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**Nottingham**

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# Computer Performance

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**2023 Spring Semester**  
**COMP1047 Systems & Architecture**



- **Timing Performance**
- **Other Performance Metrics**







# Response Time and Throughput

- Response time (execution time)
  - The **total time** for the computer to complete a task
- Throughput (bandwidth)
  - The **number of tasks** completed per unit time
- How are response time and throughput affected?
  - Replacing the processor with a faster version?
    - Improves both response time and throughput
  - Adding more processors?
    - Improves throughput
- Our focus will be on response time



- Response time (Elapsed Time)
  - **Total time** to complete a task, including all aspects:
  - Disk accesses, memory accesses, I/O activities, CPU time, etc.
- CPU execution time (CPU time)
  - The **actual time the CPU spends** computing a specific task
  - Does not include time spent waiting for I/O or running other programs
  - Can be further divided into
    - User CPU time: the CPU time spent in a program itself
    - System CPU time: the CPU time spent in the OS performing tasks on behalf of the program



# Relative Performance

- To maximize performance, we want to minimize execution time, then we can relate performance and execution time for a computer X as

$$\text{Performance}_X = 1 / \text{Execution\_Time}_X$$

- Computer X is  $n$  times faster than computer Y, then their relative performance  $n$  is

$$\begin{aligned} n &= \text{Performance}_X / \text{Performance}_Y \\ &= \text{Execution\_Time}_Y / \text{Execution\_Time}_X \end{aligned}$$

- **Question: If Computer A runs a program in 10 secs and Computer B runs the same program in 15 secs, which one is faster? And by how much?**



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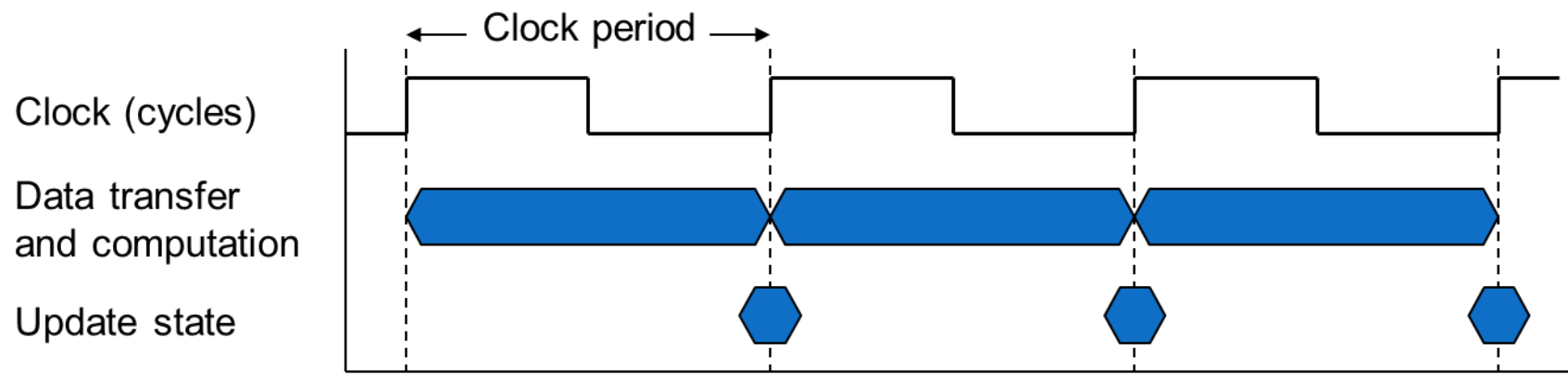
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- **Question: If Computer A runs a program in 10 secs and Computer B runs the same program in 15 secs, which one is faster? And by how much?**
- **Computer A is 1.5 times as fast as Computer B**

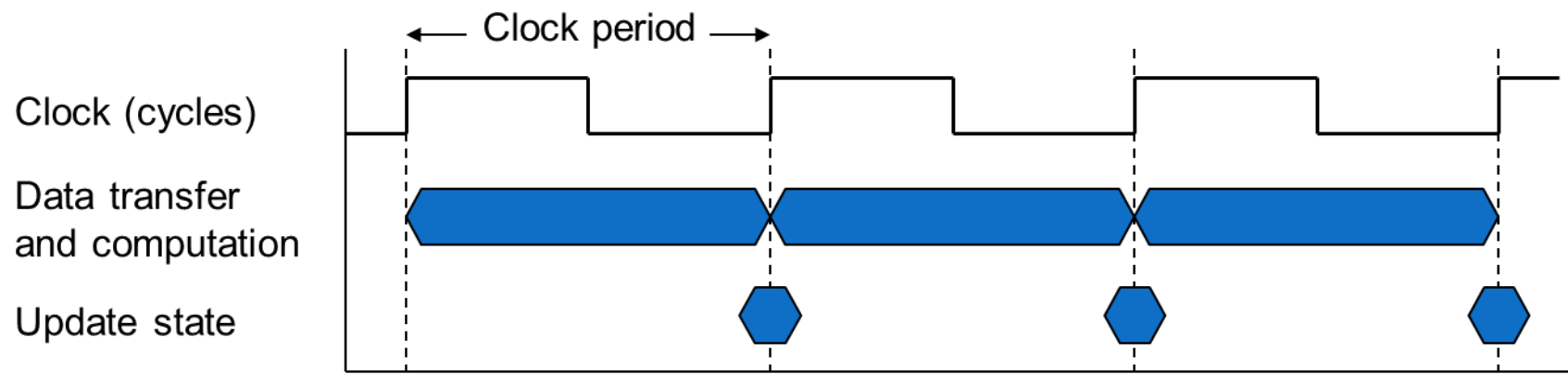
# CPU Clocking

- Computers are constructed using a clock that determines when events take place in hardware
- The clock signal is produced by an external oscillator circuit that generates a consistent number of pulses each second in the form of a periodic square wave
- **One clock cycle (clock tick): the unit of the CPU clock. It must be constant as CPU clock runs.**
- **Clock period: the time spend to run one clock cycle.**



# CPU Clocking

- **One clock cycle (clock tick):** the unit of the CPU clock. It must be constant as CPU clock runs.
  - e.g.  $250\text{ps} = 0.25\text{ns} = 250 \times 10^{-12}\text{s}$  (ps: picosecond)
- **Clock frequency (clock rate):** cycles per second, which is the inverse of the clock period
  - e.g.  $4.0\text{GHz} = 4000\text{MHz} = 4.0 \times 10^9\text{Hz}$
  - **Clock frequency =  $1/\text{Clock period}$**







- A simple formula relates CPU clock cycles and CPU clock period to CPU time

$$\begin{aligned}\text{CPU Time} &= \text{CPU Clock Cycles} \times \text{Clock Period} \\ &= \frac{\text{CPU Clock Cycles}}{\text{Clock Rate}}\end{aligned}$$

- The performance can be improved by
  - Reducing number of clock cycles
  - Increasing clock rate
  - But they can not be altered arbitrarily – needs to adhere to circuit limitations.



# CPU Time Example

- Computer A: 2GHz clock, 10s CPU time to run a program.
- Build Computer B
  - Aim for 6s CPU time to run the same program
  - Can do a faster clock, but it requires 1.2 times as many clock cycles as computer A  
( $\text{Clock Cycles}_B = 1.2 \times \text{Clock Cycles}_A$ )
- **Question: What clock rate should we tell the designer to target on Computer B?**



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- **Question: What clock rate should we tell the designer to target on Computer B?**

$$\begin{aligned}\text{Clock Rate}_B &= \frac{\text{Clock Cycles}_B}{\text{CPU Time}_B} \\ \text{Clock Cycles}_A &= \text{CPU Time}_A \times \text{Clock Rate}_A \\ &= 10\text{s} \times 2\text{GHz} = 20 \times 10^9 \\ \text{Clock Rate}_B &= \frac{1.2 \times 20 \times 10^9}{6\text{s}} = \frac{24 \times 10^9}{6\text{s}} = 4\text{GHz}\end{aligned}$$

- The computer need to execute the instructions to run the program, and the execution time should depend on the number of instructions in a program
- **Clock cycles per instruction (CPI)**: the average number of clock cycles each instruction takes to execute
- The number of clock cycles required for a program is

$$\text{CPU Clock Cycles} = \text{Instruction Count} \times \text{CPI}$$

- The instruction count for a program
  - Determined by program, ISA and compiler
- CPI
  - Determined by how you design the CPU

```
hanoi:    addi $a0, $a0, -1
          bne  $a0, $zero, hanoi_1
          addi $v0, $zero, 1
          j    return
hanoi_1:  jal  hanoi
          sll  $v0, $v0, 1
          addi $v0, $v0, 1
return:   jr   $ra
```



# The Classic CPU Performance Equation

$$\begin{aligned}\text{CPU Time} &= \text{CPU Clock Cycles} \times \text{Clock Period} \\ &= \frac{\text{CPU Clock Cycles}}{\text{Clock Rate}}\end{aligned}$$

$$\text{CPU Clock Cycles} = \text{Instruction Count} \times \text{CPI}$$

Use **Instruction Count**, **CPI**, **Clock Period** or **Clock Rate** to describe the **CPU Time**

$$\begin{aligned}\text{CPU Time} &= \text{Instruction Count} \times \text{CPI} \times \text{Clock Period} \\ &= \frac{\text{Instruction Count} \times \text{CPI}}{\text{Clock Rate}}\end{aligned}$$



# CPI Example

- Two computers
  - Computer A: Clock Period = 250ps, CPI = 2.0
  - Computer B: Clock Period = 500ps, CPI = 1.2
  - Same ISA
- **Which computer is faster, and by how much?**

$$\begin{aligned}\text{CPU Time}_A &= \text{Instruct. Count} \times \text{CPI}_A \times \text{Clock Period}_A \\ &= C \times 2.0 \times 250\text{ps} = C \times 500\text{ps}\end{aligned}$$

$$\begin{aligned}\text{CPU Time}_B &= \text{Instruct. Count} \times \text{CPI}_B \times \text{Clock Period}_B \\ &= C \times 1.2 \times 500\text{ps} = C \times 600\text{ps}\end{aligned}$$

$$\frac{\text{CPU Time}_B}{\text{CPU Time}_A} = \frac{C \times 600\text{ps}}{C \times 500\text{ps}} = 1.2$$

**A is faster**

**A is 1.2 times as fast as B**



- Typically different instruction classes take different numbers of cycles

$$\text{Clock Cycles} = \sum_{i=1}^n (\text{CPI}_i \times \text{Instruction Count}_i)$$

- **Average CPI**

$$\text{CPI} = \frac{\text{Clock Cycles}}{\text{Instruction Count}} = \sum_{i=1}^n \left( \text{CPI}_i \times \underbrace{\frac{\text{Instruction Count}_i}{\text{Instruction Count}}}_{\text{Relative Frequency}} \right)$$



## Exercise

- A compiler designer is trying to decide between two code sequences for a particular computer. The CPI for each instruction class and the instruction counts for each instruction class are given as

Class	A	B	C
CPI for class	1	2	3
IC in sequence 1	2	1	2
IC in sequence 2	4	1	1

- Question: What is the average CPI for each sequence?**



## Exercise

- A compiler designer is trying to decide between two code sequences for a particular computer. The CPI for each instruction class and the instruction counts for each instruction class are given as

Class	A	B	C
CPI for class	1	2	3
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- Question: What is the average CPI for each sequence?**
  - Sequence 1: instruction count = 5
    - Clock Cycles  
 $= 1 \times 2 + 2 \times 1 + 3 \times 2$   
 $= 10$
    - Avg. CPI =  $10/5 = 2.0$
  - Sequence 2: instruction count = 6
    - Clock Cycles  
 $= 1 \times 4 + 2 \times 1 + 3 \times 1$   
 $= 9$
    - Avg. CPI =  $9/6 = 1.5$



# Performance Summary

- The basic components of performance and how each is measured

Components of performance	Units of measure
CPU execution time for a program	Seconds
Instruction count	Instructions executed for the program
Clock cycles per instruction (CPI)	Average number of clock cycles per instruction
Clock cycle time (period)	Seconds per clock cycle

- The big picture

$$\text{CPU Time} = \text{Instruction Count} \times \text{CPI} \times \text{Clock Period}$$



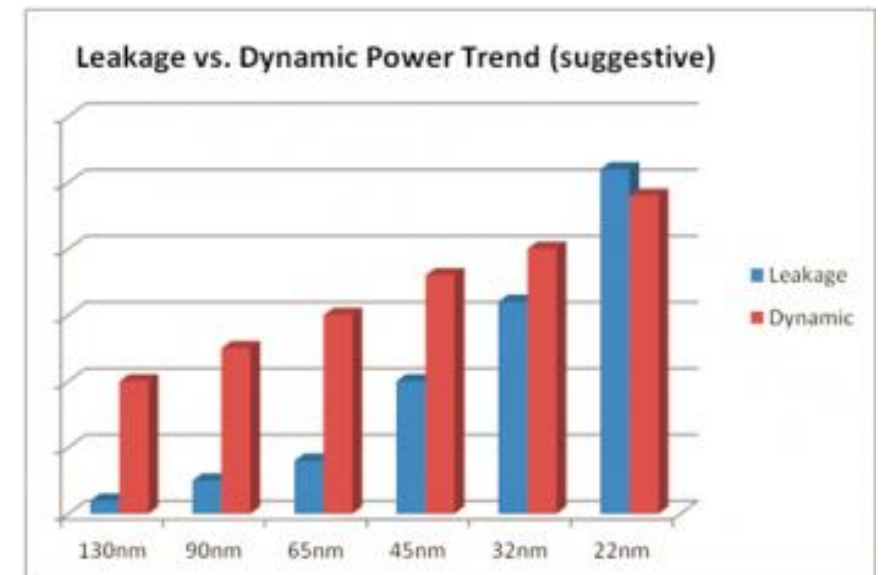


The performance of a program may depend on a series of hardware or software components

- Program
  - Affects instruction count
  - Possibly affects CPI – by favoring slower or faster instructions
- Programming language
  - Affects instruction count
  - Affects CPI – because of its own features
- Compiler
  - Affects instruction count
  - Affects CPI
- ISA
  - Affects instruction count
  - Affects CPI, clock rate

## Power & Energy

- Dynamic power:  $P = 0.5 * CV^2f$ 
  - C: effective capacitance
  - V: voltage
  - f: frequency, usually linear with V
- Doubling the clock frequency consumes more power than a quadcore processor!
- Static/Leakage power becomes the dominant factor in the most advanced process technologies.
- Power is the direct contributor of “heat”
  - Packaging of the chip
  - Heat dissipation cost
- Dynamic energy =  $P * t$ 
  - Battery life is related to energy
  - Lower power does not necessarily mean better battery life



## Bandwidth

- The amount of work (or data) during a period of time
  - Network or Disks: MB/sec, GB/sec, Gbps, Mbps
  - Game or Video: Frames per second
- Also called “throughput”, but with subtle differences
- “Work done” / “execution time”

## Reliability

- Mean time to failure (MTTF)
  - Average time before a system stops working
  - Very complicated to calculate for complex systems
- Hardware can fail because of
  - Electromigration
  - Temperature
  - High-energy particle strikes



- Concepts of and basic factors that affect response time and bandwidth.
- Relative performance that is used to compare performance of different computers.
- Concepts and calculation of CPU time related factors.
- Concepts and calculation of CPI related factors.
- Knowledge of other performance metrics.



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