 0 (the last digit is ignored)
  - The sum of a number and its one's complement will always equal -0 (all 1 bits)

# Example of 4-Bit Signed Encodings

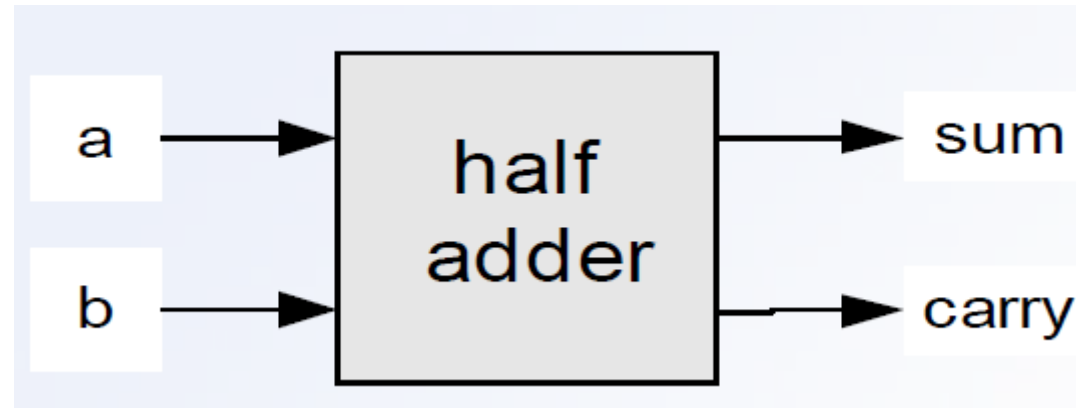
Sign and Mag.		Ones' Comp.		Excess-3		Two's Comp.	
1111	-7	1000	-7	0000	-3	1000	-8
1110	-6	1001	-6	0001	-2	1001	-7
1101	-5	1010	-5	0010	-1	1010	-6
1100	-4	1011	-4	0011	0	1011	-5
1011	-3	1100	-3	0100	+1	1100	-4
1010	-2	1101	-2	0101	+2	1101	-3
1001	-1	1110	-1	0110	+3	1110	-2
1000	-0	1111	-0	0111	+4	1111	-1
0000	+0	0000	+0	1000	+5	0000	0
0001	+1	0001	+1	1001	+6	0001	+1
0010	+2	0010	+2	1010	+7	0010	+2
0011	+3	0011	+3	1011	+8	0011	+3
0100	+4	0100	+4	1100	+9	0100	+4
0101	+5	0101	+5	1101	+10	0101	+5
0110	+6	0110	+6	1110	+11	0110	+6
0111	+7	0111	+7	1111	+12	0111	+7

# Adder

- Build an Adder:
  - Half adder: adds two bits
  - Full adder: adds three bits
  - Adder: adds two integers

# Half Adder

- Add **two** single binary digits and provide the **output** plus a **carry value**
- It has two inputs, called A(a) and B(b), and two outputs S (sum) and C (carry)



# Half Adder

- Least significant bit in the addition is called sum ( $a+b$ )
- Most significant bit is called carry (carry of  $a+b$ )

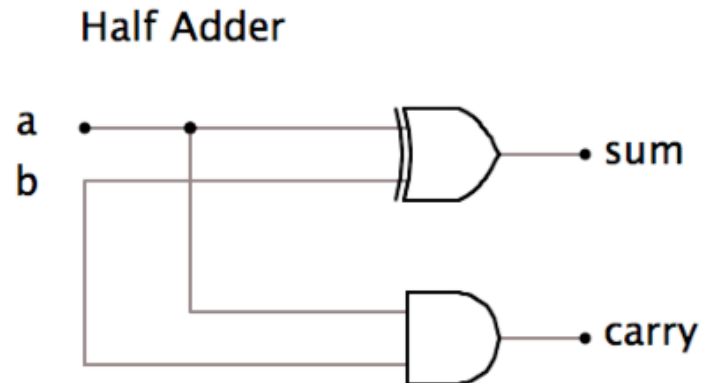
a	b	Carry	Sum
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

- **Never has a situation when sum and carry are both 1**

# Half Adder

a	b	Carry	Sum
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

- The common representation uses a XOR and a AND gate





# Full Adder

- Add **three** single binary digits and provide the **output** plus a **carry value**
- It has three inputs, called A, B and Carry(in), and two outputs S (sum) and Carry(out)



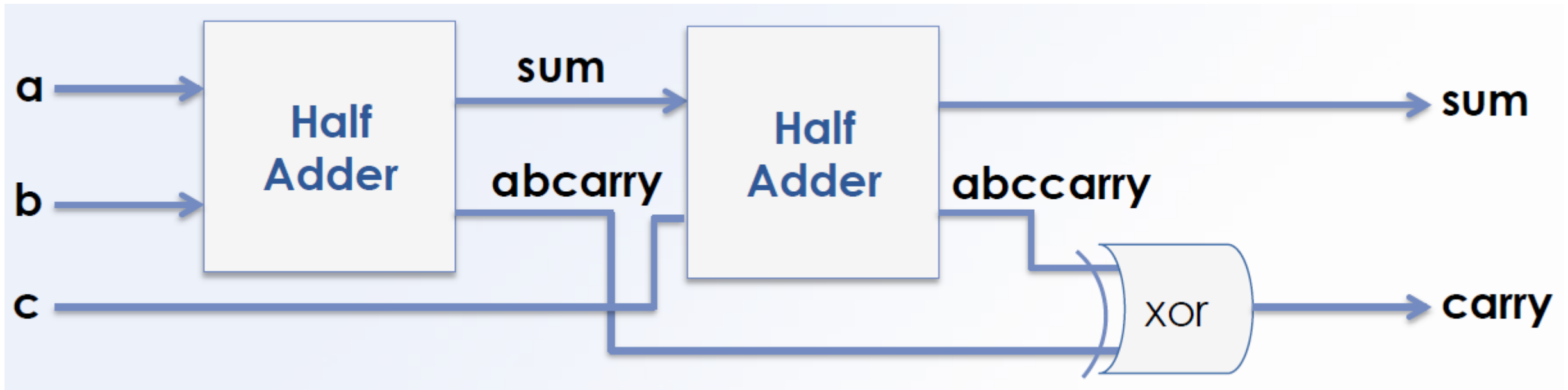
# Full Adder

- Least significant bit in the addition is called sum ( $a+b+c_{in}$ )
- Most significant bit is called carry(out) (carry of  $a+b+c_{in}$ )

a	b	Carry(in)	Carry(out)	Sum
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

# Full Adder: Implementation

- Use two half adders to build a full adder



A	B	$A \oplus B$
0	0	0
0	1	1
1	0	1
1	1	0

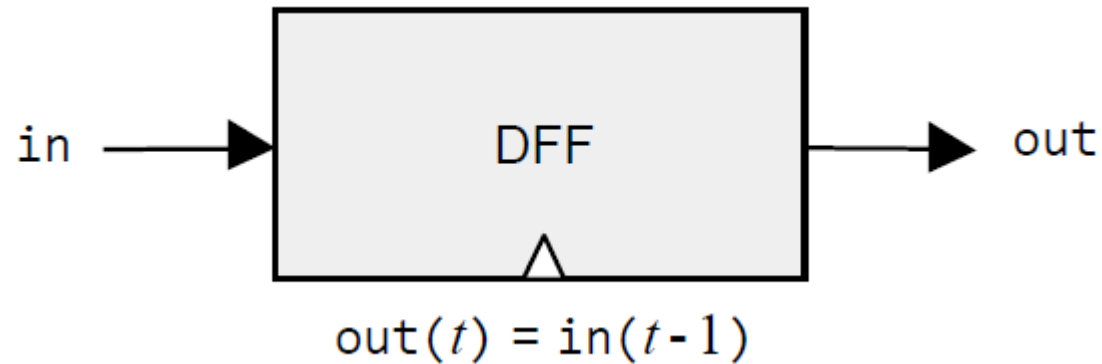
# Sequential Logic and ALU

# Sequential Logic Circuits

- Combinational chips compute functions that **depend solely on combinations of their input values**
- Sequential Logic Circuits
  - Output depends **not only on the present value** of its input signals but **on the sequence of past inputs**, the input history as well

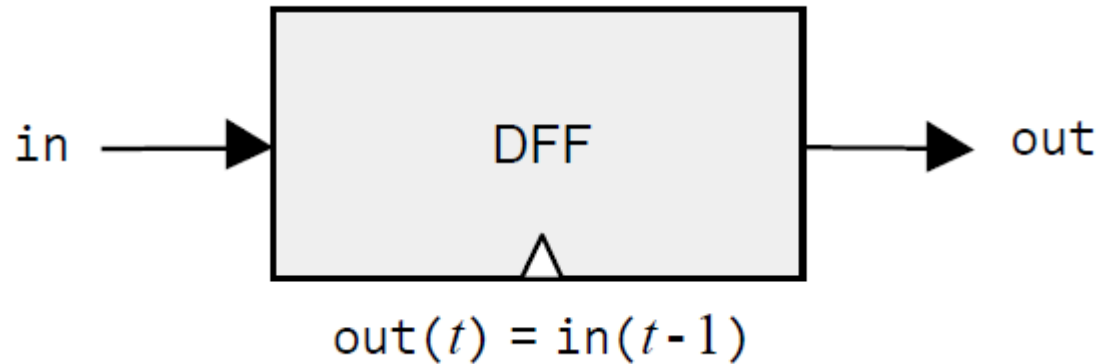
# Flip Flops

- The flip flop is the most elementary sequential element in the computer
- Data Flip Flop (DFF): the simplest state keeping gate (built-in)



- Contains a **single** bit **input** and a **single** bit **output**

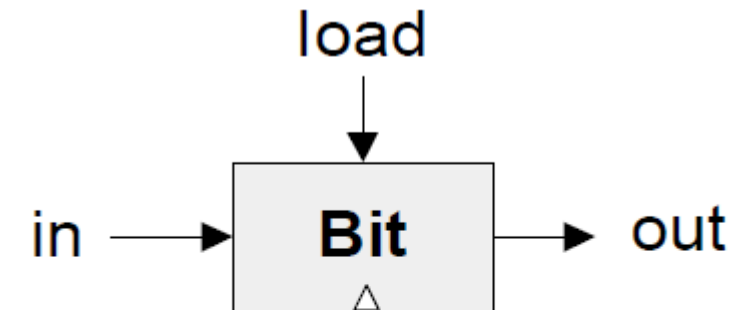
# Flip Flops



- The gate outputs its previous input:  $out(t) = in(t-1)$
- Implementation: a gate that can flip between two stable states:
  - Remembering 0/Remembering 1
  - Also can be made from looping NAND gates

# Register

- A register is a storage device that can “**store**” or “**remember**” a value over time
- Typically is composed of flip flops
- 1-bit register:
  - Store (maintain) a bit
  - Until it is instructed to load(store) another bit

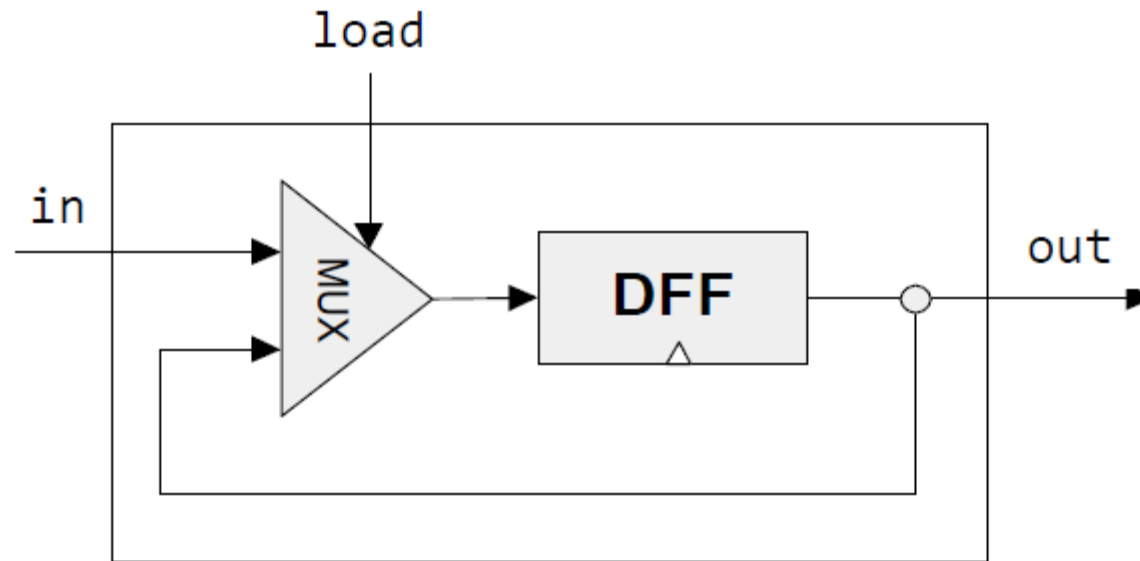


if  $\text{load}(t)$  then  $\text{out}(t+1) = \text{in}(t)$   
else  $\text{out}(t+1) = \text{out}(t)$



# 1-bit Register: Implementation

- The select bit of the Mux can become the load bit!



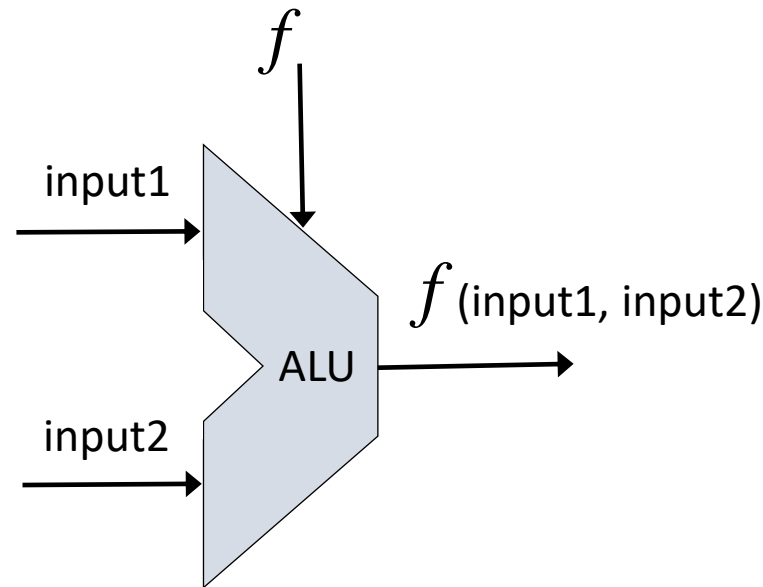
# Arithmetic Logical Unit

- **A combinational circuit** that performs arithmetic and bitwise operations on integers represented as binary numbers.
- Input the **data** and some **code for the operation**
- Output will be some **data** and any **additional information**
- ALUs perform simple functions, because of this they can be executed at high speeds (i.e., very short propagation delays)

# The Arithmetic Logical Unit

The ALU computes a function on the two inputs, and outputs the result

$f$ : one out of a family of pre-defined arithmetic and logical functions

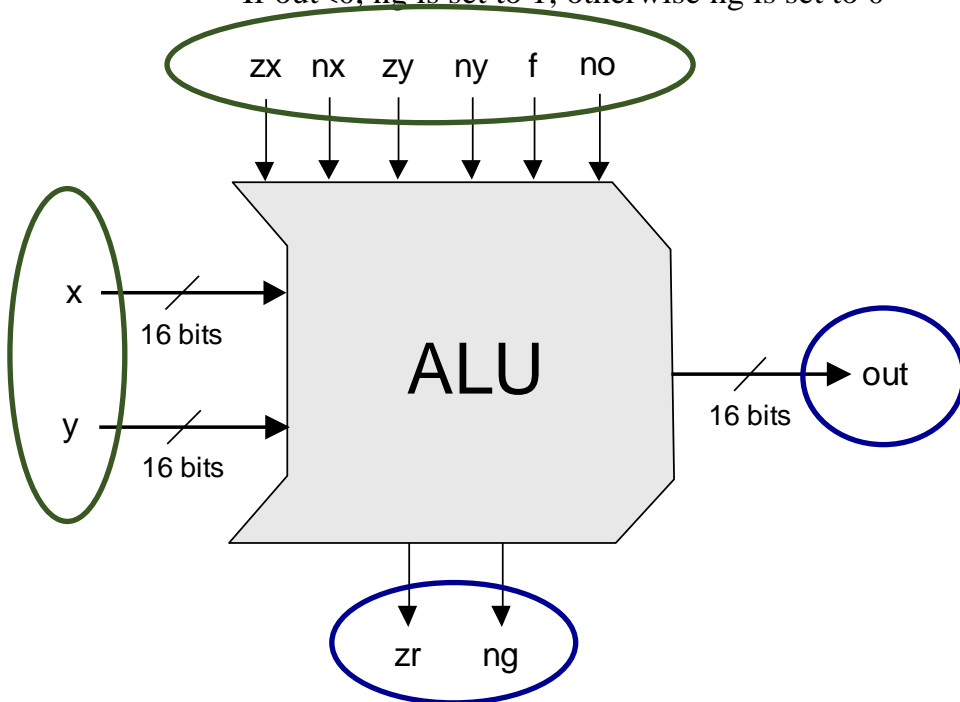


- Arithmetic functions: integer addition, multiplication, division, ...
- logical functions: And, Or, Xor, ...

Which functions should the ALU perform?  
A hardware / software tradeoff.

# The Hack ALU

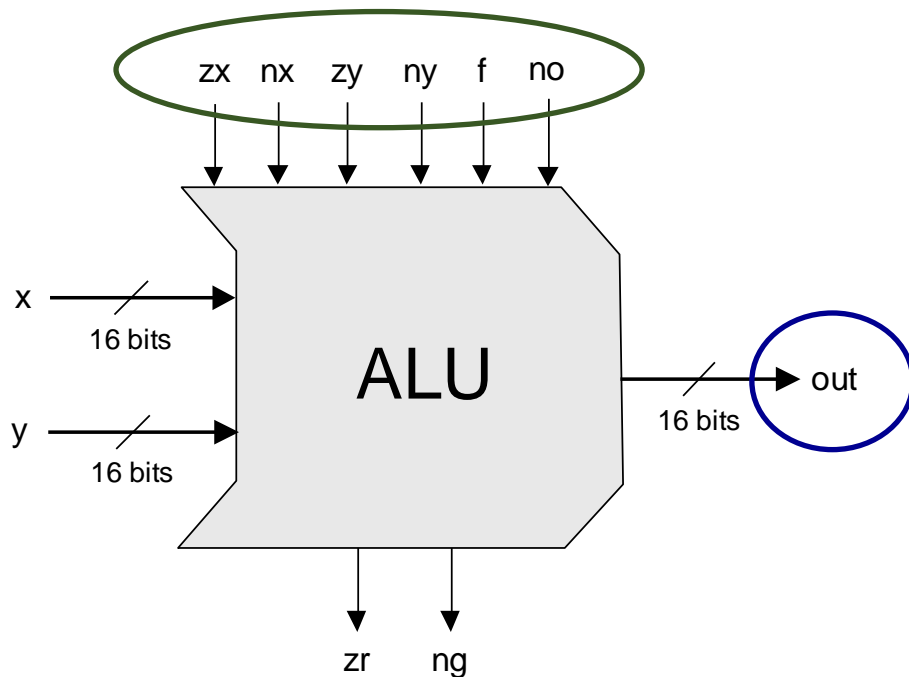
- Operates on two 16-bit, two's complement values
- Outputs a 16-bit, two's complement value
- Which function to compute is set by six 1-bit inputs
- Computes one out of a family of 18 functions
- Also outputs two 1-bit values
  - if the ALU output is 0, zr is set to 1; otherwise zr is set to 0
  - If  $\text{out} < 0$ , ng is set to 1; otherwise ng is set to 0



out
0
1
-1
x
y
!x
!y
-x
-y
x+1
y+1
x-1
y-1
x+y
x-y
y-x
x&y
x y

# The Hack ALU

To cause the ALU to compute a function, set the control bits to one of the binary combinations listed in the table.



control bits

zx	nx	zy	ny	f	no	out
1	0	1	0	1	0	0
1	1	1	1	1	1	1
1	1	1	0	1	0	-1
0	0	1	1	0	0	<i>x</i>
1	1	0	0	0	0	<i>y</i>
0	0	1	1	0	1	! <i>x</i>
1	1	0	0	0	1	! <i>y</i>
0	0	1	1	1	1	- <i>x</i>
1	1	0	0	1	1	- <i>y</i>
0	1	1	1	1	1	<i>x</i> +1
1	1	0	1	1	1	<i>y</i> +1
0	0	1	1	1	0	<i>x</i> -1
1	1	0	0	1	0	<i>y</i> -1
0	0	0	0	1	0	<i>x</i> + <i>y</i>
0	1	0	0	1	1	<i>x</i> - <i>y</i>
0	0	0	1	1	1	<i>y</i> - <i>x</i>
0	0	0	0	0	0	<i>x</i> & <i>y</i>
0	1	0	1	0	1	<i>x</i>   <i>y</i>

Memory

# Fetch-Decode-Execute Cycle

- At some level, every programmable processor implements a **fetch-execute cycle**
- Automatically implemented by processor hardware, allows processor to move through program steps
- **Fetch** — The opcode for the instruction is fetched from memory
- **Decode** — Opcode decoded to work what parts of the CPU are needed
- **Execute** — CPU processes the instruction
- And repeat for the next instruction

# Fetch-Execute Algorithm

Repeat {

## **Fetch (PC) :**

- Fetch the instruction word (at PC)
- Instruction decoded
- Calculate next instruction address

## **Execute (ALU, Registers and Control) :**

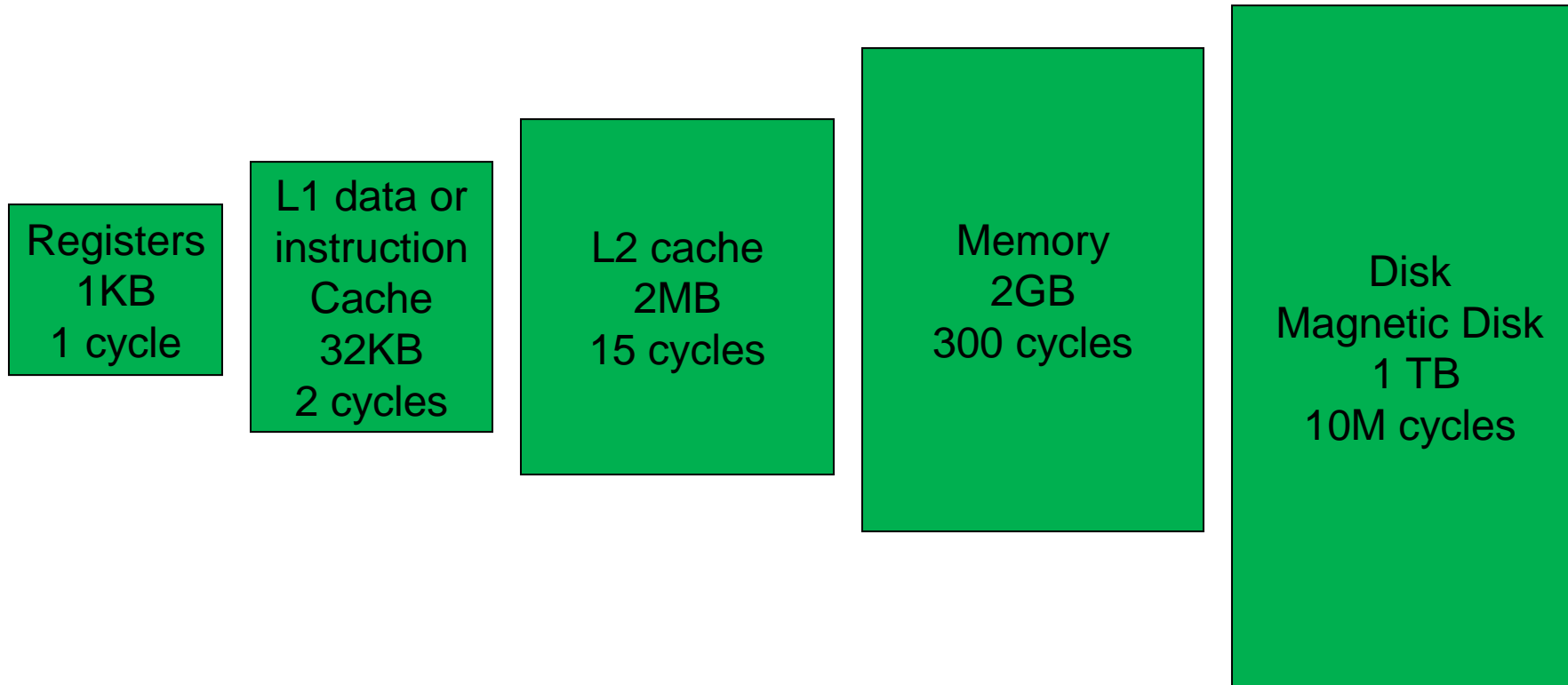
- Read operands
- Executes the operations
- Write/store results

}



# Memory Hierarchy

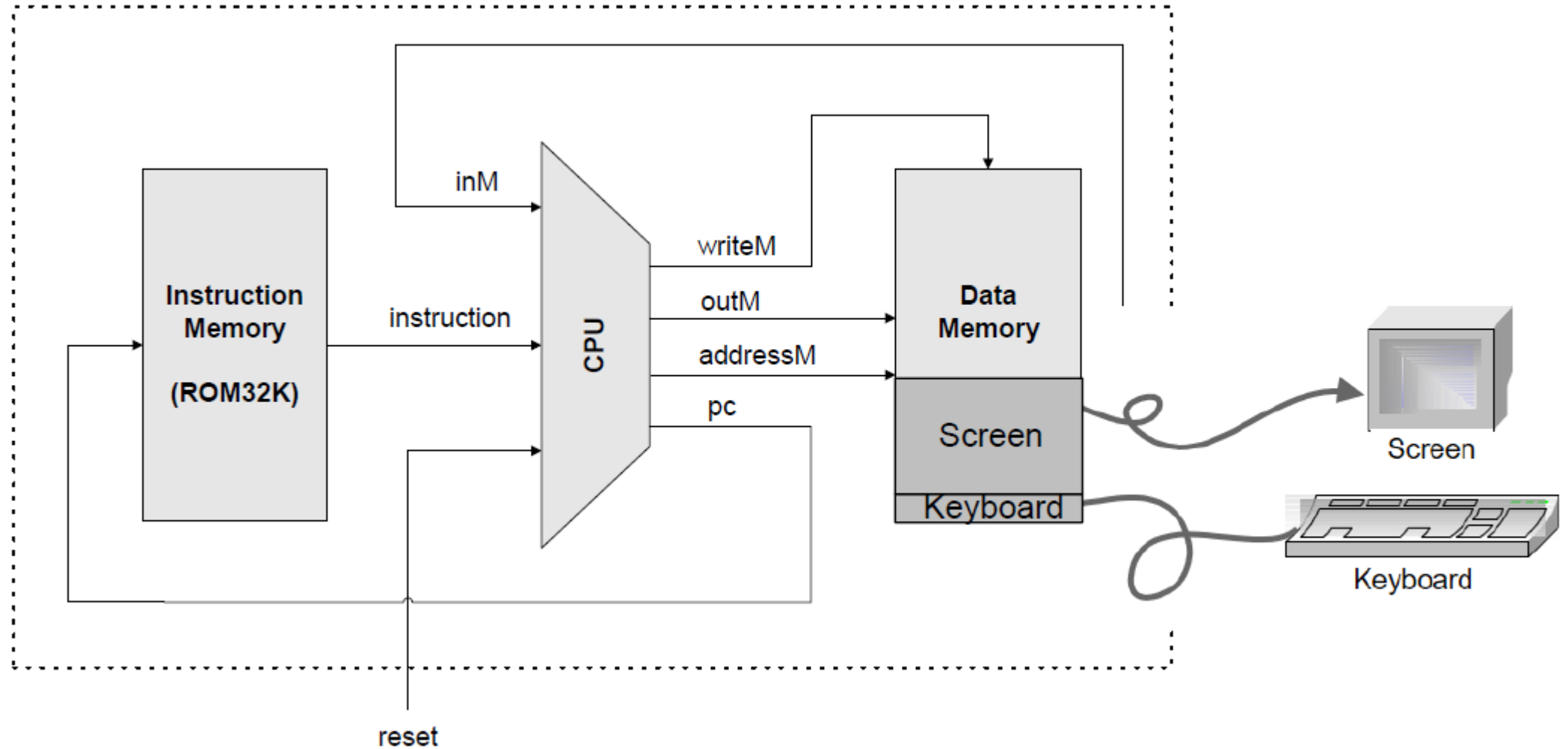
- As it goes further, capacity and latency increase



# The Hack Computer: Main Parts

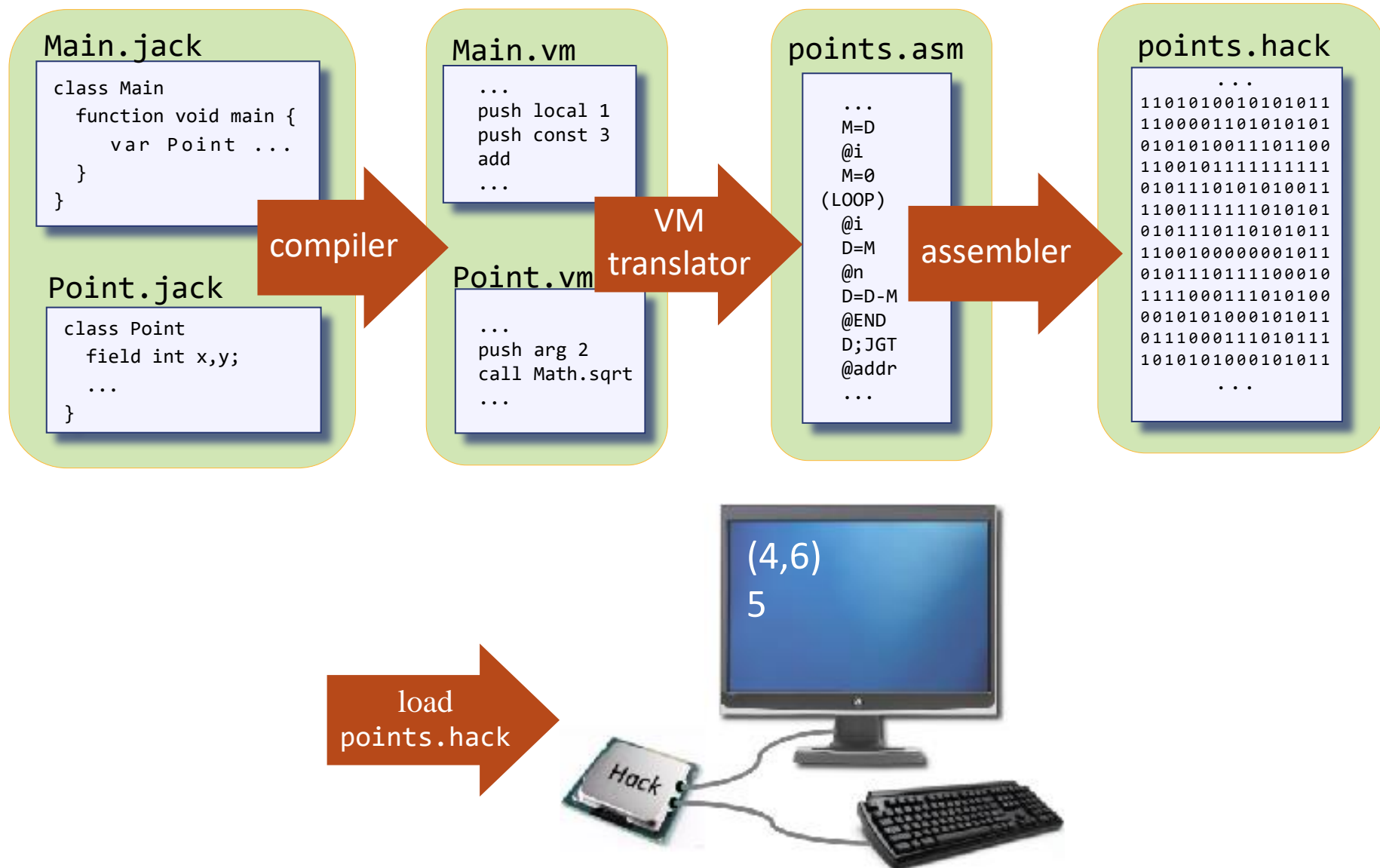
- Instruction memory (ROM)
- Memory (RAM)
  - Data memory
  - Screen (memory map)
  - Keyboard (memory map)
- CPU
- Computer (the logic that holds everything together)

# The Hack Computer (Put Together)



# Part 2

# Big picture

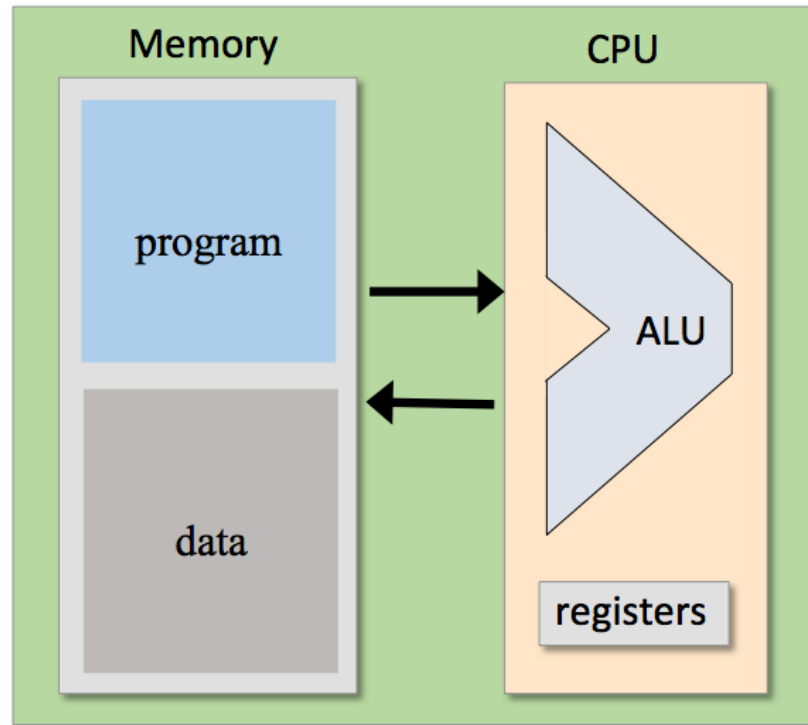


# Outlines

- Hack assembly programming
- Assembler
- Virtual machine

# An informal definition

- A *machine language* can be viewed as an agreed-upon formalism, designed to manipulate a *memory* using a *processor* and a set of *registers*. (Nisan & Schocken)

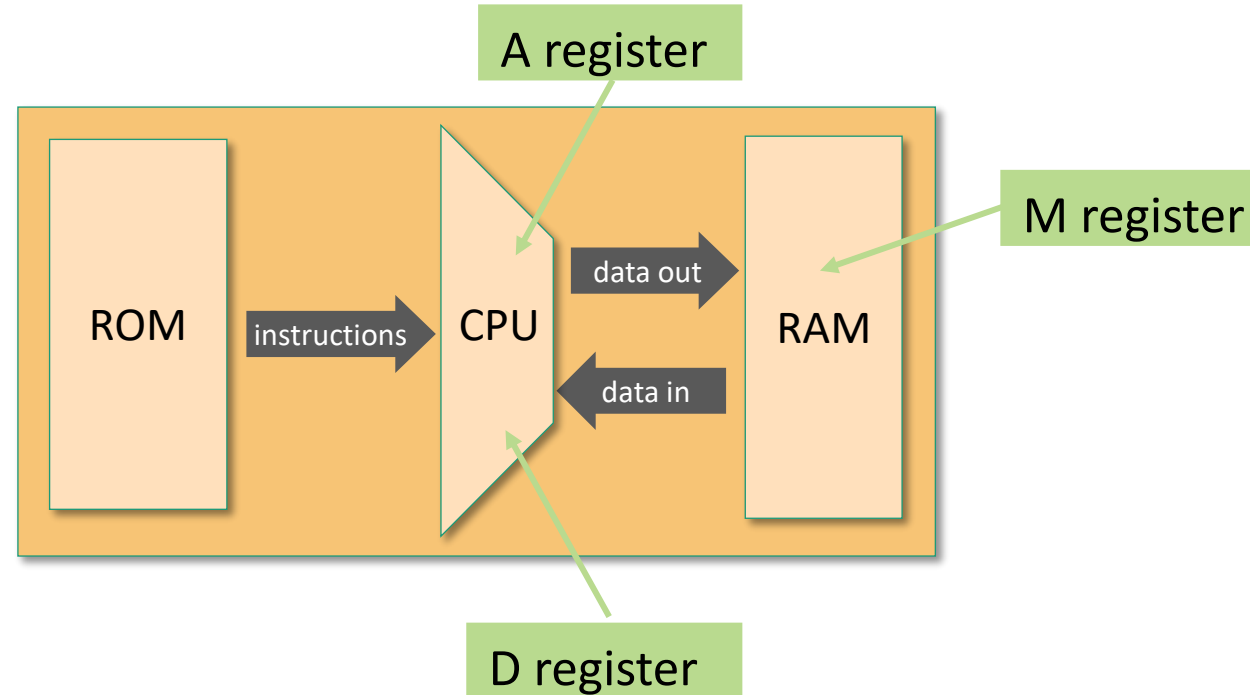


# Addressing modes

- Register
  - `ADD R1, R2`      `// R2 ← R2 + R1`
  - Access data from a **register** R2.
- Direct
  - `ADD R1, M[67]`    `// Mem[67] ← Mem[67] + R1`
  - `LOAD R1, 67`      `// R1 ← Mem[67]`
  - Access data from **fixed memory address** 67.
- Indirect
  - `ADD R1, @A`      `// Mem[A] ← Mem[A] + R1`
  - Access data from **memory address specified by variable A**.
- Immediate
  - `ADD 67, R1`      `// R1 ← R1 + 67`
  - `LOADI R1, 67`    `// R1 ← 67`
  - Access the data of **value** 67 immediately.



# Hack computer: registers



- Three 16-bit registers:
  - D: Store data
  - A: Store data / address the memory
  - M: Represent currently addressed memory register: **M = RAM[A]**

# A-instruction specification

Semantics: Set the A register to *value*

Symbolic syntax:

@ *value*

Example:

@ 21

set A to 21

Where *value* is either:

- a non-negative decimal constant  $\leq 65535$  ( $=2^{15}-1$ ) or
- a symbol referring to a constant (*come back to this later*)

Binary syntax:

0 *value*

Where *value* is a 15-bit binary constant

Example:

0 0000000000010101

opcode signifying  
an A-instruction

set A to 21

# C-instruction

Syntax: `dest = comp ; jump` (both *dest* and *jump* are optional)

where:

*comp* =

0, 1, -1, D, A, !D, !A, -D, -A, D+1, A+1, D-1, A-1, D+A, D-A, A-D, D&A, D|A  
M, !M, -M, M+1, M-1, D+M, D-M, M-D, D&M, D|M

*dest* =

null, M, D, MD, A, AM, AD, AMD (M refer to **RAM[A]**)

*jump* =

null, JGT, JEQ, JGE, JLT, JNE, JLE, JMP

## Semantics:

- Computes the value of *comp*
- Stores the result in *dest*
- If the Boolean expression (***comp jump 0***) is true, jumps to execute the instruction at **ROM[A]**

# C-instruction specification

Symbolic syntax:

*dest* = *comp* ; *jump*

Binary syntax:

1 1 1 a c1 c2 c3 c4 c5 c6 d1 d2 d3 j1 j2 j3

opcode

not used

*comp* bits

*dest* bits

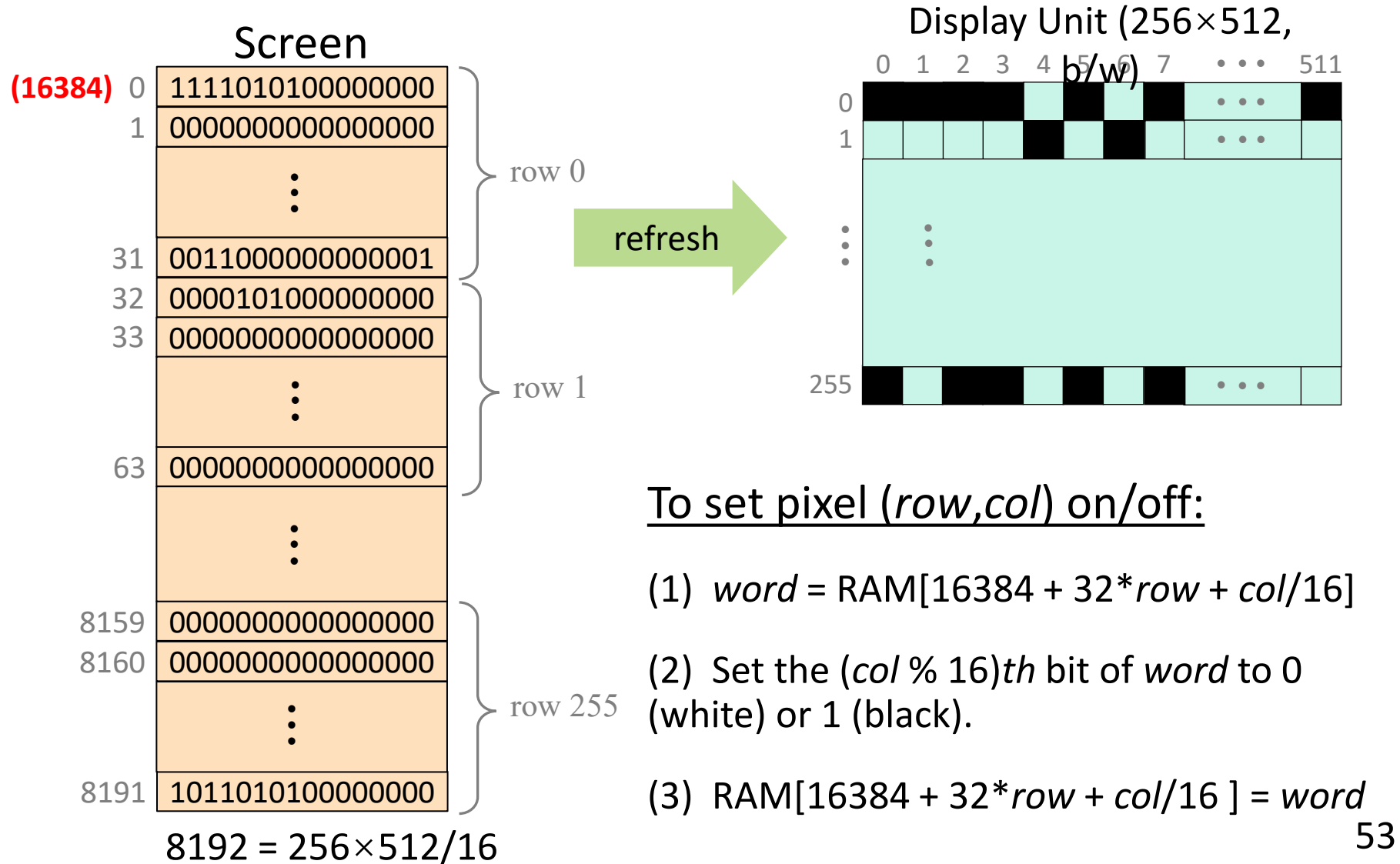
*jump* bits

<i>comp</i>		c1	c2	c3	c4	c5	c6
0		1	0	1	0	1	0
1		1	1	1	1	1	1
-1		1	1	1	0	1	0
D		0	0	1	1	0	0
A	M	1	1	0	0	0	0
!D		0	0	1	1	0	1
!A	!M	1	1	0	0	0	1
-D		0	0	1	1	1	1
-A	-M	1	1	0	0	1	1
D+1		0	1	1	1	1	1
A+1	M+1	1	1	0	1	1	1
D-1		0	0	1	1	1	0
A-1	M-1	1	1	0	0	1	0
D+A	D+M	0	0	0	0	1	0
D-A	D-M	0	1	0	0	1	1
A-D	M-D	0	0	0	1	1	1
D&A	D&M	0	0	0	0	0	0
D A	D M	0	1	0	1	0	1
a==0	a==1						

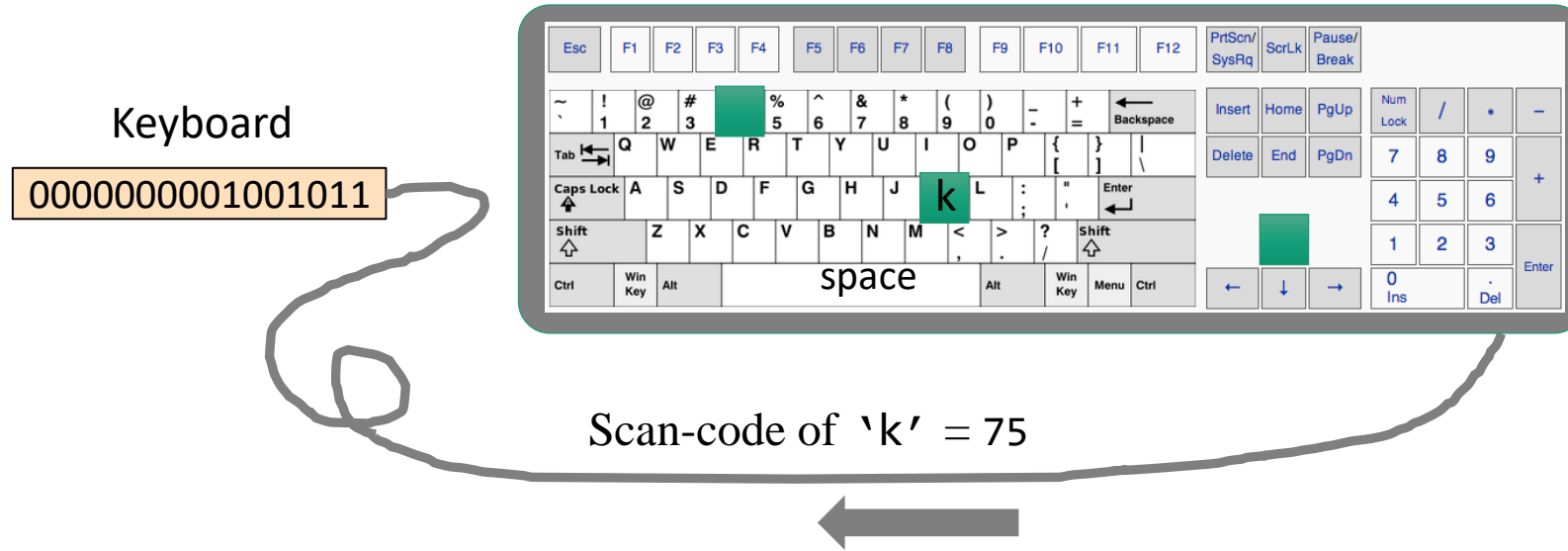
<i>dest</i>	d1	d2	d3	effect: the value is stored in:
null	0	0	0	The value is not stored
M	0	0	1	RAM[A]
D	0	1	0	D register
MD	0	1	1	RAM[A] and D register
A	1	0	0	A register
AM	1	0	1	A register and RAM[A]
AD	1	1	0	A register and D register
AMD	1	1	1	A register, RAM[A], and D register

<i>jump</i>	j1	j2	j3	effect:
null	0	0	0	no jump
JGT	0	0	1	if out > 0 jump
JEQ	0	1	0	if out = 0 jump
JGE	0	1	1	if out ≥ 0 jump
JLT	1	0	0	if out < 0 jump
JNE	1	0	1	if out ≠ 0 jump
JLE	1	1	0	if out ≤ 0 jump
JMP	1	1	1	Unconditional jump

# Memory mapped output



# Handle the keyboard



- To check which key is currently pressed:
  - Probe the contents of the Keyboard chip
  - In the Hack computer: probe the contents of **RAM[24576]**.

# Terminate a program

## Hack assembly code

```
// Program: Add2.asm
// Computes: RAM[2] = RAM[0] + RAM[1]
// Usage: put values in RAM[0], RAM[1]
0  @0
1  D=M  // D = RAM[0]

2  @1
3  D=D+M // D = D + RAM[1]

4  @2
5  M=D  // RAM[2] = D

6  @6
7  0; JMP
```

translate  
and  
load

- Jump to instruction number A (which happens to be 6)
- 0: syntax convention for jmp instructions

## Best practice:

To terminate a program safely, end it with an infinite loop.

## Memory (ROM)

0	@0
1	D=M
2	@1
3	D=D+M
4	@2
5	M=D
6	@6
7	0; JMP
8	
9	
10	
11	
12	
13	
14	
15	
	⋮
32767	

# Built-in symbols

The Hack assembly language features *built-in symbols*:

<u>symbol</u>	<u>value</u>	<u>symbol</u>	<u>value</u>
R0	0	SP	0
R1	1	LCL	1
...	...	ARG	2
R15	15	THIS	3
SCREEN	16384	THAT	4
KBD	24576		

- R0, R1 ,..., R15 : “virtual registers”, can be used as variables
- SCREEN and KBD : base addresses of I/O memory maps
- Remaining symbols: used in the implementation of the Hack virtual machine, discussed in chapters 7-8.



# Labels

```
0 // Program: Signum.asm
1 // Computes: if R0>0
2 //     R1=1
3 //     else
4 //     R1=0
5 // Usage: put a value in RAM[0],
6 //     run and inspect RAM[1].
7
8 @R0
9 D=M // D = RAM[0]
10
11 @POSITIVE
12 D;JGT // If R0>0 goto 8
13
14 @R1
15 M=0 // RAM[1]=0
16 @END
17 0;JMP // goto end
18
19 (POSITIVE)
20 @R1
21 M=1 // R1=1
22
23 (END)
24 @END // end
25 0;JMP
```

referring to a label

declaring a label

resolving labels

## Implications:

- Instruction numbers no longer needed in symbolic programming
- The symbolic code becomes *relocatable*.

Memory	
0	@0
1	D=M
2	@8 // @POSITIVE
3	D;JGT
4	@1
5	M=0
6	@10 // @END
7	0;JMP
8	@1
9	M=1
10	@10 // @END
11	0;JMP
12	
13	
14	
15	
	⋮
32767	

# Variables

```
// Program: Flip.asm  
// flips the values of  
// RAM[0] and RAM[1]
```

```
// temp = R1  
// R1 = R0  
// R0 = temp
```

```
@R1  
D=M  
@temp  
M=D      // temp = R1
```

```
@R0  
D=M  
@R1  
M=D      // R1 = R0
```

```
@temp  
D=M  
@R0  
M=D      // R0 = temp
```

```
(END)  
@END  
0;JMP
```

symbol used for  
the first time

symbol used  
again

resolving symbols

## Symbol resolution rules:

- A reference to a symbol without label declaration is treated as a reference to a variable.
- If the reference *@symbol* occurs in the program for first time, *symbol* is allocated to address **16** onward (say *n*), and the generated code is *@n*.
- All subsequent *@symbol* commands are translated into *@n*.

Note: variables are allocated to **RAM[16]** onward.

## Memory

0	@1
1	D=M
2	@16 // @temp
3	M=D
4	@0
5	D=M
6	@1
7	M=D
8	@16 // @temp
9	D=M
10	@0
11	M=D
12	@12
13	0;JMP
14	
15	
	⋮
32767	

# Iterative processing

## pseudo code

```
// Compute RAM[1] =  
1+2+ ... +RAM[0]  
n = R0  
i = 1  
sum = 0  
  
LOOP:  
  if i > n goto STOP  
  sum = sum + i  
  i = i + 1  
  goto LOOP  
  
STOP:  
  R1 = sum
```

## assembly code

```
// Compute RAM[1] = 1+2+ ... +n  
// Usage: put a number (n) in  
// RAM[0]  
@R0  
D=M  
@n  
M=D // n = R0  
@i  
M=1 // i = 1  
@sum  
M=0 // sum = 0  
  
(LOOP)  
@i  
D=M // D = i  
@n  
D=D-M // D = i - n  
@STOP  
D;JGT // if i > n goto STOP
```

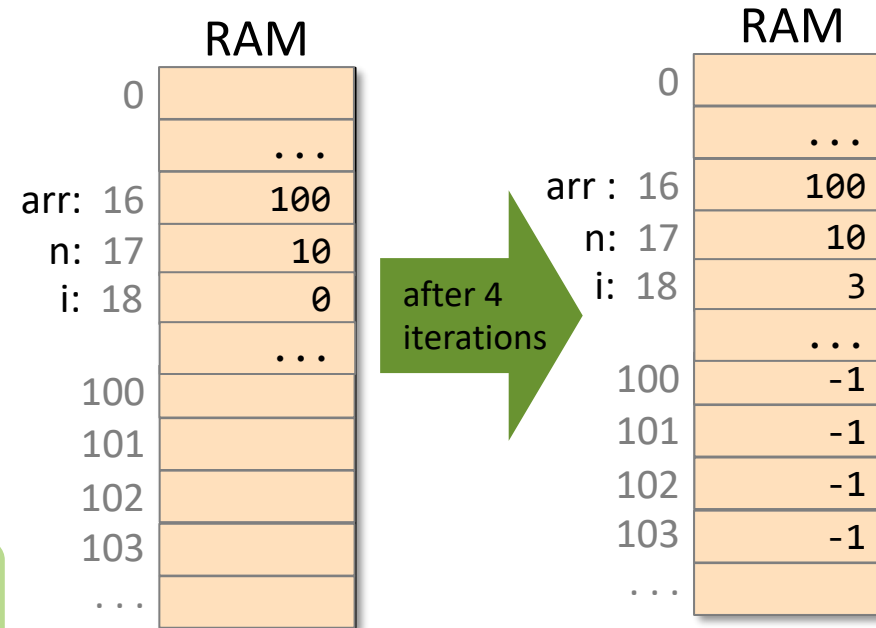
```
@sum  
D=M // D = sum  
@i  
D=D+M // D = sum + i  
@sum  
M=D // sum = sum + i  
@i  
M=M+1 // i = i + 1  
@LOOP  
0;JMP // goto LOOP  
  
(STOP)  
@sum  
D=M // D = sum  
@R1  
M=D // RAM[1] = sum  
  
(END)  
@END  
0;JMP // end
```

# Pointers

Example:

```
(LOOP)
  // if (i==n) goto END
  @i
  D=M // D = i
  @n
  D=D-M // D = i-n
  @END
  D;JEQ // if (i==n) goto END
  // RAM[arr+i] = -1
  @arr
  D=M // D = arr
  @i
  A=D+M // A = arr + i
  M=-1 // M[arr+i] = -1
  // i++
  @i
  M=M+1 // i = i + 1
  @LOOP
  0;JMP // goto LOOP
(END)
  @END
  0;JMP // END
```

typical pointer manipulation



- Pointers: Variables that store memory addresses (like arr).
- Pointers in Hack: Whenever we have to access memory using a pointer, we need an instruction like **A = expression**.
- Semantics:  
“set the address register to some value”.

# Outlines

- Hack assembly programming
- **Assembler**
- Virtual machine

# Translating A-instructions

## Symbolic syntax:

*@ value*

## Examples:

*@ 21*

*@foo*

Where *value* is either

- a non-negative decimal constant or
- a symbol referring to such a constant

## Binary syntax:

*0 valueInBinary*

## Example:

*00000000000010101*

## Translation to binary:

- If *value* is a decimal constant, generate the equivalent binary constant
- If *value* is a symbol, later.

# Translating C-instructions

Symbolic syntax:

*dest* = *comp* ; *jump*

Binary syntax:

1 1 1 a c1 c2 c3 c4 c5 c6 d1 d2 d3 j1 j2 j3

<i>comp</i>		c1	c2	c3	c4	c5	c6
0		1	0	1	0	1	0
1		1	1	1	1	1	1
-1		1	1	1	0	1	0
D		0	0	1	1	0	0
A	M	1	1	0	0	0	0
!D		0	0	1	1	0	1
!A	!M	1	1	0	0	0	1
-D		0	0	1	1	1	1
-A	-M	1	1	0	0	1	1
D+1		0	1	1	1	1	1
A+1	M+1	1	1	0	1	1	1
D-1		0	0	1	1	1	0
A-1	M-1	1	1	0	0	1	0
D+A	D+M	0	0	0	0	1	0
D-A	D-M	0	1	0	0	1	1
A-D	M-D	0	0	0	1	1	1
D&A	D&M	0	0	0	0	0	0
D A	D M	0	1	0	1	0	1
a=0	a=1						

<i>dest</i>	d1	d2	d3	effect: the value is stored in:
null	0	0	0	The value is not stored
M	0	0	1	RAM[A]
D	0	1	0	D register
MD	0	1	1	RAM[A] and D register
A	1	0	0	A register
AM	1	0	1	A register and RAM[A]
AD	1	1	0	A register and D register
AMD	1	1	1	A register, RAM[A], and D register

<i>jump</i>	j1	j2	j3	effect:
null	0	0	0	no jump
JGT	0	0	1	if out > 0 jump
JEQ	0	1	0	if out = 0 jump
JGE	0	1	1	if out ≥ 0 jump
JLT	1	0	0	if out < 0 jump
JNE	1	0	1	if out ≠ 0 jump
JLE	1	1	0	if out ≤ 0 jump
JMP	1	1	1	Unconditional jump

Symbolic:

Binary:

Example:

MD = D+1

1 1 1 0 0 1 1 1 1 1 0 1 1 0 0 0

# Hack language specification: symbols

## Pre-defined symbols:

<u>symbol</u>	<u>value</u>	<u>symbol</u>	<u>value</u>
R0	0	SP	0
R1	1	LCL	1
R2	2	ARG	2
...	...	THIS	3
R15	15	THAT	4
SCREEN	16384		
KBD	24576		

Label declaration:      *(label)*

Variable declaration:    *@variableName*

```
// Computes RAM[1]=1+...+RAM[0]
@i
M=1 // i = 1
@sum
M=0 // sum = 0

(LOOP)
@i // if i>RAM[0] goto STOP
D=M
@R0
D=D-M
@STOP
D;JGT
@i // sum += i
D=M
@sum
M=D+M
@i // i++
M=M+1
@LOOP // goto LOOP
0;JMP
...
```



# Outlines

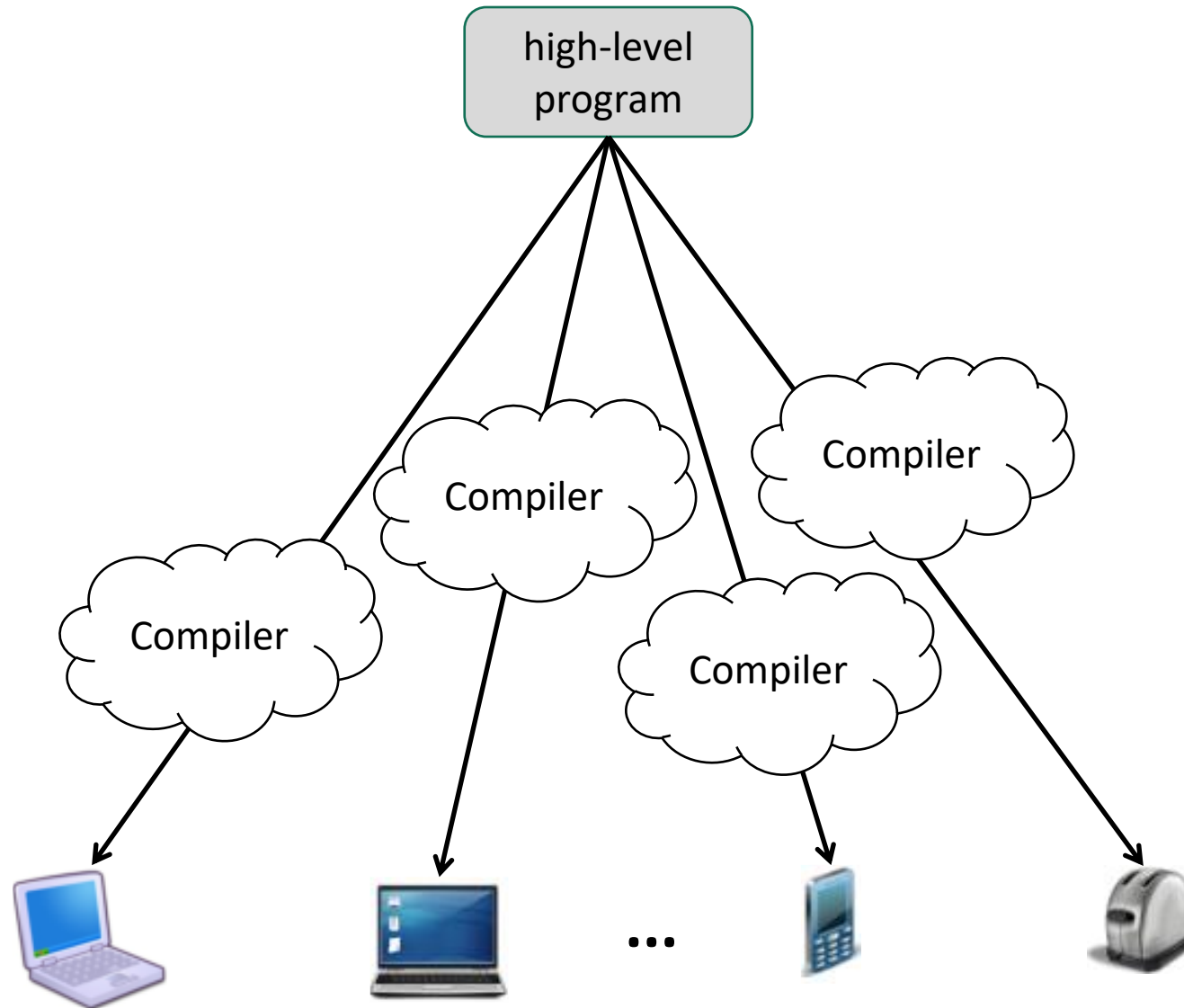
- Hack assembly programming
- Assembler
- Virtual machine

# Why we need virtual machine?

- **Code transportability**

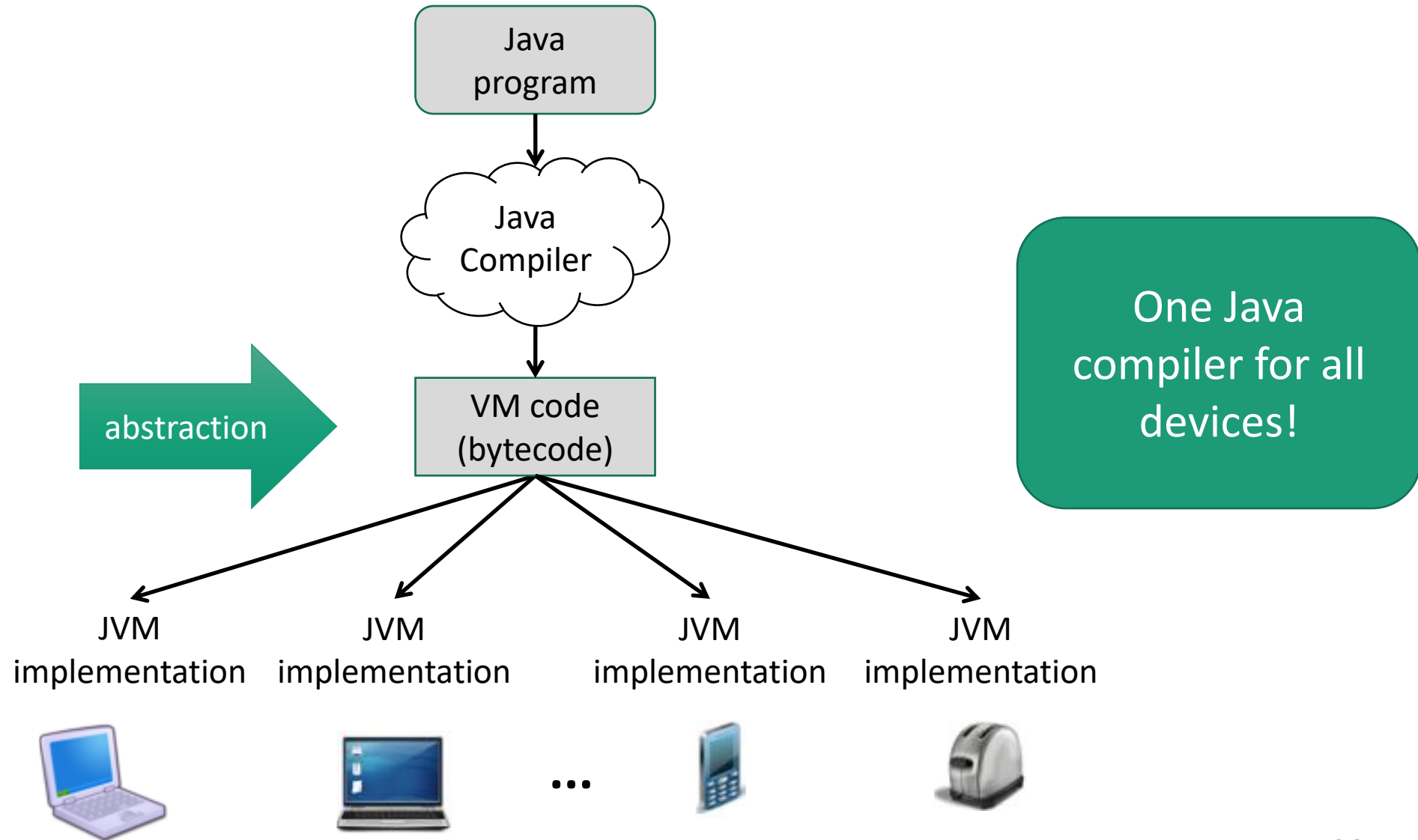
- **Many** high-level languages can work on the same platform: virtual machine.
- VM may be implemented with relative ease on **multiple** target platforms.
- As a result, VM-based software can run on **many** processors and operating systems without modifying source code.

# Program compilation: 1-tier



One compiler for  
each device!

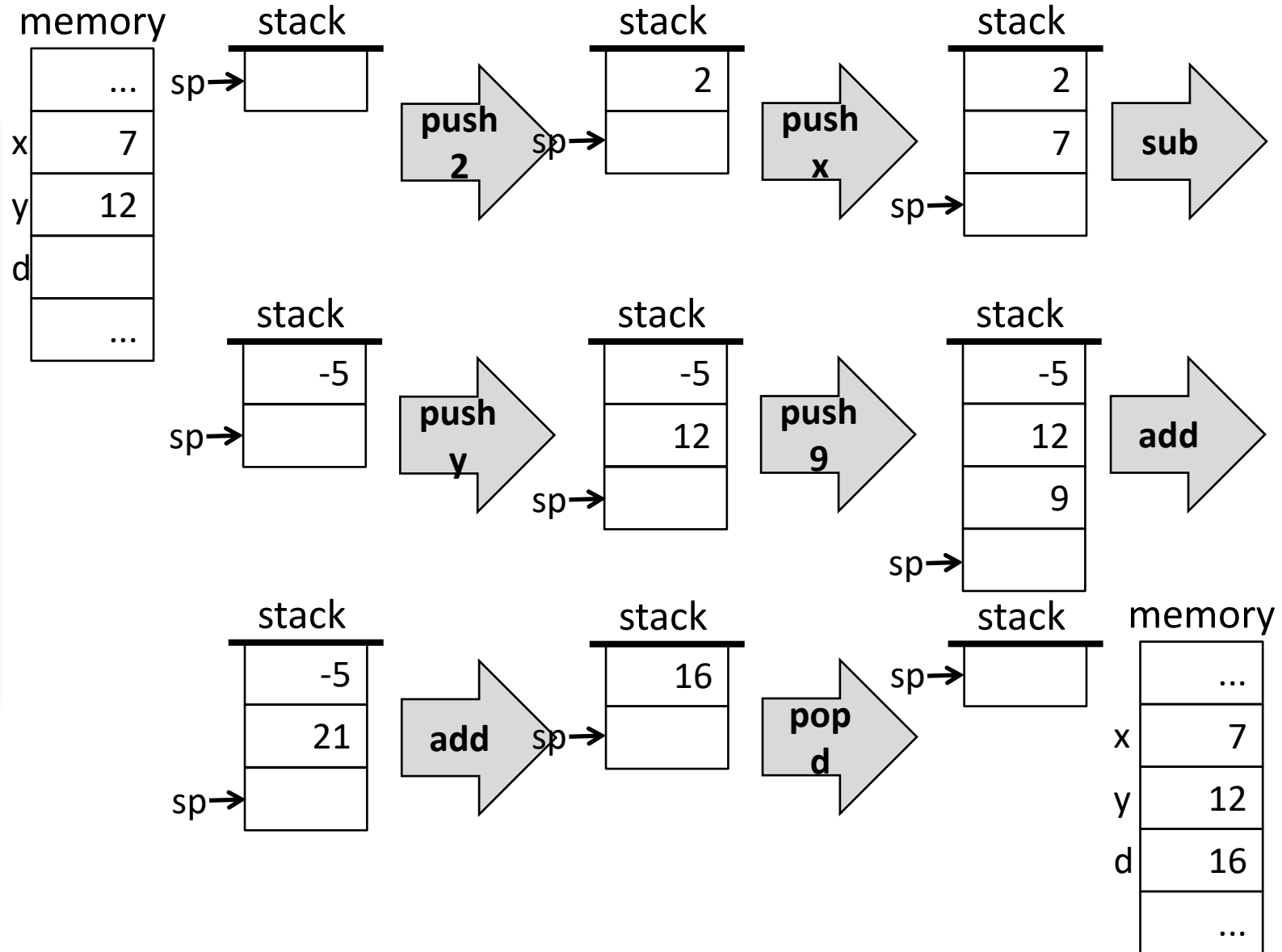
# Program compilation: 2-tier



# Arithmetic commands

VM code

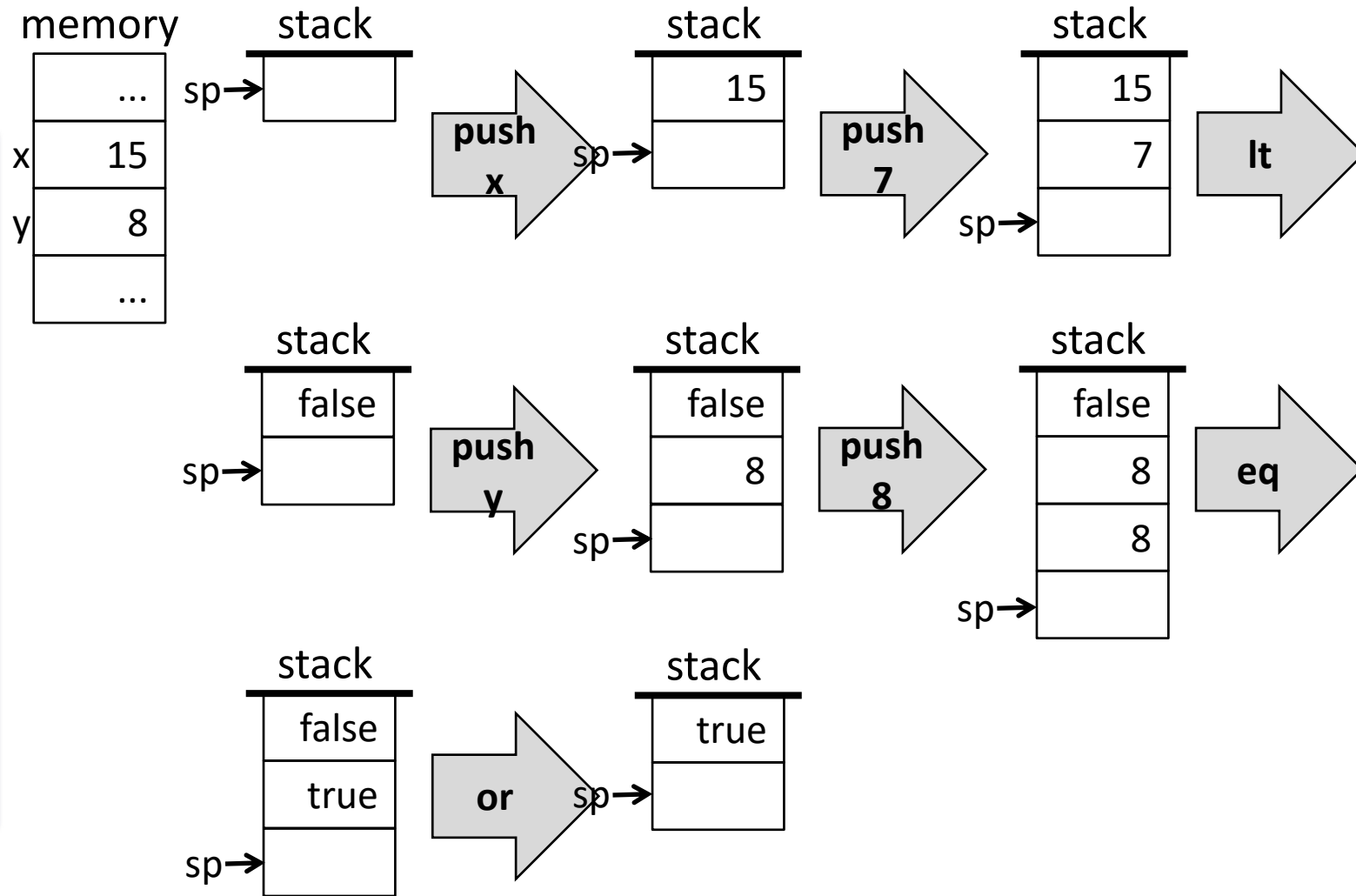
```
// d=(2-x) +  
// (y+9)  
push 2  
push x  
sub  
push y  
push 9  
add  
add  
pop d
```



# Logical commands

VM code

```
// (x<7)  
// or  
// (y==8)  
push x  
push 7  
lt  
push y  
push 8  
eq  
or
```



# Arithmetic / Logical commands

Command	Return value	Return value
add	$x + y$	integer
sub	$x - y$	integer
neg	$-y$	integer
eq	$x == y$	boolean
gt	$x > y$	boolean
lt	$x < y$	boolean
and	$x \text{ and } y$	boolean
or	$x \text{ or } y$	boolean
not	not $x$	boolean

Observation: Any arithmetic or logical expression can be expressed and evaluated by applying some sequence of the above operations on a stack.

# Pointer manipulation

## Pseudo assembly code

```
D = *p // D becomes 23
p--    // RAM[0] becomes 256
D = *p // D becomes 19

*q = 9 // RAM[1024] becomes 9
q++    // RAM[1] becomes 1025
```

### In Hack:

@p

A=M

D=M

## Notation:

\*p // the memory location that p points at

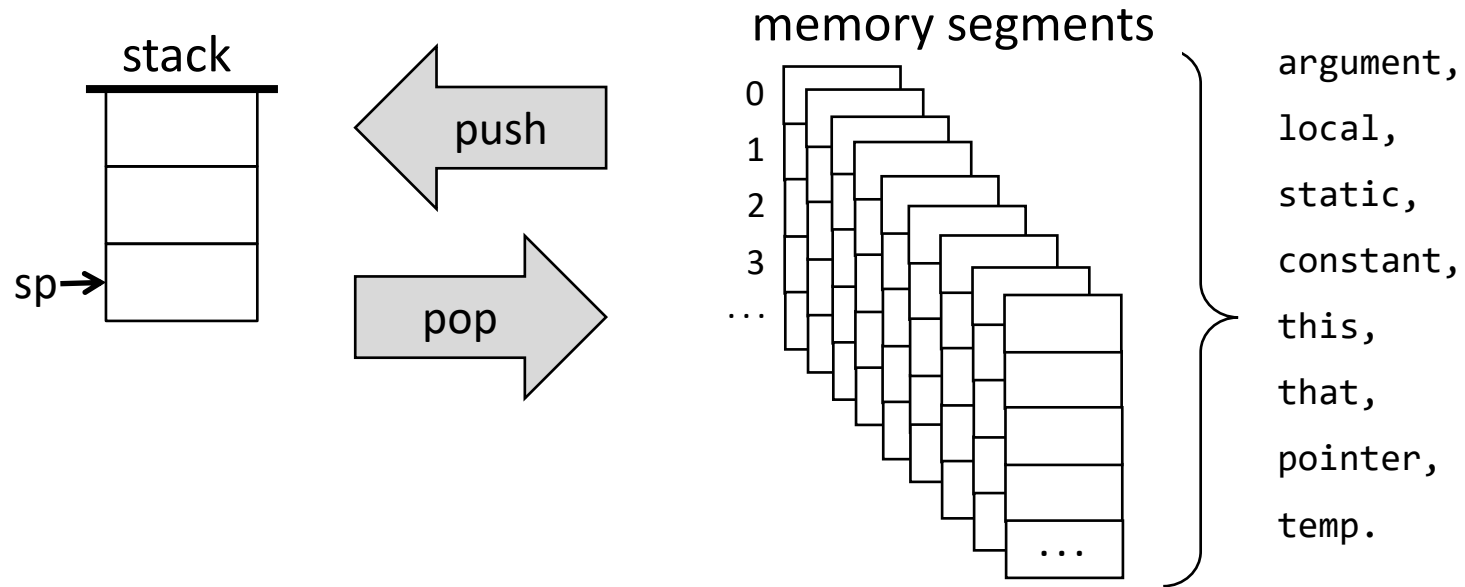
x-- // decrement:  $x = x - 1$

x++ // increment:  $x = x + 1$

RAM		
0	257	p
1	1024	q
2	1765	
...	...	
256	19	
257	23	
258	903	
...	...	
1024	5	
1025	12	
1026	-3	
...	...	



# Memory segments



Syntax: `push segment i`  
where *segment* is: argument, local, static, constant,  
this, that, pointer, or temp  
and *i* is a non-negative integer.

Syntax: `pop segment i`  
Where *segment* is: argument, local, static,  
this, that, pointer, or temp  
and *i* is a non-negative integer.

# Implement push constant $i$

VM code:

push constant  $i$

VM Translator

Assembly psuedo code:

$*SP = i, SP++$

(no pop constant operation)

Implementation:

Supplies the specified constant.

Hack assembly:

```
// D = i
@i
D=A
// *SP=D
@SP
A=M
M=D
// SP++
@SP
M=M+1
```

# Implement `pop local i`

## Abstraction

`pop local i`

## Implementation:

`addr=LCL+ i, SP--, *addr=*SP`

*i* is a constant here!!!  
but LCL is a variable.

## Hack assembly:

```
@i      // addr=LCL+i
D=A
@LCL
D=D+M
@addr
M=D
@SP      // SP--
M=M-1
@SP      // D=*SP
A=M
D=M
@addr    // *addr=D
A=M
M=D
```

# Implement push/pop local *i*

VM code:

```
pop local i
```

```
push local i
```

VM Translator

Assembly pseudo code:

```
addr = LCL + i, SP--, *addr = *SP
```

```
addr = LCL + i, *SP = *addr, SP++
```

Stack pointer

Base address of  
the local segment

Implementation:

The local segment  
is stored some-  
where in the RAM

RAM		
0	258	SP
1	1015	LCL
2		
...		
256	12	
257	5	
258		
...		
1015	...	
1016	...	
1017	...	
...		

Hack assembly:

```
// implement  
// push local i  
// addr=LCL+i  
@i  
D=A  
@LCL  
D=D+M  
@addr  
M=D
```

```
// *SP = *addr  
@addr // D=*addr  
A=M  
D=M  
@SP // *SP=D  
A=M  
M=D  
// SP++  
@SP  
M=M+1
```

# Implement push / pop local / argument / this / that *i*

VM code:

```
push segment i
```

```
pop segment i
```

VM translator

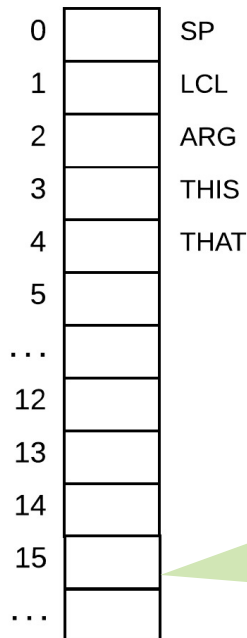
Assembly pseudo code:

```
addr = segmentPointer + i, *SP = *addr, SP++
```

```
addr = segmentPointer + i, SP--, *addr = *SP
```

*segment* = {local, argument, this, that}

Host RAM



base addresses of the four segments are stored in these pointers

the four segments are stored somewhere in the RAM

- push/pop local *i*
- push/pop argument *i*
- push/pop this *i*
- push/pop that *i*

implemented precisely the same way.

# Implement push/pop temp $i$

VM code:

push temp  $i$

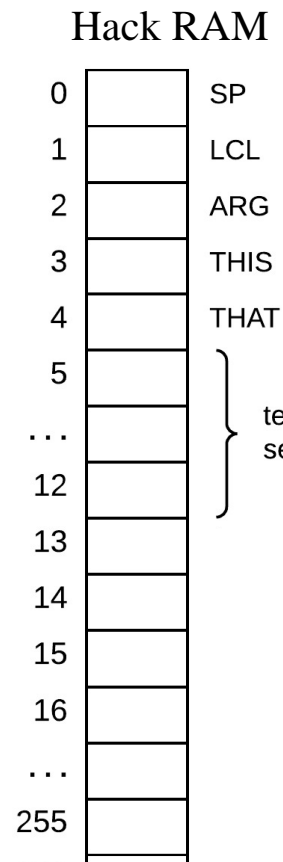
Assembly psuedo code:

addr =  $5 + i$ , \*SP = \*addr, SP++

VM Translator

pop temp  $i$

addr =  $5 + i$ , SP--, \*addr = \*SP



A fixed, **8-place** memory segment, stored in RAM locations 5 to 12

# Implement push/pop pointer 0/1

VM code:

push pointer 0/1

pop pointer 0/1

VM Translator

Assembly psuedo code:

\*SP = THIS/THAT, SP++

SP--, THIS/THAT = \*SP

A fixed, 2-place segment:

- accessing pointer 0 should result in accessing THIS
- accessing pointer 1 should result in accessing THAT

Implementation:

Supplies THIS or THAT // (the base addresses of this and that).

# Branching

- *goto label*
  - jump to execute the command just after *label*
- *if-goto label*
  - *cond* = pop
  - if *cond* jump to execute the command just after *label*
- *label label*
  - label declaration command
- Implementation (VM translation):
  - The assembly language has **similar branching commands**.



# Functions in VM language

```
// Computes 3 + 5 * 8
0 function main 0
1 push constant 3
2 push constant 8
3 push constant 5
4 call mult 2
5 add
6 return
```

caller

```
// Computes the product of two given arguments
0 function mult 2
1 push constant 0
2 pop local 0
3 push constant 1
4 pop local 1
5 label LOOP
6 push local 1
7 push argument 1
  //... computes the product into local 0
19 label END
20 push local 0
21 return
```


callee

## Implementation

We can write low-level code to

- Handle the VM command call
- Handle the VM command function
- Handle the VM command return.

# Functions in VM language



```
// Computes 3 + 5 * 8
0 function main 0
1 push constant 3
2 push constant 8
3 push constant 5
4 call mult 2
5 add
6 return
```

caller

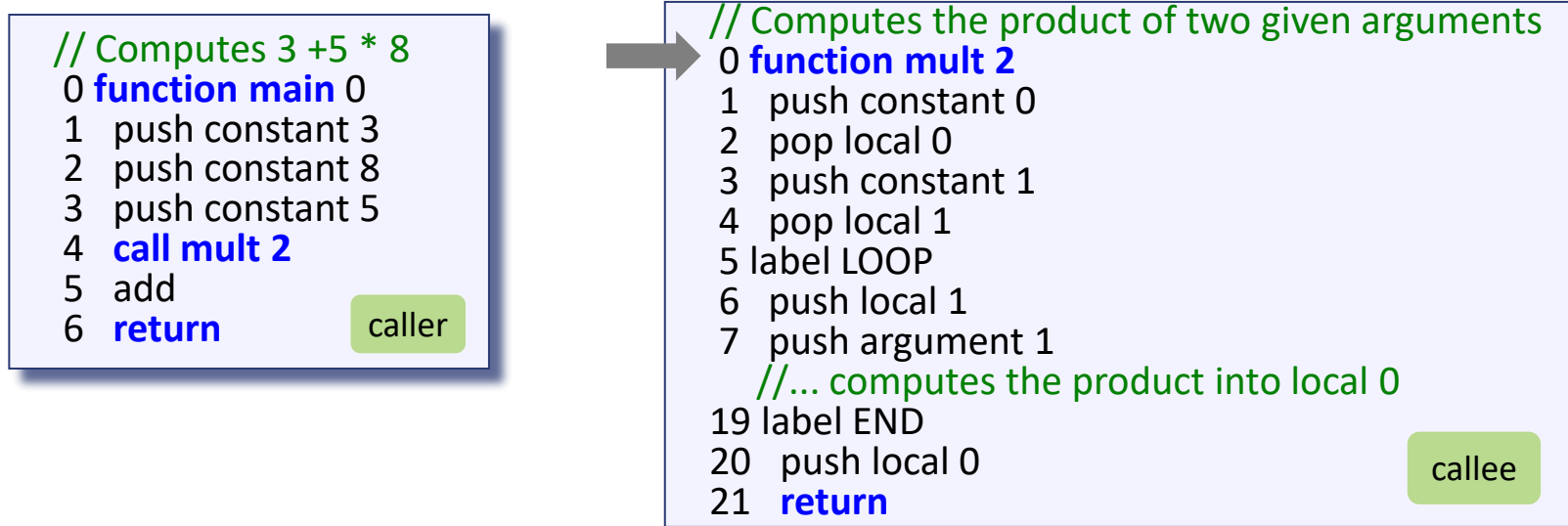
```
// Computes the product of two given arguments
0 function mult 2
1 push constant 0
2 pop local 0
3 push constant 1
4 pop local 1
5 label LOOP
6 push local 1
7 push argument 1
  //... computes the product into local 0
19 label END
20 push local 0
21 return
```

callee

## Handling call:

- Determine the **return address** within the caller's code;
- **Save** the caller's return address, stack and memory segments;
- **Pass parameters** from the caller to the callee;
- **Jump** to execute the callee.

# Functions in VM language



## Handling function:

- Initialize the local variables of the callee;
- Handle some other simple initializations (later);
- Execute the callee function.

# Functions in VM language

```
// Computes 3 + 5 * 8
0 function main 0
1 push constant 3
2 push constant 8
3 push constant 5
4 call mult 2
5 add
6 return
```

caller

```
// Computes the product of two given arguments
0 function mult 2
1 push constant 0
2 pop local 0
3 push constant 1
4 pop local 1
5 label LOOP
6 push local 1
7 push argument 1
  //... computes the product into local 0
19 label END
20 push local 0
21 return
```

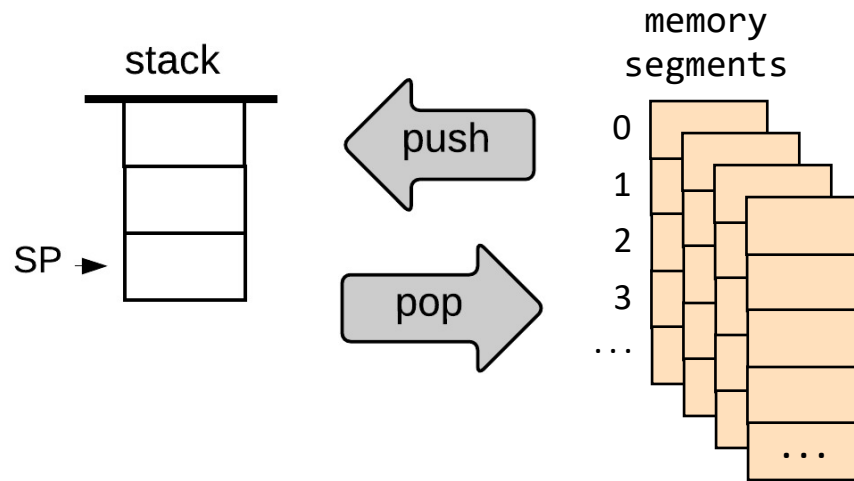
callee

## Handling return:

(a function always ends by pushing a return value on the stack)

- **Return** the *return value* to the caller;
- **Recycle** the memory resources used by the callee;
- **Reinstate** the caller's stack and memory segments;
- **Jump** to the return address in the caller's code.

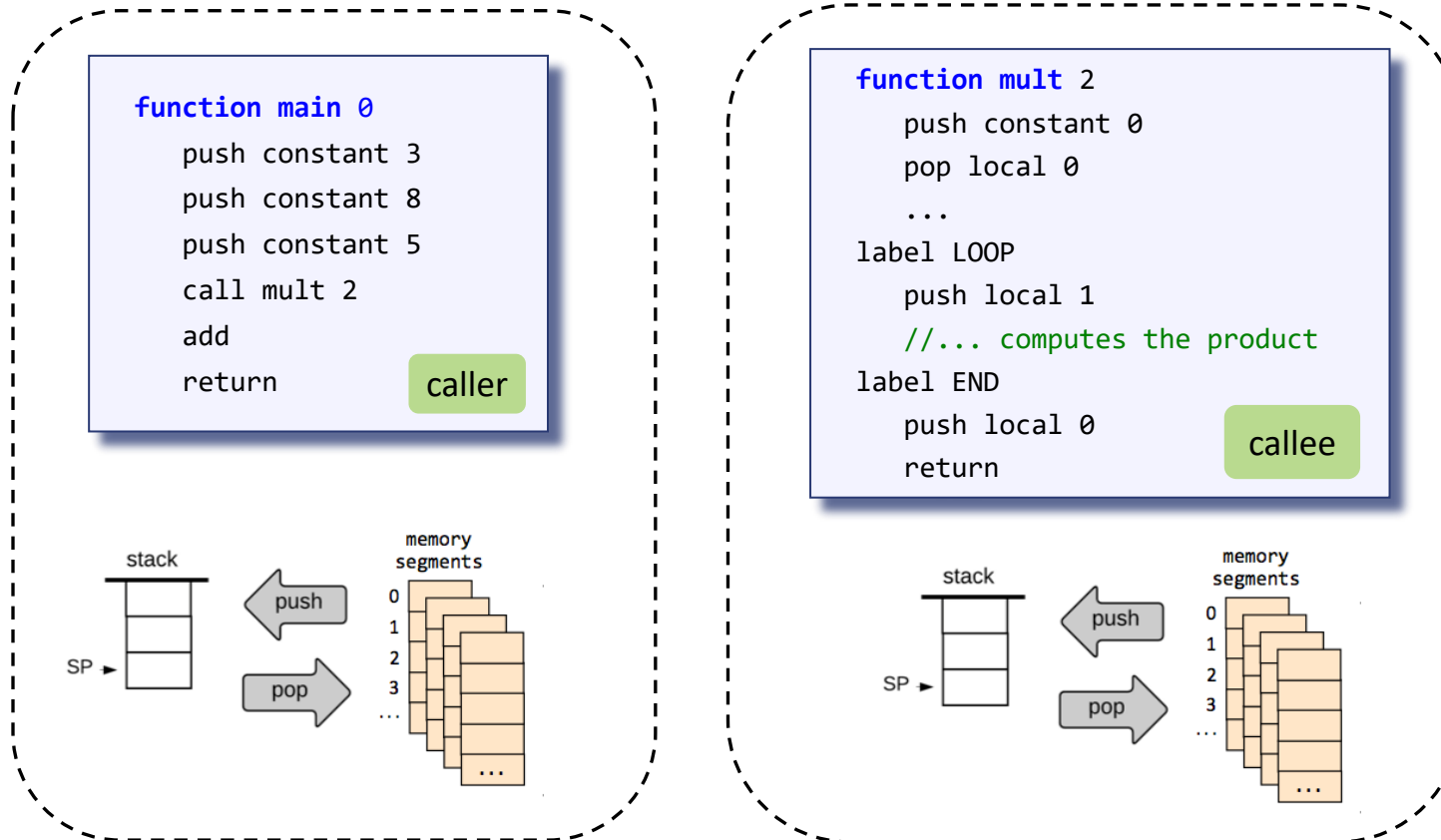
# The function's state



## During run-time:

- Each function uses a **working stack** + **memory segments**
- The working stack and some of the segments should be:
  - Created when the function starts running,
  - Maintained as long as the function is executing,
  - Recycled when the function returns.

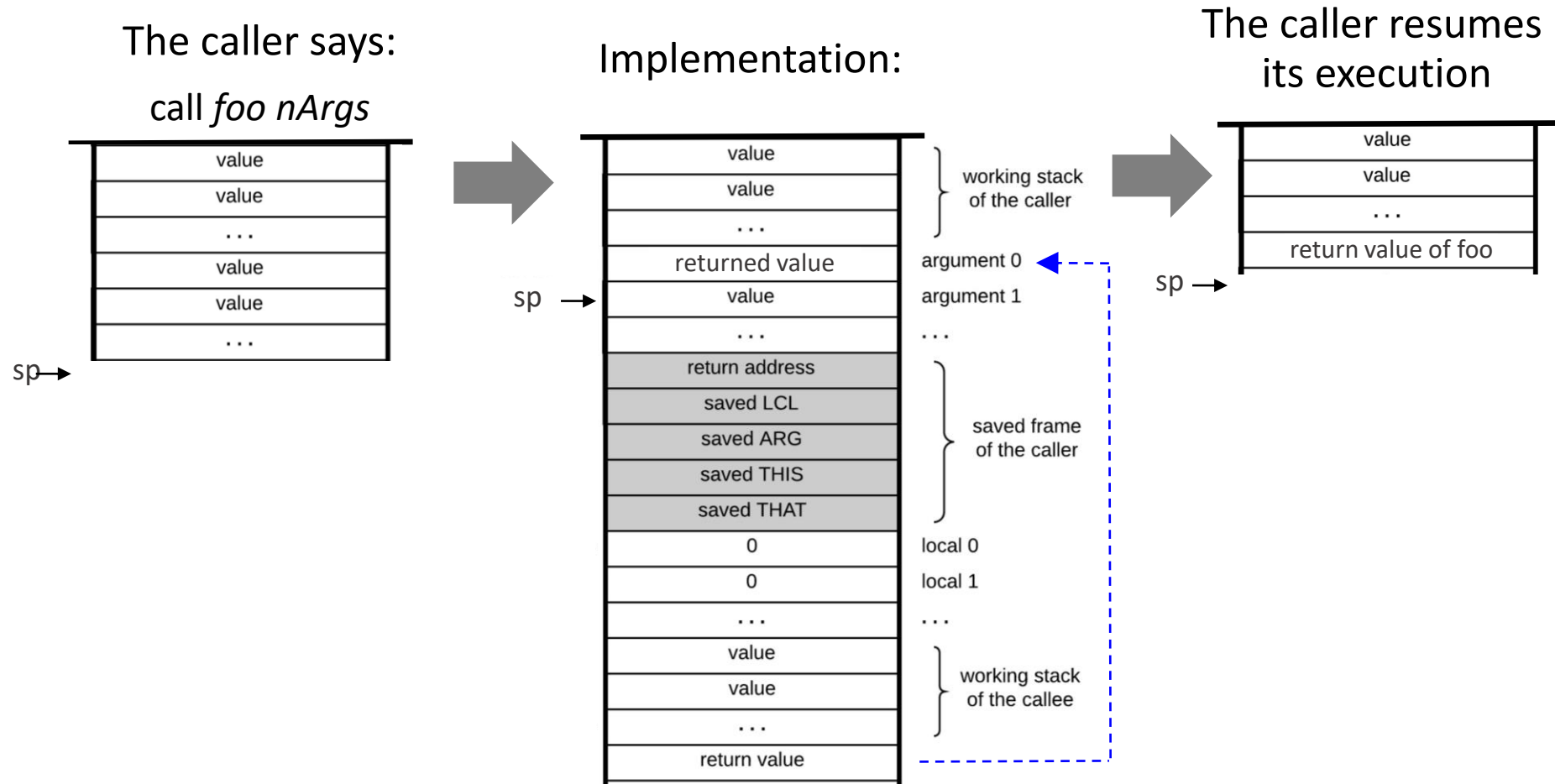
# The function's state



## Challenge:

- Maintain the states of all the functions up the calling chain.
- Can be done by using a single **global stack**.

# Recap: function call and return



# Final remark

- Be sure that you know how to program in hack assembly language.
- Be sure that you know how to translate hack assembly codes into binary machine codes.
- Be sure that you know how to perform stack operations in VM. (VM abstraction)
- Be sure that you know how to program in VM code. (VM abstraction)
- Be sure that you know how to translate VM codes to hack assembly codes. (VM implementation)
- Make sure that you understand all the **examples**, **exercises** and **quizes** given in the lecture slides.